

SELF-CONSOLIDATING CONCRETE FOR PRECAST, PRESTRESSED CONCRETE BRIDGE ELEMENTS

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Abstract

The following thesis presents the results of four full scale beams tests as part of a research program conducted at McGill University. The purpose is to study the applicability of existing design provisions, in the American Association of State Highway and Transportation Officials (AASHTO) specifications, for the use of self-consolidating concrete (SCC) in precast pretensioned bridge girders.

The test specimens had an overall length of 31 ft (9.4m) with a center-to-center span of 29 ft (8.8m). They were cast in four batches with different concrete attributes: two non air-entrained SCC mixtures and two high-performance concretes. For each type, compressive strengths of 8,000 and 10,000 psi (55.2 and 69 MPa) with release strengths of 5,000 and 6,250 psi (34.5 and 43 MPa) at 18 hours, respectively, were tested. Each girder was prestressed with eight Grade 270 seven-wire low-relaxation prestressing strands of 0.6 in (15.2 mm) diameter. Six of the strands were straight and two were harped twice, 4'-11" (1.5 m) from mid-span. The specimens were supported on neoprene bearing pads at their ends, and were tested with two equal point loads located 4'-11" (1.5 m) from mid-span.

This research project demonstrated that the shear failure of the girders exceeded the predicted nominal shear resistance given by the 2004 AASHTO Specifications. The experimental flexural resistance also exceeded the predicted nominal resistance.

Résumé

Le présent mémoire expose les résultats de quatre poutres pleine grandeur faisant partie intégrante d'une étude effectuée à l'Université McGill. Le but de cette étude est de valider l'applicabilité des provisions de conception existantes, de l'Association Américaine des Autoroutes d'État et des Officiers de Transport (norme AASHTO), pour l'usage de béton autoplaçant (BAP) dans les poutres précontraintes et préfabriquées de ponts.

Les spécimens testés ont une longueur maximale de 31 pieds (9.4 m) avec une distance du centre au centre de 29 pieds (8.8 m). Les poutres ont été coulées une à la fois avec différentes sortes de béton: deux d'entre-elles à partir de béton autoplaçant sans air entrappé, et deux avec du béton haute-performance. Pour chaque sorte, une résistance compressive de 8,000 et 10,000 psi (55.2 et 69 MPa) avec une résistance, avant de précontraindre le béton, de 5,000 et 6,250 psi (34.5 et 43 MPa) à 18 heures, respectivement, ont été testées. Chaque poutre était précontrainte avec huit tendons, grade 270, de 0.6 in (15.2 mm) de diamètre. Six de ces tendons étaient horizontaux alors que deux étaient inclinés 59 pouces (1.5 m) de chaque bord de l'axe central. Les spécimens étaient supportés aux deux extrémités sur des pads de néoprène et étaient testés avec deux charges concentriques situées 59 pouces (1.5 m) de l'axe central.

Cette recherche a démontré que la capacité en cisaillement des poutres testées excédait les valeurs nominales prévues par les normes AASHTO 2004. Les valeurs expérimentales de la résistance à la flexion des poutres aussi excèdent les valeurs nominales prédites.

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Chapter 1: Introduction and Literature review

The purpose of this thesis is to study the applicability of existing design provisions, in the American Association of State Highway and Transportation Officials (AASHTO) specifications, for the use of self-consolidating concrete (SCC) in precast pretensioned bridge girders. The research program consisted of the construction and testing of four full-scale precast, prestressed bridge girders with selected Self-Consolidating Concrete (SCC) mixtures and companion high performance concrete (HPC) specimens. This thesis provides both SI Units and U.S. Customary Units due to the fact that the research was carried out for the U.S. National Cooperative Highway Research Program (NCHRP).

1.1 Chapter overview

This chapter presents a review of the literature regarding the various topics that will be studied in this thesis.

The literature review will begin with a brief history describing the developments in understanding of shear behaviour and the relevant codes of practice (see Section 1.2).

Section 1.3 will summarize the benefits of prestressing, and will discuss the codes and standards used for design.

Section 1.4 describes the precasting operations: history, benefits and tradeoffs.

Section 1.5 introduces the concept of Self-Consolidating Concrete (SCC).

Finally, Section 1.6 presents the different objectives of the research program.

1.2 Shear design

This report reviews the literature on the shear problem in reinforced and prestressed concrete beams, with particular attention devoted to beams constructed with HPC. Section 1.2.1 reviews the historical development of the research; Section 1.2.2 presents the 318-08 ACI Code (ACI 318 2008); and Section 1.2.3 covers the 2004 AASHTO LRFD (AASHTO 2004) bridge design specifications. Section 1.2.4 summarizes a study comparing the ACI code approach to that used in the AASHTO LRFD specifications.

1.2.1 History behind the shear design

In the early ages of reinforced concrete studies, pioneers developed two mechanisms for estimating shear failures in reinforced concrete members. The first mechanism considered horizontal shear as the basic cause of shear failures (ACI-ASCE Committee 326, 1962). This seemed a reasonable approach at the time when engineers and researchers were familiar with the action of web rivets in steel girders and shear-keys in wooden beams, for which shearing stresses were computed using the classical equation:

$$v = \frac{VQ}{Ib} \quad \text{Eq. 1}$$

Where:

v = Unit horizontal shear stress at a distance y from the neutral axis

V = Total vertical shear at the section

Q = First moment of the part of the cross-sectional area cut off at distance y from the neutral axis, with respect to the neutral axis

I = Moment of inertia of the cross-sectional area with respect to the neutral axis

b = Width of the cross section at a distance y from the neutral axis

Reinforced concrete beams were tested as an extension of the older materials assuming that the concrete could only resist low horizontal shearing stresses, and that vertical stirrups acted as shear-keys for higher shearing stresses.

The second mechanism considered diagonal tension as the basic cause of shear failures (ACI-ASCE Committee 326, 1962). In 1899, W. Ritter presented a clear explanation of the diagonal tension using a 45° truss model (Collins and Mitchell, 1997). He stated that stirrups resisted tension not horizontal shear, and suggested that the design of stirrups for vertical shear be determined from the following expression:

$$V = \frac{A_v f_v j d}{s} \quad \text{Eq. 2}$$

Where:

A_v = Total cross-sectional area of one stirrup

f_v = Allowable stress in the stirrups

jd = Internal moment arm

s = Spacing of stirrups in the direction of the axis of the member

Ritter's design expression for vertical stirrups is identical to that appearing in modern design specifications of most countries.

Discussions between the proponents of horizontal shear and diagonal tension continued for nearly a decade until laboratory tests resolved the issue mainly through the efforts of E. Mörsch in Germany. He pointed out that, if a state of pure shear stress exists, then a tensile stress of equal magnitude must exist on a 45-degree plane (ACI-ASCE Committee 326, 1962). Mörsch explained Ritter's model in more detail. He also predicted that the shear stress would reach its maximum value at the neutral axis and would remain constant from the neutral axis down to the flexural steel (Figure 1). The value of the maximum shear stress was evaluated by:

$$v = \frac{V}{bjd} \quad \text{Eq. 3}$$

Where:

V = Shear in beam

b = Width of rectangular section

d = Effective depth to center of gravity or reinforcement

j = Ratio of lever arm of tensile reinforcement to effective depth to steel computed by straight-line theory for ordinary reinforced concrete beams

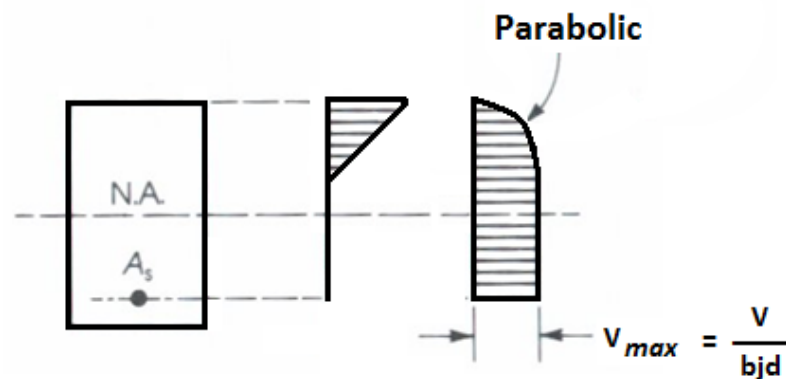


Figure 1: Stress distribution in a reinforced concrete beam containing flexural cracks
[Adapted from Collins and Mitchell, 1997)]

Succeeding papers by Mörsch in 1906 and 1907 (ACI-ASCE Committee 326, 1962) explained the diagonal tension mechanism and listed the following arguments against the horizontal shear concept:

- 1- The ultimate minimal shearing stresses in beams without web reinforcement, as computed by Eq. 3, are close to the tensile strength of concrete. Punching tests, on the other hand, indicate that the shearing strength of concrete is considerably greater than its tensile strength. Hence, shear failure in beams is due to tension, not horizontal shear (ACI-ASCE Committee 326, 1962).
- 2- The effectiveness of stirrups far surpasses the values computed by the horizontal shear theory. The effectiveness of stirrups derived from the tensile force transmitted across a diagonal tension crack is in better accord with tests (ACI-ASCE Committee 326, 1962).
- 3- Eq. 3, which expresses the nominal shearing stress, is intended to be only a nominal measure of diagonal tension (ACI-ASCE Committee 326, 1962).

By 1910, a return to Ritter's pioneering concepts had been made, though the concepts of horizontal shear kept on reappearing in literature up until the early 1960s.

In the 1950s, researchers such as Zwoyer and Siess (1954), Bresler and Pister (1958), Guralnick (1959), and Walther (1962) studied the stress conditions in the concrete above flexural cracks in order to develop expressions for the shear capacity of members containing flexural-shear cracks. They typically assumed that all of the shear would be carried in the flexural compression zone and hence believed that the actual shear stress distribution was significantly different from that shown in Figure 1. The uncertainty about the actual distribution of shear stresses over the section caused engineers to refer to Eq. 3 as the “nominal” shear stress (Collins and Mitchell, 1997).

In 1963, ACI Committee 318 pointed out that this classical computation of the shear stress involved an oversimplified concept of diagonal tension stress. Since the actual distribution of the shear stress had not yet been fully clarified, the use of an average shear stress seemed advisable. The ACI 318-63 Code (ACI 318, 1963) found the use of the moment arm, jd , unwarranted. The ultimate shear stress was altered to average stress on the full effective cross section, and became:

$$v = \frac{V}{bd} \quad \text{Eq. 4}$$

Where b , previously defined as the “width of rectangular section”, was reduced for I and T-sections to the width of the web. If the web was to be slightly tapered, an average web width was to be used in computations.

In addition, Ritter’s equation (Eq. 2) for the design of vertical stirrups was adjusted to:

$$V = \frac{A_v f_v d}{s} \quad \text{Eq. 5}$$

The 1963 ACI code also incorporated two empirical equations for nominal shear stress at the flexure-shear cracking load. Both of these equations were developed by the ACI/ASCE Shear Committee by reviewing available research. The equations were simplified to ease every-day design work, and placed as such that the ultimate strength of beams be governed by flexure failures rather than by shear failures.

The first expression for the nominal shear stress at the flexure-shear cracking load of a reinforced concrete beam is:

$$V = \left(1.9 \sqrt{f'_c} + 2500 \rho_w \frac{Vd}{M} \right) b_w d \leq 3.5 \sqrt{f'_c} b_w d \quad (\text{inch-pound system}) \quad \text{Eq. 6}$$

$$V = \left(0.16 \sqrt{f'_c} + 17 \rho_w \frac{Vd}{M} \right) b_w d \leq 0.29 \sqrt{f'_c} b_w d \quad (\text{mm-Newton system})$$

Where:

V = External shear at diagonal tension cracking of the section considered

V/M = Ratio of shear to moment at section considered

ρ_w = Ratio of non-prestressed tension reinforcement = A_s/bd

The second equation is a simplified version of the first one:

$$V = 2 \sqrt{f'_c} b_w d \quad (\text{inch-pound system}) \quad \text{Eq. 7}$$

$$V = 0.17 \sqrt{f'_c} b_w d \quad (\text{mm-Newton system})$$

These two equations, valid for members subjected to shear and flexure only, are found in the ACI 318-08 Code.

In 1973, the ACI-ASCE Shear Committee wrote “During the next decade it is hoped that the design regulations for shear strength can be integrated, simplified and given a physical

significance so that designers can approach unusual design problems in a rational manner” (ACI-ASCE Committee 426, 1973). Nonetheless, in 1984, MacGregor described the shear equations in the ACI code as “empirical mumbo-jumbo” (MacGregor, 1984).

In 1974, a “rational” solution for the design of reinforced concrete beams to resist torsion was developed by Mitchell and Collins (1974) known as the “compression field theory”. This concept followed the strain compatibility conditions in the “tension field theory” developed by Wagner (1929) to describe the post-buckling behaviour of thin webs of steel girders. He assumed that after buckling, the thin webs would not resist compression and that the shear would be carried by a field of diagonal tension. The compression field theory is similar to Neilsen’s (Brook and Brown, 1967) lower bound solution: it described shear behaviour through the entire cracked range up to failure. The compression field theory idealized the diagonally cracked concrete as a material with coinciding principal stress and strain axes which develop to satisfy both equilibrium and compatibility of strains.

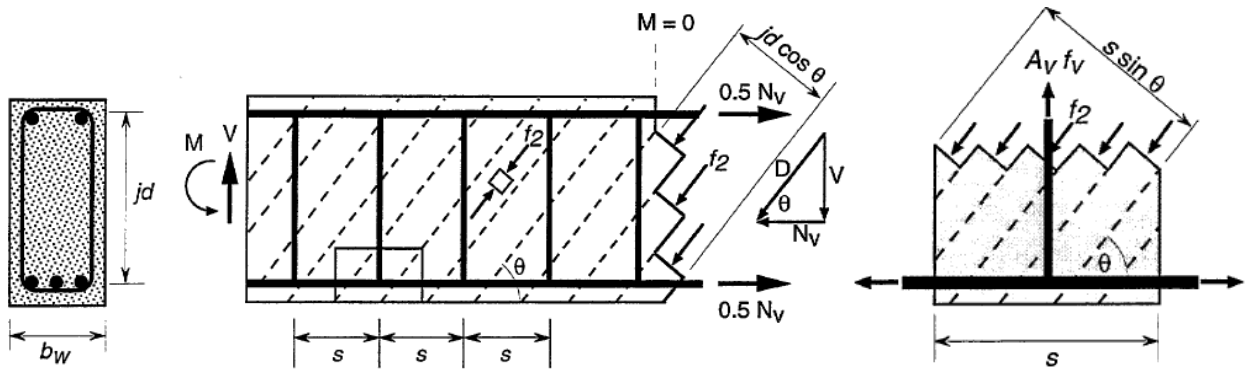


Figure 2: Design of transverse reinforcement for shear: compression field theory
[Adapted from Collins and Mitchell, 1997]

The vertical component of the diagonal compressive force in the concrete, which is inclined at the angle θ to the longitudinal axis, must equal the applied shear force (Figure 2) and hence:

$$f_2 = \left(\frac{V}{b_w jd} \right) \left(\tan \theta + \frac{1}{\tan \theta} \right) \quad \text{Eq. 8}$$

In turn, the diagonal compression in the concrete transfers vertical forces to the stirrups so that:

$$\frac{A_v f_v}{s} = \frac{V}{jd} \tan \theta \quad \text{Eq. 9}$$

The longitudinal component of the diagonal compression in the concrete is equilibrated by tension:

$$N_v = A_x f_x + A_p f_p = \frac{V}{\tan \theta} \quad \text{Eq. 10}$$

The compression field theory also assumed that concrete, once cracked, carries no tension and that the shear is carried by a field of diagonal compression. Applying Wagner's approach to reinforced concrete resulted in the following expression for the angle of inclination of the diagonal compression (Figure 3):

$$\tan^2 \theta = \frac{\epsilon_x + \epsilon_2}{\epsilon_t - \epsilon_2} \quad \text{Eq. 11}$$

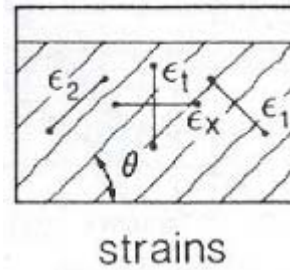


Figure 3: Average strains in web elements

[Adapted from Collins and Mitchell, 1986]

In 1982, Vecchio and Collins tested reinforced concrete panels under biaxial stresses and pure shear. They found that the principal compressive stress in the concrete, f_2 , is a function not only of the principal compressive strain ϵ_2 , but also of the coexisting principal tensile strain ϵ_1 . In fact, the concrete web is not only in compression in direction 2, but is also in tension in direction 1. They suggested the following parabolic stress-strain relationship:

$$f_2 = f_{2,\max} \left[2 \left(\frac{\epsilon_2}{\epsilon_c} \right) - \left(\frac{\epsilon_2}{\epsilon_c} \right)^2 \right] \quad \text{Eq. 12}$$

Where:

$$\frac{f_{2,\max}}{f_c'} = \frac{1}{0.8 + 170\epsilon_1} \leq 1.0 \quad \text{Eq. 13}$$

By using these equations, it was possible to predict not only the strength but the load-deformation response of members loaded in shear. However, it was found that this theory overestimates the

deformations and underestimates the strengths because it neglects the contribution of the tensile stresses in cracked concrete (Collins and Mitchell, 1997). By 1986, Vecchio and Collins came up with the “modified compression field theory”. This theory stated that shear force is resisted by the diagonal compressive stresses, f_2 , together with the diagonal tensile stresses, f_1 , accounting for the contribution of the concrete in tension, even after it has cracked (Figure 4).

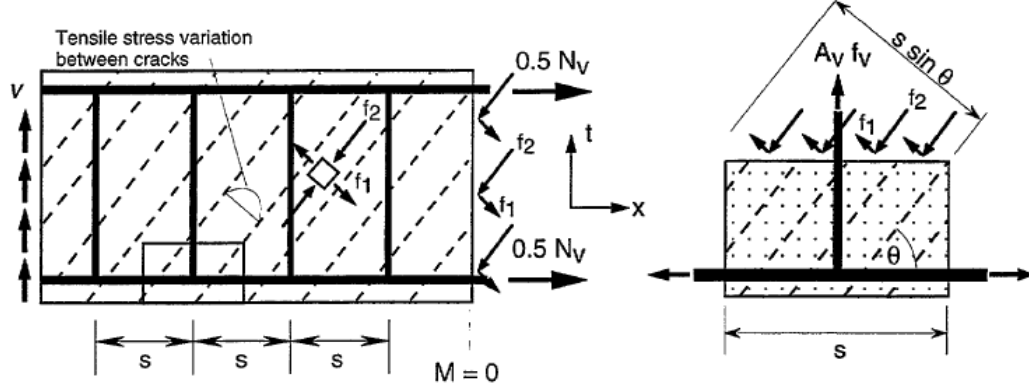


Figure 4: Design of transverse reinforcement for shear: modified compression field theory
[Adapted from Collins and Mitchell, 1997]

From Mohr’s stress circle, the following expression for f_2 was derived:

$$f_2 = v \left(\tan \theta + \frac{1}{\tan \theta} \right) - f_1 \quad \text{Eq. 14}$$

Where:

$$v = \frac{V}{b_w jd}$$

Compared with the previous equilibrium Eq. 8 of the compression field theory, Eq. 14 incorporates the concrete tensile stresses contributing to carrying the load. The diagonal compressive stresses f_2 push apart the flanges of the beam while the diagonal tensile stresses f_1 pull them together. The vertical imbalance is carried by tension in the web reinforcement. The equilibrium requirement is expressed as:

$$\frac{A_v f_v}{s} = (f_2 \sin^2 \theta - f_1 \cos^2 \theta) b_w \quad \text{Eq. 15}$$

Combining Eq. 14 and 15 quantified the concrete contribution, a value up until then always approximated:

$$V = \frac{A_v f_v}{s} jd \cot \theta + f_1 b_w jd \cot \theta \quad \text{Eq. 16}$$

$$V = V_s + V_c \quad \text{Eq. 17}$$

$V = \text{Steel contribution} + \text{Concrete contribution}$

In fact, between 1904 and 1922, several hundred reinforced concrete beams were tested by Talbot at the University of Illinois (Hognestad, 1952) and by Moritz at the University of Wisconsin (Hognestad, 1952). These tests demonstrated that the stirrup stresses were considerably lower than those predicted by the 45° truss model. This was due to the neglect of tensile stresses in the concrete and the choice of 45° for the compressive strut inclination. According to the 45° truss model, a beam without any transverse reinforcement would have zero shear strength. In order to account for the contribution of the tensile stresses in the concrete, the first ACI code, in 1910 (ACI 1910) stated:

“In calculating web reinforcement the concrete shall be considered to carry 40 psi (0.275 MPa), the remainder to be provided for by means of web-reinforcement in tension.”

As the typical concrete compressive strength in those days was 2,000 psi (13.8 MPa), this working stress code permitted concrete tensile stress at working load of $0.02f'_c$, equating about $0.04f'_c$ at ultimate.

In 1989, the ACI Code (ACI 318, 1989) separated the shear resistance of a beam into two components, the “concrete contribution” due to tensile stresses in the concrete and the “steel contribution” due to tensile stresses in the stirrups.

A number of experiments were conducted to study the influence of concrete strength on the shear strength of reinforced concrete beams. Mphonde and Frantz (1985) tested 12 reinforced concrete beams with f'_c ranging from 3,500 to 13,000 psi (24.2 to 89.7 MPa). They concluded that the ACI Code (Eq. 6, 16 and 17), are conservative for all values of f'_c . Soon after, Elzanati, Nilson and State (1986) and Nilson (1987) tested 9 reinforced concrete beams with $f'_c > 9,500 \text{ psi}$ (65.55 MPa) for shear strength and compared the results with 6 beams of $f'_c \leq 5,800 \text{ psi}$ (40 MPa). They concluded that the ACI Code Equation 6 is unconservative by 10 to 30% for beams combining high strength concrete with medium to high shear span ratios and typical or relatively low longitudinal steel ratios.

In 1989, Johnson and Ramirez (1989) tested 8 rectangular beams with concrete strength ranging from 5,000 to 10,500 psi (34.5 to 72.5 MPa), and with web reinforcement ratios ν_s of 0 to 100 psi (0.69 MPa). Their results indicated that the overall reserve shear strength after diagonal cracking, $V_{fail} - V_c$, diminishes as the concrete compressive strength increases, for a constant reinforcement ratio. This data was used to justify the ACI 318-89 Code expressions in §11.1.2.1 which limits f'_c to 10,000 psi (69 MPa) or increases the minimum amount of reinforcement by a factor equal to $f'_c/5,000$ psi (34.5 MPa) but less than 3 times the amount provided for concrete with $f'_c < 5,000$ psi (34.5 MPa).

Roller and Russell (1990) reviewed 150 tests and confirmed the validity of the ACI Code equations for shear. They also tested 10 beams with f'_c ranging from 10,500 psi to 18,000 psi (72.5 to 124.2 MPa), all of which confirmed the findings of Johnson and Ramirez's research. Throughout the years, the provision requiring a sudden increase in the minimum amount of transverse reinforcement for concrete strengths between 10,000 and 15,000 psi (69 and 103.5 MPa) was replaced by a gradual increase in the minimum A_v , as f'_c increases.

Despite all the tests done in the past, research is still to be continued. In fact, due to the number of variables involved, a general shear theory has been evasive. Design has been based on empirical evidence, resulting in almost as many empirical equations as investigators. This basis has provided a multitude of design equations for the design of structures in shear. For instance, the ACI Building Code provides five different equations to evaluate the concrete contribution to shear resistance for nonprestressed members, and three for prestressed members. To calculate V_c according to the AASHTO design specifications is dependent on the version of specifications used. In general, the 16th edition conforms to the ACI Building Code. However, the AASHTO LRFD bridge design specifications have introduced substantially different provisions for shear design, based on the modified compression field theory.

1.2.2 ACI 318 Building Code (318-08)

ACI 318, while generally providing ease in calculation, has been identified as having many shortcomings including lack of conservatism for lightly reinforced cross-sections, for sections utilizing high strength concrete, and deep sections.

The ACI 318-08 code starts by stipulating that the design shear strength of a member, ϕV_n , must be greater than the factored shear, V_u :

$$V_u \leq \phi V_n \quad \text{ACI 11- 1}$$

Where:

ϕ = Strength reduction factor, taken equal to 0.85 for shear

With the nominal shear strength V_n given as:

$$V_n = V_c + V_s \quad \text{ACI 11- 2}$$

Where:

V_c = Nominal shear strength provided by concrete

V_s = Nominal shear strength provided by steel

Assuming that all stirrups yield at failure, the shear resisted by the stirrups perpendicular to the axis is computed by:

$$V_s = \frac{A_v f_{yt} d}{s} \quad \text{ACI 11- 15}$$

Where:

A_v = Area of shear reinforcement within spacing s , in^2 (mm^2)

f_{yt} = Specified yield strength of transverse reinforcement, psi (MPa)

d/s = Number of vertical stirrups spaced s apart, in a beam of d effective depth, crossed by a 45° crack

d = Distance from extreme compression fiber to centroid of the prestressed and nonprestressed longitudinal tension reinforcement, if any, but need not be taken less than $0.80h$

1.2.2.1 Shear strength provided by concrete for nonprestressed members

The ACI code assumes that V_c is equal to the shear strength of a beam without stirrups, which in turn is taken equal to the load at which inclined cracking occurs. For members subjected to flexure and shear only:

$$V_c = 2\lambda\sqrt{f'_c}b_wd \quad , lb \quad \text{ACI 11-3}$$

$$V_c = 0.17\sqrt{f'_c}b_wd \quad , N$$

This equation was developed by ACI-ASCE Committee 326 in 1962 who also permitted a more detailed calculation for V_c . For members subjected to flexure and shear only:

$$V_c = \left(1.9\lambda\sqrt{f'_c} + 2500\rho_w \frac{V_u d}{M_u} \right) b_w d \leq 3.5\sqrt{f'_c}b_wd \quad , lb \quad \text{ACI 11-5}$$

$$V_c = \left(0.16\sqrt{f'_c} + 17\rho_w \frac{V_u d}{M_u} \right) b_w d \leq 0.29\sqrt{f'_c}b_wd \quad , N$$

Where:

b_w = Web width, in (mm)

f'_c = Concrete compressive strength, psi (MPa)

M_u = Factored moment at section, in · lb (N · mm)

ρ_w = Longitudinal reinforcement ratio

λ = Modification factor reflecting the reduced mechanical properties of lightweight concrete, all relative to normalweight concrete of the same compressive strength
= 1 for normalweight concrete

$\frac{M_u}{V_u d}$ = Shear span to depth ratio, a/d

$$\frac{V_u d}{M_u} \leq 1.0$$

For members subjected to axial compression and axial tension, equations ACI 11-3 and ACI 11-5 are not applicable. The code provides a simplified and a more detailed equation for each of these loading cases.

For members subjected to axial compression, the simplified method sets V_c as:

$$V_c = 2 \left(1 + \frac{N_u}{2000A_g} \right) \lambda \sqrt{f'_c} b_w d \quad , lb \quad \text{ACI 11- 4}$$

$$V_c = 0.17 \left(1 + \frac{N_u}{14A_g} \right) \sqrt{f'_c} b_w d \quad , N$$

Where:

N_u = Factored axial force normal to cross section; to be taken as positive for compression and negative for tension, lb (N)
 > 0 in this case

A_g = Gross area of concrete section, in^2 (mm^2)

Whereas the detailed method, for members subjected to axial compression, specifies:

$$V_c = \left(1.9 \lambda \sqrt{f'_c} + 2500 \rho_w \frac{V_u d}{M_m} \right) b_w d \leq 3.5 \lambda \sqrt{f'_c} b_w d \sqrt{1 + \frac{N_u}{500A_g}} \quad , lb \quad \text{ACI 11- 6}$$

$$V_c = \left(0.16 \sqrt{f'_c} + 17 \rho_w \frac{V_u d}{M_m} \right) b_w d \leq 0.29 \sqrt{f'_c} b_w d \sqrt{1 + \frac{0.29 N_u}{A_g}} \quad , N$$

Where:

M_m = Factored moment modified to account for effect of axial compression

$$= M_u - N_u \frac{(4h - d)}{8} \quad , in \cdot lb \quad (N \cdot mm) \quad \text{ACI 11- 7}$$

$$\frac{V_u d}{M_u} = \text{Not restricted to 1.0}$$

For members subjected to axial tension, Clause 11.2.1.3 for the simplified method stipulates that V_c is taken as zero, unless a more detailed analysis is performed using:

$$V_c = 2 \left(1 + \frac{N_u}{500A_g} \right) \lambda \sqrt{f'_c} b_w d \geq 0 \quad , lb \quad \text{ACI 11- 8}$$

$$V_c = 0.17 \left(1 + \frac{0.29N_u}{A_g} \right) \sqrt{f'_c} b_w d \geq 0 \quad , N$$

Where:

N_u = Factored axial force normal to cross section; to be taken as positive for compression and negative for tension, lb (N)
 < 0 in this case

1.2.2.2 Shear strength provided by concrete for prestressed members

The situation for members with an effective prestress force of at least 40 percent of the tensile strength of flexural reinforcement is different and is managed by other equations for V_c .

The simplified method sets V_c as:

$$V_c = \left(0.6 \lambda \sqrt{f'_c} + 700 \frac{V_u d_p}{M_u} \right) b_w d \quad , lb \quad \text{ACI 11- 9}$$

$$\geq 2 \lambda \sqrt{f'_c} b_w d$$

$$\leq 5 \lambda \sqrt{f'_c} b_w d$$

$$V_c = \left(0.05 \sqrt{f'_c} + 4.8 \frac{V_u d_p}{M_u} \right) b_w d \quad , N$$

$$\geq 0.17 \sqrt{f'_c} b_w d$$

$$\leq 0.42 \sqrt{f'_c} b_w d$$

Where:

$$\frac{V_u d_p}{M_u} \leq 1.0$$

A more detailed method allows V_c to be taken as the lesser of V_{ci} and V_{cw} .

V_{ci} represents the nominal shear strength provided by concrete when diagonal cracking results from combined shear and moment, and is calculated as:

$$V_{ci} = 0.6\lambda\sqrt{f'_c}b_wd_p + V_d + \frac{V_iM_{cre}}{M_{max}} \geq 1.7\lambda\sqrt{f'_c}b_wd \quad , \text{ lb} \quad \text{ACI 11- 10}$$

$$V_{ci} = 0.05\sqrt{f'_c}b_wd_p + V_d + \frac{V_iM_{cre}}{M_{max}} \geq 0.14\sqrt{f'_c}b_wd \quad , N$$

Where:

M_{cre} = Moment causing flexural cracking at section due to externally applied loads

$$\left(\frac{I}{y_t} \right) \left(6\lambda\sqrt{f'_c} + f_{pe} - f_d \right) \quad , \text{ in} \cdot \text{ lb} \quad \text{ACI 11- 11}$$

$$\left(\frac{I}{y_t} \right) \left(0.5\sqrt{f'_c} + f_{pe} - f_d \right) \quad , (N \cdot \text{ mm})$$

M_{max} and V_i : Taken from the load combination causing maximum factored moment

V_{cw} , on the other hand, represents the nominal shear strength provided by concrete when diagonal cracking results from high principal tensile stress in the web

$$V_{cw} = \left(3.5\lambda\sqrt{f'_c} + 0.3f_{pc} \right) b_wd_p + V_p \quad , \text{ lb} \quad \text{ACI 11- 12}$$

$$V_{cw} = \left(0.29\sqrt{f'_c} + 0.3f_{pc} \right) b_wd_p + V_p \quad , N$$

Where:

$$V_p \geq 0.80h$$

V_{cw} : Computed as the shear force corresponding to dead load plus live load that results in a principal tensile stress of $4\lambda\sqrt{f'_c}$ psi $\left(0.33\sqrt{f'_c} \text{ MPa} \right)$ at the centroidal axis of member, or at the intersection of flange and web when the centroidal axis is in the flange

1.2.2.3 Minimum shear reinforcement

The shear design reinforcement, for prestressed and nonprestressed members, is summarized in Table 1.

Table 1: ACI 318-08 Design of shear reinforcement

$V_u \leq 0.5\phi V_c$	
	No stirrups required
$V_u > 0.5\phi V_c$ to $V_u \leq \phi V_c$	
	$s \leq 0.50d$ (nonprestressed members) $s \leq 0.75h$ (prestressed members) $s \leq 24in$ (600mm)
$V_u > \phi V_c$ to $V_u \leq V_c + 4\sqrt{f'_c} b_w d$ (lb)	<p>Minimum reinforcement, for prestressed and nonprestressed members, must be provided such that:</p> $A_{v,min} = 0.75\sqrt{f'_c} \frac{b_w s}{f_{yt}} \geq \frac{50b_w s}{f_{yt}} \text{ (in}^2\text{)}$ $A_{v,min} = 0.062\sqrt{f'_c} \frac{b_w s}{f_{yt}} \geq \frac{0.35b_w s}{f_{yt}} \text{ (mm}^2\text{)}$ <p>(ACI 11- 13)</p>
$V_u > \phi V_c$ to $V_u \leq V_c + 0.33\sqrt{f'_c} b_w d$ (N)	
$s \leq 0.50d$ (nonprestressed members) $s \leq 0.75h$ (prestressed members) $s \leq 24in$ (600mm)	
<p>Shear reinforcement perpendicular to axis of member:</p> $V_s = \frac{A_v f_{yt} d}{s} \Rightarrow s \leq \frac{A_v f_{yt} d}{\frac{V_u}{\phi} - V_c}$ <p>(ACI 11- 15)</p>	
$V_u > V_c + 4\sqrt{f'_c} b_w d$ to $V_u \leq V_c + 8\sqrt{f'_c} b_w d$ (lb)	<p>For prestressed members:</p> $A_{v,min} = \frac{A_{ps} f_{pu} s}{80 f_{yt} d} \sqrt{\frac{d}{b_w}} \text{ (in}^2\text{, mm}^2\text{)}$ <p>(ACI 11- 14)</p>
$V_u > V_c + 0.33\sqrt{f'_c} b_w d$ to $V_u \leq V_c + 0.66\sqrt{f'_c} b_w d$ (N)	
$s \leq 0.25d$ (nonprestressed members) $s \leq 0.375h$ (prestressed members) $s \leq 12in$ (300mm)	
<p>Shear reinforcement perpendicular to axis of member:</p> $V_s = \frac{A_v f_{yt} d}{s} \Rightarrow s \leq \frac{A_v f_{yt} d}{\frac{V_u}{\phi} - V_c}$ <p>(ACI 11- 15)</p>	
$V_u > V_c + 8\sqrt{f'_c} b_w d$ (lb)	
$V_u > V_c + 0.66\sqrt{f'_c} b_w d$ (N)	
	Cross section too small

1.2.2.4 High strength concrete

The value of $\sqrt{f'_c}$ in the ACI Code is specified in clause §11.1.2 is limited to be less than or equal to 100 psi (8.3 MPa). If this limit is exceeded, the values V_c , V_{ci} and V_{cw} for reinforced nonprestressed or prestressed concrete beams, with minimum web reinforcement, are to be computed in accordance with Table 2.

Table 2: ACI 318-08 Particular considerations for High Strength Concrete

Where torsion is allowed to be neglected, for prestressed and non prestressed members	$A_{v,min} = 0.75\sqrt{f'_c} \frac{b_w s}{f_{yt}} \geq \frac{50b_w s}{f_{yt}} \text{ (in}^2\text{)}$ $A_{v,min} = 0.062\sqrt{f'_c} \frac{b_w s}{f_{yt}} \geq \frac{0.35b_w s}{f_{yt}} \text{ (mm}^2\text{)}$	ACI 11- 13
For prestressed members with an effective prestress force not less than 40 percent of the tensile strength of the flexural reinforcement	$A_{v,min} = \frac{A_{ps} f_{pu} s}{80 f_{yt} d} \sqrt{\frac{d}{b_w}} \text{ (in}^2\text{, mm}^2\text{)}$	ACI 11- 14
Where torsional reinforcement is required	$(A_v + 2A_t) = 0.75\sqrt{f'_c} \frac{b_w s}{f_{yt}} \geq \frac{50b_w s}{f_{yt}} \text{ (in}^2\text{)}$ $(A_v + 2A_t) = 0.062\sqrt{f'_c} \frac{b_w s}{f_{yt}} \geq \frac{0.35b_w s}{f_{yt}} \text{ (mm}^2\text{)}$	ACI 11- 23

1.2.3 2004 AASHTO LRFD Bridge design specifications

The 2004 AASHTO LRFD bridge design specifications are based on the Modified Compression Field Theory (MCFT) and on the Strut-and-Tie modeling. There are advantages to the LRFD method such as unified treatment of nonprestressed reinforced members and prestressed members. However, the LRFD has been identified as being complex, requiring time-consuming iteration.

The 2004 AASHTO LRFD code starts by stipulating that the shear resistance of a member must be greater than the factored nominal shear:

$$V_r = \phi V_n$$

AASHTO LRFD 5.8.2.1-2

Where the nominal shear is evaluated as:

$$V_n = V_c + V_s + V_p \leq 0.25 f'_c b_v d_v + V_p$$

AASHTO LRFD 5.8.3.3-1
AASHTO LRFD 5.8.3.3-2

In which the nominal shear resistance provided by tensile stresses in the concrete, V_c , is evaluated as::

$$V_c = 0.0316 \beta \sqrt{f'_c} b_v d_v \quad \text{kip}$$

AASHTO LRFD 5.8.3.3-3

$$V_c = 0.083 \beta \sqrt{f'_c} b_v d_v \quad N$$

Where:

b_v = Effective web width, in (mm)

d_v = Effective shear depth: distance between resultants of tensile and compressive forces
 $(d_e - a/2)$, but not less than the greater of $0.9 d_e$ or $0.72h$

Where:

d_e = The corresponding effective depth from the extreme compression fiber to the centroid of the tension force in the tensile reinforcement

a = Depth of the compression block

h = Total height of the section

f'_c = Concrete compressive strength, ksi (MPa)

β = Factor indicating the ability of diagonally cracked concrete to transmit tension

And the transverse reinforcement contribution, when vertically placed, is evaluated as:

$$V_s = \frac{A_v f_y d_v \cot \theta}{s} \quad \text{kip (MPa)}$$

AASHTO LRFD C5.8.3.3-1

Where:

A_v = Area of shear reinforcement within spacing s , in² (mm²)

f_y = Specified minimum yield strength of reinforcing bars, ksi (MPa)

θ = Angle of inclination of diagonal compressive stresses

The prestressing contribution to shear resistance, V_p , is the vertical component of the prestressing force. It is positive when resisting the applied shear.

The expressions for V_c and V_s apply to both prestressed and nonprestressed section, with the terms β and θ depending on the applied loading and the properties of the section. Both of these values are obtained from tables which depend on whether the section contains the minimum transverse reinforcement, given by the following equation, or not:

$$A_v = 0.0316 \sqrt{f'_c} \frac{b_v s}{f_y} \quad , \text{ in}^2 \quad \text{AASHTO LRFD 5.8.2.5-1}$$

$$A_v = 0.083 \sqrt{f'_c} \frac{b_v s}{f_y} \quad , \text{ mm}^2$$

This reinforcement is mandatory where consideration of torsion is required by:

$$T_u > 0.25 \phi T_{cr} \quad \text{AASHTO LRFD 5.8.2.1-3}$$

Or where

$$V_u > 0.5 \phi (V_c + V_p) \quad \text{AASHTO LRFD 5.8.2.4-1}$$

If a member does contain the minimum reinforcement, then ε_x , calculated using equation 5.8.3.4.2-1, shall be taken as the calculated longitudinal strain at the mid-depth of the member when the section is subjected to M_u , N_u , and V_u . Table 3 is used.

$$\varepsilon_x = \frac{\left(\frac{M_u}{d_v} + 0.5 N_u + 0.5 (V_u - V_p) \cot \theta - A_{ps} f_{po} \right)}{2(E_s A_s + E_p A_{ps})} \geq 0.001 \quad \text{AASHTO LRFD 5.8.3.4.2-1}$$

Table 3: Value of θ and β for sections with transverse reinforcement (AASHTO LRFD Table 5.8.3.4.2-1)

$\frac{v_u}{f'_c}$	$\varepsilon_x \times 1000$								
	≤ -0.20	≤ -0.10	≤ -0.05	≤ 0	≤ 0.125	≤ 0.25	≤ 0.50	≤ 0.75	≤ 1.0
≤ 0.075	22.3 6.32	20.4 4.75	21.0 4.10	21.8 3.75	24.3 3.24	26.6 2.94	30.5 2.59	33.7 2.38	36.4 2.23

$\frac{v_u}{f_c}$	$\varepsilon_x \times 1000$								
	≤ -0.20	≤ -0.10	≤ -0.05	≤ 0	≤ 0.125	≤ 0.25	≤ 0.50	≤ 0.75	≤ 1.0
≤ 0.100	18.1 3.79	20.4 3.38	21.4 3.24	22.5 3.14	24.9 2.91	27.1 2.75	30.8 2.50	34.0 2.32	36.7 2.18
≤ 0.125	19.9 3.18	21.9 2.99	22.8 2.94	23.7 2.87	25.9 2.74	27.9 2.62	31.4 2.42	34.4 2.26	37.0 2.13
≤ 0.150	21.6 2.88	23.3 2.79	24.2 2.78	25.0 2.72	26.9 2.60	28.8 2.52	32.1 2.36	34.9 2.21	37.3 2.08
≤ 0.175	23.2 2.73	24.7 2.66	25.5 2.65	26.2 2.60	28.0 2.52	29.7 2.44	32.7 2.28	35.2 2.14	36.8 1.96
≤ 0.200	24.7 2.63	26.1 2.59	26.7 2.52	27.4 2.51	29.0 2.43	30.6 2.37	32.8 2.14	34.5 1.94	36.1 1.79
≤ 0.225	26.1 2.53	27.3 2.45	27.9 2.42	28.5 2.40	30.0 2.34	30.8 2.14	32.3 1.86	34.0 1.73	35.7 1.64
≤ 0.250	27.5 2.39	28.6 2.39	29.1 2.33	29.7 2.33	30.6 2.12	31.3 1.93	32.8 1.70	34.3 1.58	35.8 1.50

For section with less reinforcement than the minimum, ε_x is calculated as the double of equation 5.8.3.4.2-1, with double the upper limit. It should be taken as the largest calculated longitudinal strain which occurs within the web of the member when subjected to M_u , N_u , and V_u . Table 4 is used.

Table 4: Value of θ and β for sections with less than minimum transverse reinforcement (AASHTO LRFD Table 5.8.3.4.2-2)

s_{xe} (in)	$\varepsilon_x \times 1000$										
	≤ -0.20	≤ -0.10	≤ -0.05	≤ 0	≤ 0.125	≤ 0.25	≤ 0.50	≤ 0.75	≤ 1.0	≤ 1.50	≤ 2.0
≤ 5	25.4 6.36	25.5 6.06	25.9 5.56	26.4 5.15	27.7 4.41	28.9 3.91	30.9 3.26	32.4 2.86	33.7 2.58	35.6 2.21	37.2 1.96
≤ 10	27.6 5.78	27.6 5.78	28.3 5.38	29.3 4.89	31.6 4.05	33.5 3.52	36.3 2.88	38.4 2.50	40.1 2.23	42.7 1.88	44.7 1.65
≤ 15	29.5 5.34	29.5 5.34	29.7 5.27	31.1 4.73	34.1 3.82	36.5 3.28	39.9 2.64	42.4 2.26	44.4 2.01	47.4 1.68	49.7 1.46
≤ 20	31.2 4.99	31.2 4.99	31.2 4.99	32.3 4.61	36.0 3.65	38.8 3.09	42.7 2.46	45.5 2.09	47.6 1.85	50.9 1.52	53.4 1.31
≤ 30	34.1 4.46	34.1 4.46	34.1 4.46	34.2 4.43	38.9 3.39	42.3 2.82	46.9 2.19	50.1 1.84	52.6 1.60	56.3 1.30	59.0 1.10
≤ 40	36.6 4.06	36.6 4.06	36.6 4.06	36.6 4.06	41.2 3.20	45.0 2.62	50.2 2.00	53.7 1.66	56.3 1.43	60.2 1.14	63.0 0.95
≤ 60	40.8 3.50	40.8 3.50	40.8 3.50	40.8 3.50	44.5 2.92	49.2 2.32	55.1 1.72	58.9 1.40	61.8 1.18	65.8 0.92	68.6 0.75
≤ 80	44.3 3.10	44.3 3.10	44.3 3.10	44.3 3.10	47.1 2.71	52.3 2.11	58.7 1.52	62.8 1.21	65.7 1.01	69.7 0.76	72.4 0.62

Table 4 requires the crack spacing parameter, s_{xe} , which is computed as:

$$s_{xe} = s_x \frac{1.38}{a_g + 0.63} \leq 80in \ (2.0m) \quad \text{AASHTO LRFD 5.8.3.4.2-4}$$

a_g = Maximum aggregate size (in)

s_x = Lesser of d_v or the maximum distance between layers of longitudinal crack control reinforcement

If ε_x is computed negative when using equation 5.8.3.4.2-1, then the strain must be calculated according to equation 5.8.3.4.2-3 and Table 3 or Table 4, for reinforced section or not, respectively, must be used to get the θ and β values:

$$\varepsilon_x = \frac{\left(\frac{M_u}{d_v} + 0.5N_u + 0.5(V_u - V_p) \cot \theta - A_{ps} f_{po} \right)}{2(E_c A_c + E_s A_s + E_p A_{ps})} \quad \text{AASHTO LRFD 5.8.3.4.2-3}$$

1.2.3.1 Minimum shear reinforcement

The shear design reinforcement is summarized in Table 5.

Table 5: AASHTO LRFD Shear design reinforcement

$V_u \leq 0.5\phi(V_c + V_p)$		
	No stirrups required	
$V_u > 0.5\phi(V_c + V_p)$ to $V_u < 0.125f'_c b_w d$		
	$s \leq 0.8d_v$ $s \leq 24in \ (600mm)$ AASHTO LRFD 5.8.2.7-1	$A_v \geq 0.0316\sqrt{f'_c} \frac{b_v s}{f_y} \ (in^2)$ $A_v \geq 0.083\sqrt{f'_c} \frac{b_v s}{f_y} \ (mm^2)$ AASHTO LRFD 5.8.2.5-1
$V_u \geq 0.125f'_c b_w d$		
	$s \leq 0.4d_v$ $s \leq 12in \ (300mm)$ AASHTO LRFD 5.8.2.7-2	

1.2.4 Comparison between ACI method and the AASHTO method

Shahawy and Batchelor (1996) performed full scale tests of 20 AASHTO Type II pretensioned concrete girders and compared the measured shear strength with the values predicted by the 1989 AASHTO Standard Specifications, which uses the ACI method, and the 1994 AASHTO LRFD Specifications, which uses the modified compression field theory.

The main variable of the study were the amounts of shear reinforcement, shear span and strand diameter. Six girders were designed according to the provisions of the ACI method and were provided with the required (R) shear reinforcement. The other 14 girders had various shear reinforcement ρ_v ranging from 0 to $3R$. Thirteen girders were 41 feet (12.5 m) long, two girders were 25 feet (7.6 m) long and the other five girders were 21 feet (6.4 m) long. Both, the girder and the cast-in-place concrete slab, were designed for a 28-day cylinder concrete strength of 6,000 psi (41.4 MPa).

Shahawy and Batchelor's results indicate that the 1989 Standard (comparable to the current ACI) provides excellent predictions for girders having shear reinforcement $R < \rho_v < 3R$ and conservative estimates for girders with $0 < \rho_v < R$. On the other hand, the LRFD Code considerably overestimates the shear strength of over-designed girders ($2R < \rho_v < 3R$) and grossly underestimates the shear strength of under-designed girders ($0 < \rho_v < R/2$). The latter suggests that the LRFD estimate for V_c is too low. For $\rho_v = R$, although both approaches provided conservative estimates, Shahawy and Batchelor found the 1989 Standard to provide better values than the LRFD Code.

Note that as ρ_v increases from R to $3R$, the shear strength only increases slightly. This justifies the imposition of a cap on shear reinforcement. The code required the upper limit to prevent the concrete in the web from crushing prior to yielding of the shear reinforcement. However, in Shahawy and Batchelor's experiments, the maximum amount of shear reinforcement was significantly exceeded without any sign of concrete crushing in the web at failure. At the maximum specified shear reinforcement, the 1989 Standard compared very well with test results while the LRFD Code significantly overestimated the shear strength, suggesting that the LRFD limit is too high.

In regions near supports, the LRFD Code predicts higher values of shear strength than does the 1989 Standard, because the LRFD Code assumes smaller strut angles compared to the 1989

Standard, which uses $\theta = 45^\circ$. However, away from the support regions, the concrete contribution V_c is relatively small compared to the shear reinforcement V_s , and θ approaches 45° in both codes. The LRFD Code underestimates V_c in these regions, thereby resulting in lower predicted shear strength than provided by the 1989 Standard.

Shahawy and Batchelor (1996) recognized the appeal of the greater rationality of the modified compression field theory but questioned if the increased complexity and the greater discrepancy with test results justify the extensive changes to the code.

1.3 Prestressing operations

One of the major advancements in bridge construction in the United States in the second half of the twentieth century was the development and use of prestressed concrete. Prestressed concrete bridges offered a broad range of engineering solutions and a variety of aesthetic opportunities. The following sections describe the history of its development (Section 1.3.1), the structural concept behind prestressing (Section 1.3.2), the different procedure put in place (Section 1.3.3), the benefits (Section 1.3.4), and the materials needed and their behaviour (Section 1.3.5).

1.3.1 Historical development of prestressing

Prestressing concrete dates back to 1872 when P. Henry Jackson, an engineer from California, patented a prestressing system that used a tie rod to construct beams and arches from individual blocks. His effort was followed in 1888 by C.W. Doebling who obtained a patent in Germany for prestressing slabs with metal wires. However, none of these early attempts were successful because of the loss of prestress with time (Nawy, 1996).

After a long lapse of time during which little progress was made, P.E. Dill, of Nebraska, recognized the effect of the shrinkage and creep of concrete on the loss of prestress. In fact, low initial jacking stress, combined with high creep and shrinkage of the concrete, eroded the bulk of the prestressing force applied to the structure, leaving the steel practically ineffective. He subsequently developed the idea that successive post-tensioning of unbonded rods would compensate for the time-dependent loss of stress in the rods (Nawy, 1996).

Prestressing continued to develop in particular through the ingenuity of Eugene Freyssinet, of France, who proposed in 1926 through 1928 methods to overcome prestress losses by the use of high-strength steels and improved concrete with lower shrinkage and creep (Collins and Mitchell, 1997). Freyssinet is generally considered the father of modern prestressing, and it was his six bridges across the Marne, in France, built between 1945 and 1950, which established the technique (Hewson, 2003).

After World War II, it became necessary to reconstruct in a prompt manner many of the main bridges that were destroyed by war activities. While Eugene Freyssinet continued to design many new prestressed concrete bridges, Gustave Magnel developed the technique on several notable structures in Belgium. Y. Guyon of Paris extensively developed and used the concept of prestressing for the design and construction of numerous bridges in western and central Europe.

In Germany, Russia and United States, Fritz Leonhardt, V. Mikhailov and T.Y. Lin were respectively the leading exponent of prestressed concrete (Nawy, 1996 and Hewson, 2003).

In 1939, Freyssinet introduced the now well-known and well-accepted Freyssinet system comprising the conical wedge anchor for 12-wire tendons (Nawy, 1996). After 1945, other systems, such as those produced by Magnel-Blaton, BBRV and Lee-McCall began to appear, as prestressing of concrete became popular. The early prestressing systems used were comprised of wires usually 0.2 in (5 mm) or 0.28 in (7 mm) diameter, tensioned and anchored by a gripping device at the ends that transferred the load to the concrete (Hewson, 2003).

By the early 1960s, the wires were being assembled into strands and anchored by wedges onto an anchor cone cast into the concrete. This led to the development of the '7-wires' strand, most commonly used today (Nawy, 1996). Also at this time, large capacity jacks were developed capable of tensioning large multi-strand cables in one operation. Those tendons began to dominate the market (Hewson, 2003).

These twentieth-century developments have led to the extensive use of prestressing throughout the world. Today, buildings, underground structures, towers, stadia, floating storages, offshore structures, power stations, nuclear reactor vessels, and numerous types of bridge systems all use prestressed concrete (Collins and Mitchell, 1997 and Nawy, 1996).

1.3.2 Principle of prestressed concrete

In simple terms, prestressing means not only preparing a structure to receive a load by improving its resistance, but also modifying the behaviour of the members and structures in such way as to make them more suitable for their intended purposes (Benaïm, 2008). Similarly to non-prestressed concrete, prestressed concrete contains steel reinforcement. The difference lies in the fact that some of the reinforcement is made out of high-strength steel, tensioned prior to the application of external loads. This tensioning precompresses the surrounding concrete, allowing it to resist higher loads prior to cracking (Collins and Mitchell, 1997). It is important to note however that prestressed member results from self-equilibrating internal stresses: steel is tensioned and concrete is compressed. The overall prestressed system, alone, is in equilibrium and no external forces are exerted on it (Collins and Mitchell, 1997).

There are significant differences in principle between reinforced concrete and prestressed concrete. In the design of reinforced concrete beams, it is assumed that the tensile strength of the concrete is negligible, and the tensile forces created by the bending moments are resisted by

reinforcement, to which the forces are transferred by bond. Cracking and, to a large extent, deflections are irrecoverable in ordinary reinforced concrete with relatively poor bond between the steel and concrete, though with high-strength concrete and good bond a substantial degree of recovery may take place. The reinforcement usually exerts no forces on the member on its own account (Abeles and Bardhan-Roy, 1981). In prestressed concrete, on the other hand, the primary purpose of the prestressing steel is to apply a force to the concrete, either by bond or by the means of special anchoring devices. Hence, the whole of the concrete can be made to act structurally. The steel required to produce the prestressing force is thus used actively to preload the member. Cracking and deflections are recoverable to a higher degree (Abeles and Bardhan-Roy, 1981).

Despite the significant differences, there are basic similarities between reinforced and prestressed concrete. In fact, as the prestress becomes zero, the behaviour of the prestressed member becomes almost the same as that of a reinforced concrete member. Under overload conditions, as soon as the flexural strength of the concrete has been exceeded, prestressed concrete behaves in a matter similar to reinforced concrete, and at the ultimate load or collapse condition of a flexural member, the tensile and compressive resistances required to withstand these conditions are the same for both reinforced and prestressed members (Abeles and Bardhan-Roy, 1981).

1.3.3 Different types of prestressing

Prestressing can be applied in two different procedures: pretension and post-tension.

Pretensioning was developed in 1938 by the German engineer E. Hoyer. It involves tensioning the cables before the concrete is cast and anchoring them to a strengthened mould (Collins and Mitchell, 1997). Once the concrete has hardened, the cables are released, and retain their tension by their adherence to the concrete. The tension of tendon is transferred to the concrete increasing its compression and creating a positive camber. This technique is used principally for the construction of relatively short span bridge using standard bridge beams (Gerwick, 1993).

Post-tensioning was the procedure used by Freyssinet (Collins and Mitchell, 1997). It consists in feeding the reinforcing tendons through ducts encased in concrete. Once the concrete cures and the forms are removed, the tendons are anchored at one end and stressed by jacks reacting against the concrete at the other end. When the tendons reach the required tension, they are then locked to the concrete by anchors (Gerwick, 1993).

1.3.4 Benefits of prestressing

The possibility of avoiding permanent cracks is one of the major advantages of prestressed structures. The improved durability, compared to reinforced concrete, is also useful particularly in members exposed to corrosive atmospheres or aggressive ground conditions, and in marine structures (Abeles and Bardhan-Roy, 1981).

In addition, much less steel is required, since the weight of the high-strength prestressing steel is only a fraction of the weight of reinforcement which it replaces. The cross-section of the member can be smaller, since the whole of the concrete is put to structural use; and the resistance of beams to shearing and flexural cracks is considerably increased. It is therefore possible to design longer spans or cantilevers using comparatively shallow and slender sections (Abeles and Bardhan-Roy, 1981). In general, the depth of a prestressed concrete member is usually about 65 to 80 percent the depth of the equivalent reinforced concrete member. A prestressed member, when compared with an equivalent reinforced concrete member, requires less concrete, and about 20 to 35 percent of the amount of steel (Nawy, 1996). The difference in initial cost is, however, not proportional to the difference in weights of the materials. Steel and concrete, in a prestressed concrete member, need to have higher strengths and higher quality. The unit costs of such materials are therefore higher than those required for reinforced concrete construction. Formwork and moulds may be more expensive, however the forms are reuseable for standard sections, and the additional cost of prestressing operation itself must be considered. In general, there is little difference between the initial costs of reinforced and prestressed members provided that large numbers of prestressed units are required (Abeles and Bardhan-Roy, 1981).

The indirect savings which accrue from prestressed units are often substantial and should be taken fully into account. They include the reduction, or total avoidance, of maintenance and longer working life due to the greater durability of the material arising from the absence of permanently opened cracks; the reduction in the dead weight imposed on the supporting members, and foundations; the achievement of longer spans and fewer supports; and the reduction in the structural depths of members (Abeles and Bardhan-Roy, 1981).

1.3.5 Materials of prestressing

As mentioned earlier, materials used in prestressed members require higher strengths and quality. The basic necessities are outlined in the following section.

1.3.5.1 Basic concrete guidelines

Strength and endurance are the two major qualities in prestressed concrete structures. Long-term effects, such as creep and shrinkage, reduce the prestressing forces. Hence, measures have to be taken to ensure strict quality control and quality assurance at various stages of production and construction as well as maintenance (Gerwick, 1993).

Cement and cementitious materials

The almost-universal cementing material for prestressed concrete is Portland cement, Type I, II, III, or a modification of these. The first type is standard and has relatively wide tolerances in its chemical constituents. Type II is controlled as to the amount of tricalcium aluminate (C_3A), the percentage of alkalis, and the fineness of grind. It is moderately low in heat generation, and moderately sulfate-resistant. Type III has a high early strength. The cement is usually selected on the basis of rapid early strength, minimum shrinkage, durability, and economy.

In prestressed concrete, higher strengths are required and are achievable by decreasing the water/cement ratios. This decrease also reduces the creep and shrinkage as well as the concrete permeability and hence minimizes the probability of corrosion of the reinforcement and long-term deterioration of the concrete itself (Gerwick, 1993).

In order to increase the workability of concrete without jeopardizing the strength and permeability, High-Range Water-Reducing Admixtures (HRWRA), known as “superplasticizers”, are introduced to the mix. They make concrete flow with a slump of 8 to 10 inches (200 to 250 mm), with a water/cement ratio below 0.4. Supplementary cementitious materials, such as silica fume, fly ash and granulate blast furnace slag, are used to enhance rheological and mechanical properties such as the durability characteristics of the concrete.

Aggregates

In the attempt to get moderately high-strength concrete, the maximum size of coarse aggregate is somewhat limited to $\frac{3}{4}$ inch (20 mm) for most applications. Besides limiting the size, aggregates should be inert, hard, nonporous, non-expansive, clean and should have appropriate shape and grading. They should not contain deleterious amounts of substances such as salts, sulfates, or organic compounds. In fact, aggregates influence the strength and durability, and play an important role in the creep, shrinkage and thermal properties of the concrete. Their proper criteria are also important: gravel and crushed rock are both used successfully. For normal high-strength concrete, gravel will give better workability and compatibility at low water/cement ratios. For

extremely high-strength concrete, crushed rock of proper angularity is superior but requires very intensive vibration to achieve proper compaction (Gerwick, 1993).

Water

Until recently the standard requirement for water was merely that it be potable. However, water used in prestressed work should be more definitely restricted in salt, silt, and organic contents.

Water may be added to the mix in the form of crushed ice, in order to reduce the temperature of the fresh concrete mix. This would also reduce the maximum temperature during hydration and thermal strains. In extremely hot weather, the mix can be cooled even further by injecting liquid nitrogen, and in cold weather, the mixing water may be heated. The optimal temperature of the fresh mix is from 40 °F to 50 °F (4 to 10 °C). Water should not be introduced to the mix hotter than 90 °F (32 °C) (Gerwick, 1993).

1.3.5.2 Basic steel guidelines

Steel for prestressed concrete must have high tensile strength and adequate ductility. Tendons must also have the ability to sustain indefinitely a high state of stress with little loss due to relaxation, corrosion and fatigue. An ideal stress-strain diagram for prestressing steel which meets the following requirements is shown in Figure 5:

- 1- The needed high tensile stress must be accompanied by only a small amount of creep. This is achieved if the permanent elongation at the working stress is small, and the type of steel for which the stress-strain diagram is linear for a large portion of the ultimate load is used. This property is measured by the stress which produces a certain permanent deformation (usually 0.2 percent) on the first loading. Steel suitable for prestressing should have a high proof stress (Abeles and Bardhan-Roy, 1981).
- 2- An ultimate elongation of considerable magnitude should be obtained in order to reduce as much as possible the chance of sudden fracture. Such elongation, with adequate bond, for prestressing wire and strand should range between 3 and 5 percent (Abeles and Bardhan-Roy, 1981).

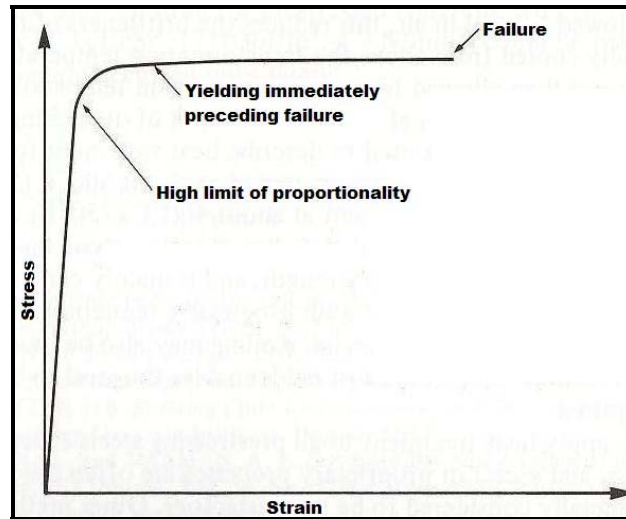


Figure 5: Ideal stress-strain diagram for prestressing steel
 [Adapted from Abeles and Bardhan-Roy, 1981]

Cold-drawn steel wire, alloy steel wire and bars have these attributes and are most common materials for tendons. Cold-drawn steel wire is produced in diameters up to 0.276 inch (0.7 mm). It has ultimate strength ranging from 250 to 300 ksi (1,725 to 2,070 MPa), and moduli of elasticity about 29,000 ksi (200 MPa).

Since the bond between smooth wires and concrete is low, weaving several wires into a strand gives a tendon of substantial capacity and excellent bonding capacity. Seven-wire strand is widely used both in pretensioning and post-tensioning. Strands are manufactured in diameters of 0.25 to 0.6 inch (6 to 15.2 mm). The most commonly used ones are the 0.6 in (15.2 mm) strand (Gerwick, 1993).

The properties of standard prestressing strands, wires, and bars conforming to the American Society for Testing and Materials (ASTM) Standard A416, A421, and A722, or to CSA Standard G279, are given in Table 6. Table 7 presents the required characteristics of prestressing tendons as specified by the ASTM Standards.

**Table 6: Standard prestressing strands, wires, and bars
(Prestressed Concrete Institute, 1985)**

Tendon Type	Grade f_{pu} , ksi, (MPa)	Nominal dimension		Weight plf (kg/m)
		Diameter in (mm)	Area in ² (mm ²)	
Seven-wire strands	250 (1724)	0.25 (6.4)	0.036 (23.2)	0.12 (0.18)
	270 (1862)	0.375 (9.5)	0.085 (54.8)	0.29 (0.43)
	250 (1724)	0.375 (9.5)	0.080 (51.6)	0.27 (0.40)
	270 (1862)	0.5 (12.7)	0.153 (98.7)	0.53 (0.79)
	250 (1724)	0.5 (12.7)	0.144 (92.9)	0.49 (0.73)
	270 (1862)	0.6 (15.2)	0.215 (138.7)	0.74 (1.1)
	250 (1724)	0.6 (15.2)	0.216 (139.4)	0.74 (1.1)
Prestressing wire	250 (1724)	0.196 (5)	0.0302 (19.5)	0.1 (0.15)
	240 (1655)	0.25 (6.35)	0.0491 (31.7)	0.17 (0.25)
	235 (1620)	0.276 (7)	0.0598 (38.6)	0.2 (0.3)
Deformed prestressing bars	157 (1082)	0.625 (15.9)	0.28 (180.6)	0.98 (1.46)
	150 (1034)	1 (25.4)	0.85 (548.4)	3.01 (4.48)
	150 (1034)	1.25 (31.75)	1.25 (806.4)	4.39 (6.53)
	150 (1034)	1.375 (34.9)	1.58 (1019.3)	5.56 (8.27)

**Table 7: Requirements for prestressing tendons specified by ASTM
(ASTM A416, A421, A722)**

Tendon Type	Minimum Tensile Strength, ksi (MPa)	Minimum Yield Strength, ksi (MPa)	Minimum Elongation at Rupture	
			%	Gage Length, in (cm)
0.5 and 0.6 in. (12.7 and 15.24 mm) stress-relieved strand	270 (1862)	230 (1586)	3.5	24 (61)
0.5 and 0.6 in. (12.7 and 15.24 mm) low-relaxation strand	270 (1862)	245 (1689)	3.5	24 (61)
0.276 in. (7 mm) wire	235 (1620)	200 (1379)	4.0	10 (25.4)
1, 1 1/4, and 1 3/8 in. (25.4, 31.75 and 34.9 mm) deformed prestressing bar	150 (1034)	120 (827)	4.0	20 d_b *

* d_b : Nominal diameter of reinforcing bar

1.3.5.3 ACI 318-08 maximum permissible stresses in concrete and reinforcement

Definition:

f_{py} = Specified yield strength of prestressing tendons, psi

f_y = Specified yield strength of nonprestressed reinforcement, psi

f_{pu} = Specified tensile strength of prestressing tendons, psi

f'_c = Specified compressive strength of concrete, psi

f'_{ci} = Compressive strength of concrete at time of initial prestress, psi

Stresses in concrete immediately after prestress transfer, before time-dependent prestress losses, shall not exceed the following:

a) Extreme fiber stress in compression	$0.60 f'_{ci}$	ACI clause 18.4.1
b) Extreme fiber stress in tension except as permitted in c)	$3\sqrt{f'_{ci}}$	
c) Extreme fiber stress in tension at ends of simply supported members	$6\sqrt{f'_{ci}}$	

Where computed tensile stresses exceed these values, bonded auxiliary reinforcement (nonprestressed or prestressed) shall be provided in the tensile zone to resist the total tensile force in concrete computed under the assumption of an uncracked section.

Stresses in concrete at service loads (after allowance for all prestress losses) shall not exceed the following:

a) Extreme fiber stress in compression due to prestress plus sustained load, where sustained dead load and live load are a large part of the total service load	$0.45 f'_c$	ACI clause 18.4.2
b) Extreme fiber stress in compression due to prestress plus total load, if the live load is transient	$0.60 f'_c$	
c) Extreme fiber stress in tension in precompressed tensile zone	$6\sqrt{f'_c}$	ACI clause 18.4.1
d) Extreme fiber stress in tension in precompression tensile zone of members (except two-way slab systems), where analysis based on transformed cracked section and on bilinear moment-deflection relationships shows that immediate and long-time deflections comply with the ACI definition requirements and minimum concrete cover requirements	$12\sqrt{f'_c}$	

Tensile stress in prestressing tendons shall not exceed the following:

a) Due to tendon jacking force But not greater than the lesser of $0.80 f_{pu}$ and the maximum value recommended by the manufacturer of prestressing tendons or anchorages.	$0.94 f_{py}$	ACI clause 18.5.1
b) Immediately after prestress transfer But not greater than $0.74 f_{pu}$	$0.82 f_{py}$	
c) Post-tensioning tendons, at anchorages and couplers, immediately after tendon anchorage	$0.70 f_{py}$	

1.3.5.4 2004 AASHTO maximum permissible stresses in concrete and reinforcement

Concrete stresses before creep and shrinkage losses

a) Stress in compression of pre-tensioned members	$0.60 f'_{ci}$	AASHTO clause 5.9.5.3 and 5.9.5.4 (Adapted: units in psi)
b) Stress in compression of post-tensioned members	$0.55 f'_{ci}$	
c) In tension area with no bonded reinforcement	200 psi or $3\sqrt{f'_{ci}}$	
d) Where the calculated tensile stress exceeds c), bonded reinforcement shall be provided to resist the total tension force in the concrete computed on the assumption of an uncracked section. The maximum tensile stress shall not exceed:	$7.5\sqrt{f'_{ci}}$	

Concrete stresses at service load after losses

a) Stress in compression	$0.40 f'_c$	AASHTO clause 5.9.4.2 (Adapted: units in psi)
b) Tension in the precompressed tensile zone <ul style="list-style-type: none"> - For members with bonded reinforcement - For sever corrosive exposure conditions, such as coastal areas - For members without bonded reinforcement 	$6\sqrt{f'_c}$ $3\sqrt{f'_c}$ 0	

Cracking stresses: modulus of rupture f_r from tests or if not available

For normal weight concrete	$7.5\sqrt{f'_c}$	AASHTO clause 5.4.2.6 (Adapted: units in psi)
For sand-lightweight concrete	$6.3\sqrt{f'_c}$	
For all other lightweight concrete	$5.5\sqrt{f'_c}$	

Prestressing steel stresses

a) Due to tendon jacking	$0.94 f_{py} \leq 0.80 f_{pu}$	AASHTO clause 5.9.5.4 (Adapted: units in psi)
b) Immediately after prestress transfer	$0.82 f_{py} \leq 0.74 f_{pu}$	
c) Post-tensioning tendons at anchorage, immediately after tendon anchorage	$0.70 f_{py}$	

Where:

For low-relaxation: $f_{py} = 0.90 f_{pu}$

1.4 Precasting

The following sections will look into the benefits of precasting, also known as prefabrication (Section 1.4.1), the general method used in precast shops (Section 1.4.2), and the few techniques used to make this practice efficient (Section 1.4.3). Section 1.4.4 presents a research conducted by Mokhtarzadeh and French (2000) comparing different HPC attributes and mixtures.

1.4.1 Benefits of precasting

In 2001, the AASHTO Technology Implementation Group chose prefabricated bridge elements and systems as one of the innovative technologies that promised the highest payoff. The FHWA (Federal Highway Administration) – through its Innovative Bridge Research and Construction program and the Resource Center – also championed prefabrication for accelerated construction. Their vision was to solve bridge deterioration with accelerated construction through increased prefabrication. As a matter of fact, prefabrication technology carries many advantages for bridge owners, engineers, builders, and the traveling public (Naito, Brunn, Parent and Tate, 2005).

In the case of precast construction there are savings in formwork assembly, concrete casting, and curing offsite in the controlled environment of a precast plant. In addition to the more rapid construction on site, the quality of the components is improved, translating into lower longer service life and lower life-cycle costs. Shipment of precast components to the job site rather than cast-in-place construction also reduces transportation costs and the impact on the environment (Naito, Brunn, Parent and Tate, 2005).

From a design point of view, fewer constraints, such as extreme elevations, long stretches over water, and tight urban work zones, are to be considered and overcome. Safety is also improved because of the reduced time exposure for workers and public who travel through construction zones. Moreover, prefabricating takes elements and systems out of the critical path of a project schedule (Naito, Brunn, Parent and Tate, 2005).

All factors put together, prefabrication makes some bridge design, whether involving a new construction or rehabilitation, more feasible, affordable and constructible.

1.4.2 Production methods

Precasting plants follow a conventional method of fabrication. In order to be productive and competitive, a cycle should not take more than 24 hours to be completed. It involves setting up

the formwork, the reinforcement and prestressing, casting, curing, releasing the prestressing once the concrete has hardened and removing the formwork.

The following section represents the main steps employed at Schuylkill Products Inc., a certified PCI plant in Cressona, Pennsylvania (Naito, Brunn, Parent and Tate, 2005).

The beams are normally cast on long stressing beds (Figure 6a). The casting bed is a multi strand tensioning operation which allows for simultaneous stressing of all strands in the cross-section (Figure 6b). This configuration also allows for slow release of prestress after casting operations are complete, thus minimizing uneven release and unintentional damage to the precast members.



a) Stressing bed



b) Stressing strands

Figure 6: Prefabrication procedure
(Naito, Brunn, Parent and Tate, 2005)

The reinforcement is then put in place and the formwork is closed. Concrete is placed and left to cure overnight. Special techniques are put in place (Section 1.4.3) to accelerate this phase and allow faster prestressing release, ideally the following morning, if the target strength is reached.



Figure 7: Flame cut unstressed strands at bulkhead
(Naito, Brunn, Parent and Tate, 2005)

The release of the prestressing is done by flame cutting (Figure 7). The formwork is then to be re-oiled and prepared for a new production cycle.

1.4.3 Particularities of precast concrete

Successful precast operations are dependent on rapid gain of concrete strength, leading to a faster production rate and a more beneficial financial outcome. In order to be able to release the stress faster, steam curing is widely employed in precast prestressed concrete manufacture to accelerate gain of strength (Benaim, 2008). A great deal of attention has been directed at the effect of this accelerated curing on long-term ultimate compressive strength, durability, shrinkage and creep, loss of prestress, etc. Other studies have been directed to the determination of the optimum cycle for the steam-curing process.

Two methods of steam curing are used: live steam at atmospheric pressure used for enclosed cast-in-place structures and large precast concrete units, and high-pressure steam in autoclaves, for small manufactured units (Cement Association of Canada, 2006).

Steam curing at atmospheric pressure is generally done in an enclosed environment to minimize moisture and heat losses (Cement Association of Canada, 2006). A typical cycle consists of (Figure 8):

- (1) An initial 3 to 5 hours delay prior to steaming, allowing for some concrete hardening resulting in higher early strengths
- (2) A period for increasing the temperature

- (3) A period holding the maximum temperature constant, and
- (4) A period for decreasing the temperature

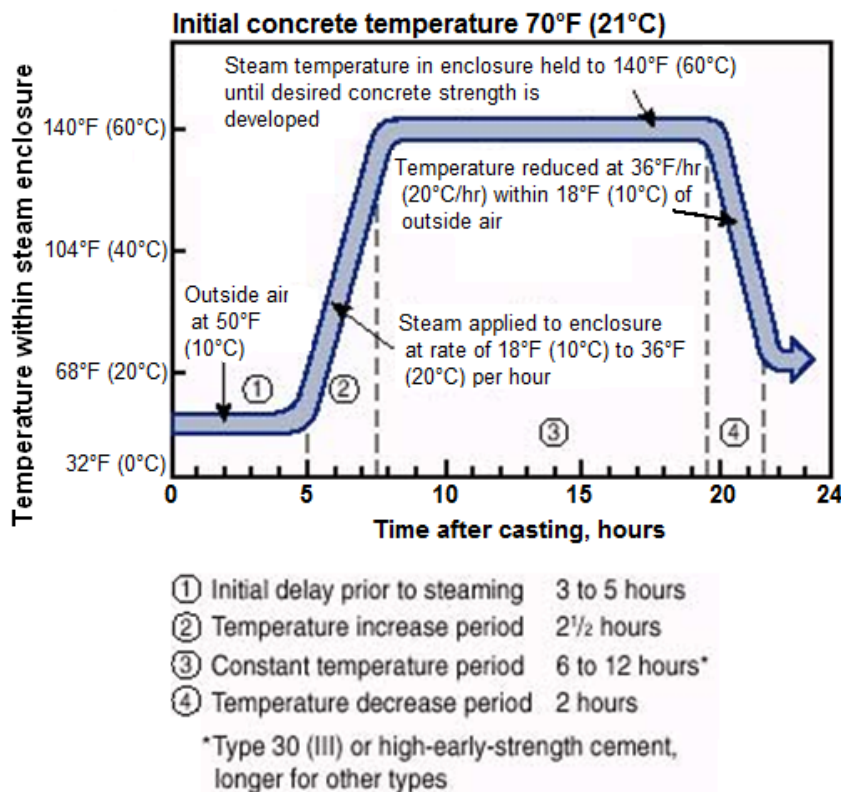


Figure 8: Typical atmospheric steam curing cycle
 [Adapted from Cement Association of Canada, 2006]

Properly applied steam curing improves the quality of the concrete product. In fact, it reduces drying shrinkage and creep when compared to regularly cured concrete at 73°C for 28 days (Klieger, 1960, and Tepponen and Eriksson, 1987)

Steam curing at atmospheric pressure has been one of the most important techniques which have made it possible to attain economical production of prestressed concrete elements by permitting daily turnover of forms. It has also made it practicable to have a short cycle between manufacture and erection, eliminating in large part the need for stockpiles and inventory.

1.4.4 Alireza Mokhtarzadeh and Catherine French's experiment (2000)

Mokhtarzadeh and French (2000) examined the mechanical properties (compressive strength, modulus of elasticity and tensile strength) of high performance concrete. They tested over 6,300

specimens from 142 HPC mixtures with 28-day compressive strengths in range of 8,000 to 18,600 psi (55.2 to 128.2 MPa). The material variables included the following:

- Composition of cementitious material: ASTM C 150 portland cement and combinations of ASTM C 68 Class C fly ash and silica fume different percentages
- Type and brand of cement (Types I and III from two different brands)
- Type of silica fume: dry-densified and slurry
- Type and brand of superplasticizer: five types
- Type and source of coarse aggregates: high and low-absorption limestone, granites, round and crushed river gravel
- Aggregate gradation
- Maximum aggregate size: $\frac{1}{2}$ and $\frac{3}{4}$ in (12.7 and 19 mm)

For each specimen cured in standard lime-saturated water, a companion specimen was heat-cured in a monitored electronically-controlled environmental chamber. After casting, the curing routine was: 3 hours at room temperature followed by a 2.5 hours period to increase the temperature from 120°F to 160°F (49°C to 71°C); the temperature was then to be kept constant over 12 hours to finally return to room temperature over a 2 hours period.

Heat-cured specimens yielded higher early-age compressive strengths than moist-cured specimens. At later ages, however, continuous application of moisture resulted in the continued increase in compressive strength of moist-cured specimens, whereas the strength of the heat-cured specimens levelled off.

Mokhtarzadeh and French also showed that moist-curing was essential for getting full advantage of using fly ash in a mixture. In the absence of adequate moisture, any benefit from inclusion of fly ash was limited to grain refinement of the cement matrix. Moist-cured specimens also proved to have an increasing modulus of elasticity with time. In fact, at 182 and 365 days of age, moist-cured cylinders had, 106 and 108% of the 28-day compressive strength value, whereas the heat-cured were only at 94 and 96%, respectively.

The compressive strength developed at early ages was higher for moist-cured concrete made with rapid hardening portland cement (Type III) than for ordinary portland cement (Type I).

1.5 Self-consolidating concrete

Concrete placement in precast plants can be time consuming and lead to unsatisfactory results if vibrations are not done properly. One innovative solution may lie in the use of a highly flowable self-consolidating concrete (SCC) mix.

1.5.1 SCC characteristics

SCC is a non-segregating concrete that can flow and fill formwork without any mechanical vibration. This highly flowable concrete was developed in Japan in the 1980s as a solution to improve the constructability of reinforced concrete structures (Ozyildirim and Lane, 2003). Since no mechanical vibration is needed when placing this concrete, significant savings in labour costs and construction time can be achieved. SCC also has the potential of increasing durability and quality resulting in a lower cost of construction. Further advantages include noise reduction during construction and a reduction of surface defects leading to a more appealing architectural finish (Gurjar, 2004).

A typical SCC mix is designed by ensuring a proper flowability and viscosity in the fresh state (Ozyildirim and Lane, 2003). Flowability is normally achieved by using high-range water-reducing admixtures (HRWRA) while viscosity is ensured by using a proper selection of fines and aggregates and by using a viscosity modifying admixture (VMA). The flowability of the product allows for placement in members with high amount of reinforcement congestion. The use of conventional concretes in this situation would require significant mechanical vibration and could result in a risk of honeycomb formation.

On the other hand, self-consolidating concrete also has the potential of lowering the permeability of the concrete resulting in reduced durability and an increase of the life-cycle costs.

1.5.2 Testing fresh-state properties of SCC

Several methods can be used to evaluate the various properties of SCC in the fresh state. Tests can be broadly split into two categories: free flow tests and restricted flow tests. These procedures enable an assessment of the filling ability, passing ability, and segregation resistance of SCC. Among the most common tests for assessing the free deformability of SCC is the slump flow test. Methods that are typically used to assess the restricted deformability include the L-box and the J-ring tests. Other tests, such as column segregation, surface settlement and rheology tests are covered in the following section.

1.5.2.1 The Slump flow and T-20 tests

A conventional slump cone is filled with concrete and placed on a Plexiglas table on which a concentric diameter of 20 inches (50.8 cm) is marked (Figure 9). The cone is then lifted and the time for the concrete diameter to reach the 20 in benchmark is recorded. This time is referred to as the T-20 value and typically varies between 2 to 10 seconds for SCC. A higher T-20 value indicates a more viscous mix: a concrete more appropriate in congested reinforcement. A lower T-20 value may be appropriate for concrete that has to travel long horizontal distances without much obstruction. When the concrete stops flowing, its final diameter (D-final) is measured (Gurjar, 2004).

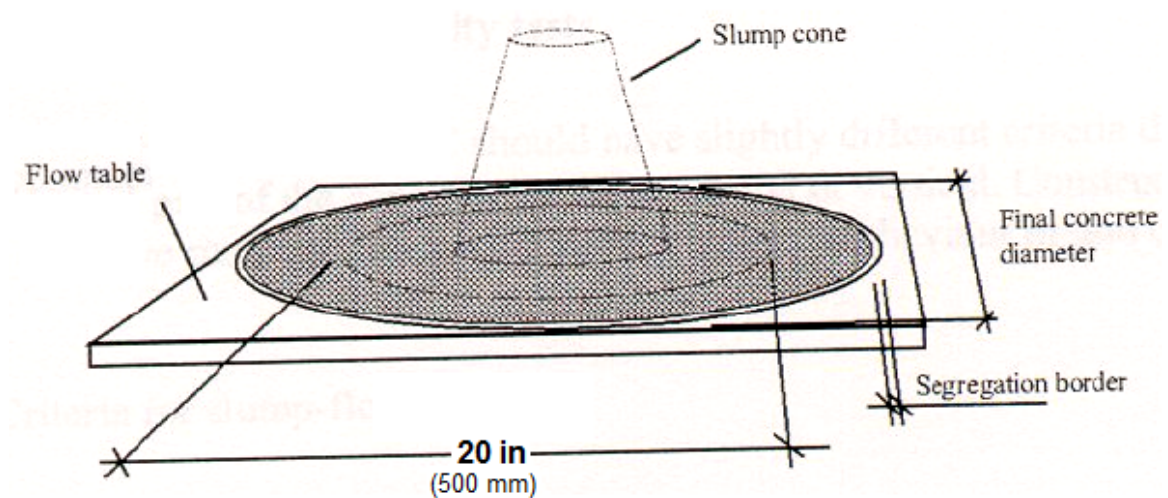


Figure 9: Slump flow test
(Gurjar, 2004)

While performing the slump flow test, the resistance to segregation is observed through a Visual Stability Index (VSI). The VSI is established based on whether bleed water is observed at the leading edge of the spreading concrete or if aggregates pile at the center. VSI test ranks the stability on a scale from 0, for “highly stable”, to 3, for unacceptable stability (Gurjar, 2004). ASTM C 1611 provides descriptions of the surface bleed, mortar halo and aggregate distribution to properly select the appropriate VSI.

Due to the simple nature of this test procedure, slump flow is one of the most common methods used in practice to measure the workability of SCC in its fresh state.

1.5.2.2 The J-ring test

The J-ring test is used to determine the passing ability of the concrete. It consists in a steel ring of 12 in (30.5 cm) diameter, drilled vertically with holes to accept threaded sections of reinforcement bar, 4 in (10.2 cm) height (Figure 10). These sections of bar can be of different diameters and spaced at different intervals (Gurjar, 2004).

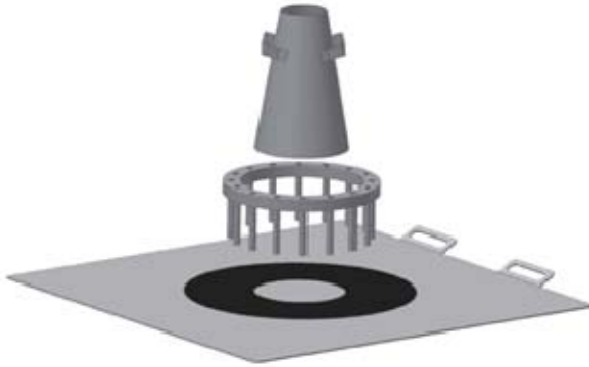


Figure 10: J-ring test
[Adapted from Gurjar, 2004]

The J-ring is placed centrally on the base-plate with the slump cone. The cone is filled without tamping and lifted to allow the concrete to flow out freely (Gurjar, 2004). When the concrete comes to rest, the final diameter is measured. The difference between the slump flow's final diameter and the J-ring flow's final diameter is a measure of the passing ability. A difference of less than 1 in (2.54 cm) indicates good passing ability. A difference greater than 2 in (5.1 cm) indicates poor passing ability (ASTM C1621). The J-ring test, used in conjunction with the slump flow also indicates the flowing ability of concrete.

1.5.2.3 The L-box and filling ability tests

The L-box test measures different properties, such as flowability, blocking and segregation. The vertical part of the box, with the extra adapter mounted, is first filled with concrete and left to rest for a minute (Figure 11). The sliding gate is then lifted allowing the concrete to flow out of the vertical part into the horizontal part of the L-box. On its way, concrete passes through a layer of reinforcement with bars usually spaced 1.5 in (3.8 cm) apart. After the sliding gate is removed, the time for the leading edge of the concrete to reach the 8 in and 16 in (20.3 cm and 40.6 cm) mark is recorded (Gurjar, 2004).

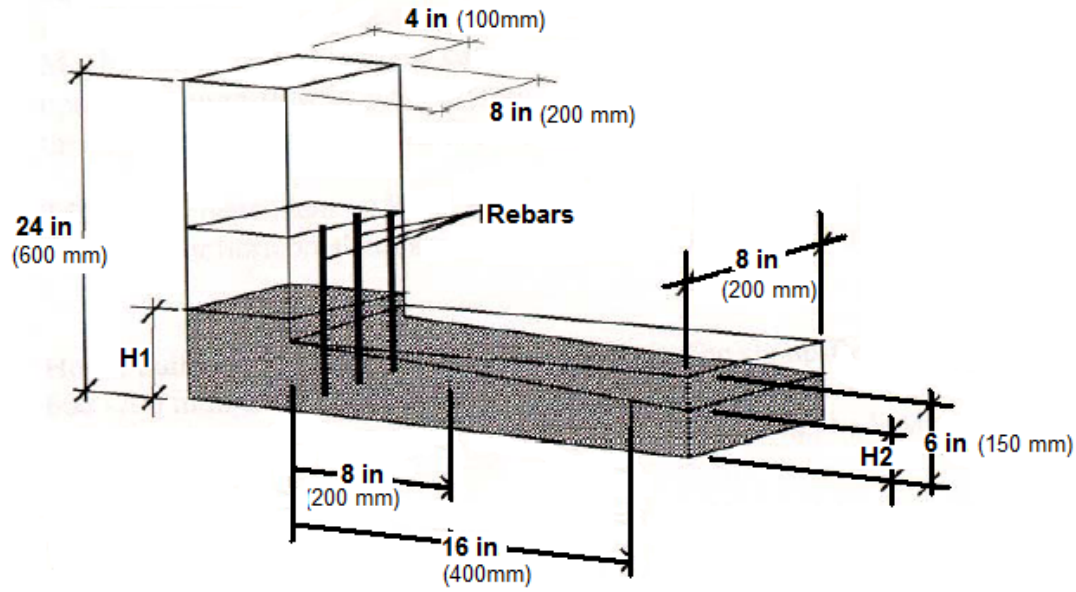


Figure 11: L-box test
[Adapted from Gurjar, 2004]

The concrete is then left to rest in the apparatus and the heights of the concrete at the end of the horizontal portion, H_2 , and in the vertical section, H_1 , are measured. The blocking ratio, H_1/H_2 , is known as the filling capacity. The filling capacity test evaluated both the narrow-opening passing ability and the self-leveling ability simultaneously (Hwang, Khayat and Bonneau, 2006). For most tests, the blocking ratio should range between 0.80 and 0.85 (Gurjar, 2004). A smaller value would indicate that the concrete built a plateau behind the reinforcement layer by either blocking or segregating. Blocking usually displays itself by coarse aggregates gathered between the reinforcement bars. If coarser aggregates are distributed on the concrete surface all the way to the end of the horizontal part, the concrete can be regarded as stable. Both blocking and stability can be detected visually (Gurjar, 2004).

While the test does give valuable information about filling and passing ability, and to a lesser extent, segregation resistance, the test is not as simple as the slump flow test. Since there are no standardized dimensions, results from different test apparatuses cannot be compared directly (Koehler and Fowler, 2003).

1.5.2.4 The column segregation test

The column segregation test evaluates the static stability of a concrete mixture by quantifying the aggregate segregation. A column is filled with concrete and left undisturbed until the concrete comes to a rest (Figure 12). The column is then separated into three or four pieces. Each section is

removed individually and the concrete from that section is washed over a No. 4 sieve. The retained aggregate are then washed and weighed. A non-segregating mix will have a consistent aggregate mass distribution in each section, as opposed to a segregating mix which will have higher concentrations of aggregate in the lower sections.

The percent of static segregation, known as the column segregation index, is then evaluated according to ASTM C 1610.



Figure 12: Column segregation test
(National Ready Mixed Concrete Association, 2008)

1.5.2.5 The surface settlement test

The surface settlement test is a simple way to evaluate the stability of concrete and its ability to insure the proper suspension of aggregate. A 20 in-high (508 mm-high) PVC column measuring 5 inches (12.7 cm) in diameter is filled with approximately 17.5 in (445 mm) of concrete. A linear deflector, or LVDT, is then fixed on top on an acrylic transparent thin plate positioned at the top surface of the concrete column allowing the surface settlement to be monitored (Khayat, 1999). In general, SCC used in structural applications should have a maximum surface settlement of 0.5% of the concrete column height (Hwang, Khayat and Bonneau, 2006).

1.5.2.6 The rheology test

It is difficult to evaluate the high flowability of SCC by means of conventional slump test. In fact, concretes with the same slump may flow differently and have different workability. The reason two concretes with the same slump behave differently during placement is that concrete flow cannot be defined by a single parameter (Bui, Akkaya, and Shah, 2002). Most researchers agree

that the flow of concrete can be described reasonably well using a Bingham equation, a linear function of the shear stress (the concrete response) versus shear rate (Banfill, *et al.*, 2000):

$$\tau = \eta \dot{\gamma}$$

Where:

$\tau =$ Shear stress

$\eta = \mu + \frac{\tau_o}{\dot{\gamma}} =$ Viscosity of the Bingham fluid ($Pa \cdot s$)

$\mu =$ Plastic viscosity ($Pa \cdot s$)

$\tau_o =$ Yield value (Pa)

$\dot{\gamma} =$ Rate of shear ($1/s$)

The yield stress and the plastic viscosity are two parameters provided by the Bingham equation. The yield stress correlates reasonably well with the slump value, but the plastic viscosity cannot be measured using the slump test. In fact, plastic viscosity governs the concrete flow behaviour once the flow has started, i.e., after the yield stress is overcome. The existence of the plastic viscosity justifies the different behaviours of concrete, with the same slump, during placements (Banfill, *et al.*, 2000).

The parameters needed in Bingham equation are measured using an instrumented and automated apparatus, known as rheometer (Figure 13). This instrument, developed in Canada by D. Beaupré and S. Mindess, was developed from the Tattershall MK III. It is applicable to concretes with a large range of workability, and has been successfully used for SCC, HPC, pumped concrete, dry and wet-process shotcrete, fiber reinforced concrete, and normal concrete. It has also been used on a few job sites as a mean of quality control.

The apparatus is fully automated and uses a data acquisition system to drive an impeller rotating in fresh concrete. The test parameters are easy to modify in order to produce any required test sequence. The analysis of the results is also automated and the rheological parameters, yield stress and plastic viscosity, are displayed on the computer screen, along with the coefficient of correlation from the linear Bingham behaviour.



Figure 13: Rheology test

1.5.3 Comparison between SCC and normal concrete

Noting the increasing demand of SCC in housing and civil engineering work, Mohammed Sonebi, Adil K. Tamimi, and Peter J.M. Bartos (2003) tested the in-place performance of beams cast with SCC. Their experiment consisted in testing full-scale beams cast using ordinary concrete and their companion SCC with two configurations of reinforcement bars. Standard compressive strength of 5,000 and 8,700 psi (34.5 and 60 MPa) were used (Sonebi, *et al.*, 2003).

The properties of the beams, such as the mode of failure and the load deflection response, were found to be similar for both SCC and ordinary concrete. For concrete of higher strength, it was observed that the ultimate moment capacity of the SCC beam was comparable to the reference beam but the maximum deflection of the SCC beam was slightly higher than that of the reference point. Moreover, at service load, there were more and wider cracks with greater penetration with the reference mixture than with the SCC of 8,700 psi (60 MPa). This was attributed to the difference of compressive strength: while the reference mixture of the ordinary concrete was at 8,700 psi (60 MPa), after 3 months, the SCC was at 8,600 psi (59.3 MPa). The maximum strength difference was less than 7% (Sonebi, *et al.*, 2003).

1.6 Objectives of this Research Program

The main objective of this research program is to investigate the applicability of existing design provisions provided by the AASHTO specifications, for the use of SCC in precast pretensioned bridge girders. The following aspects will be examined:

- The effect of SCC on the ease of casting, surface quality, heat generation, etc.
- The effect of SCC on the shear capacity
- The effect of SCC on crack formation
- The effect of high strength SCC on the shear capacity

Chapter 2: Experimental Program

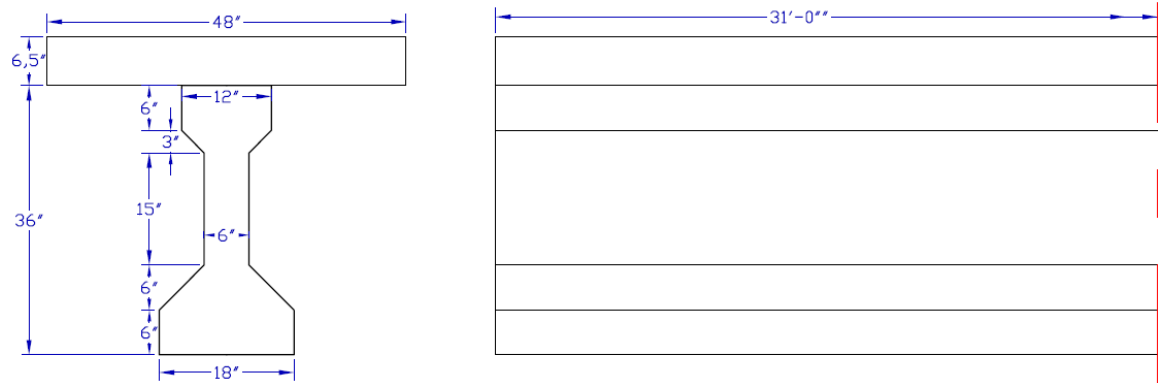
2.1 Design of the beam specimens

The experimental program, carried out in the Department of Civil Engineering Structures Laboratory at McGill University, consisted of constructing and testing four full-scale precast, prestressed bridge girders, AASHTO Type II, specimens (Figure 14). The girders had an overall length of 31 feet (9.4m) with a center-to-center span of 29 feet (8.8m). They were cast in four batches with different concrete attributes: two non air-entrained SCC mixtures and two high-performance concretes. For each type, compressive strengths of 8,000 and 10,000 psi (55.2 and 69 MPa) were chosen for the testing (Table 8). Their respective target release strengths, at 18 hours, were 5,000 and 6,250 psi (34.5 and 43 MPa). The High-Range Water-Reducing Admixture (HRWRA) concentrations for the SCC mixture were adjusted to obtain a slump flow of 26.8 ± 0.8 in (680 ± 20 mm). The target slump for the HPC mixtures was 6.3 ± 0.8 in (160 ± 20 mm). All four beams were steam cured for an 18 hours period (Section 2.3.1).

Table 8: Specimen Identification

Specimen designation	Compressive strength, <i>psi (MPa)</i>	Release strength, <i>psi (MPa)</i>	Concrete mix
H8	8,000 (55.2)	5,000 (34.5)	High-Performance Concrete
H10	10,000 (69)	6,250 (43)	High-Performance Concrete
S8	8,000 (55.2)	5,000 (34.5)	Self-Consolidating Concrete
S10	10,000 (69)	6,250 (43)	Self-Consolidating Concrete

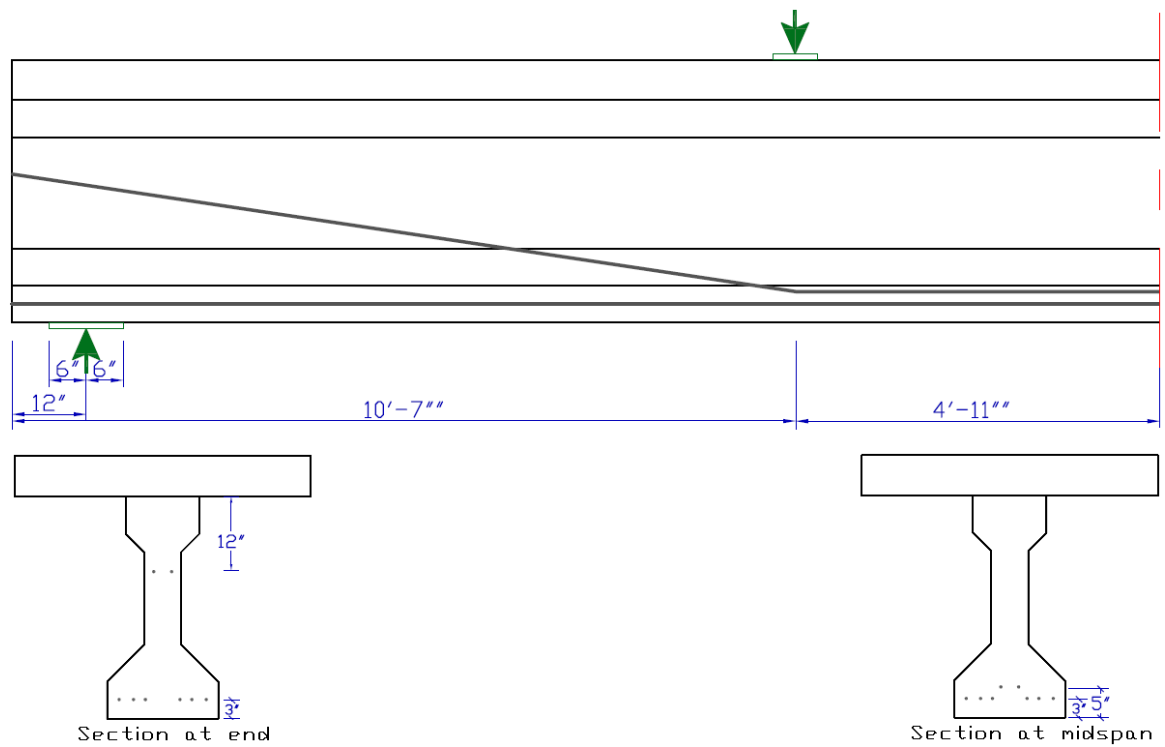
A 6.5 inches (165 mm) deep by 48 inches (1219 mm) wide cast-in-place deck slab was cast on top of each girder at least twenty eight days after the prestress release. During the casting, the girder was sitting on its end supports and the formwork was supported on the ground rather than being supported directly on the precast girder. The deck slab was cast with a conventional air-entrained concrete with a target compressive strength of 5,000 psi (34.5 MPa). It contained four No. 5 reinforcing bars in the longitudinal direction and No. 5 transverse bars spaced at 12 inches (305 mm) and 11 inches (280 mm) for the 8,000 and 10,000 psi (55.2 and 69 MPa) girders, respectively. Following the casting, the deck slab was covered with burlap and polyethylene and was moist cured for 5 days.



Unit conversion: 1.0' = 12" = 304.8 mm

Figure 14: Section properties of AASHTO type II girders

Each girder was prestressed with eight Grade 270 seven-wire low-relaxation prestressing strands of 0.6 in (15.2 mm) diameter. Six of the strands were straight and two were harped twice, 4'-11" (1.5 m) on each side of the mid-span (Figure 15 and Figure 16).



Unit conversion: 1.0' = 12" = 304.8 mm

Figure 15 - Details of precast pretensioned AASHTO II girders

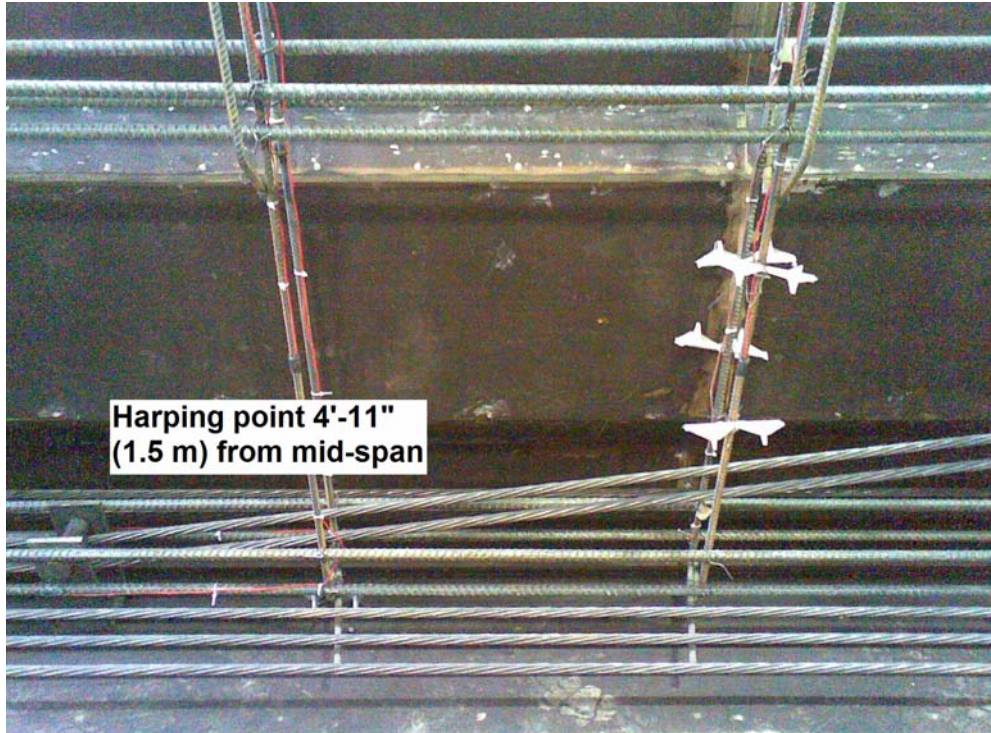


Figure 16: Details of the pretensioning

Four No. 5 longitudinal reinforcing bars were added near the top of the girder to control cracking at prestress release and four more were added in the bottom flange to increase the flexural capacity. The stirrup reinforcement was chosen to satisfy the 2004 AASHTO Clause 5.8.2.5 for minimum transverse reinforcement stipulating:

$$s \leq \frac{A_v f_y}{0.0316 \sqrt{f'_c} b_w} \quad \text{AASHTO clause 5.8.2.5}$$

Without exceeding the maximum spacing, specified in Clause 5.8.2.7, for transverse reinforcement which limits, for low shear stresses, the spacing to 24 inches (610 mm).

Hence, for both girders with the nominal concrete strength of 8 ksi (55.2 MPa), using No. 3 double legged stirrups with nominal yield stress of 60 ksi (414 MPa), required a spacing of:

$$s \leq \frac{(2 \times 0.11 \text{ in}^2) \times 60 \text{ ksi}}{0.0316 \sqrt{8 \text{ ksi}} \times 6 \text{ in}} = 24.6 \text{ in} \quad (625 \text{ mm})$$

$$s \leq 24.0 \text{ in} \quad (610 \text{ mm}) \quad \text{controls}$$

Similarly, the required spacing for both girders with the nominal concrete strength of 10 ksi (69 MPa), with the same No. 3 double legged stirrups, is of:

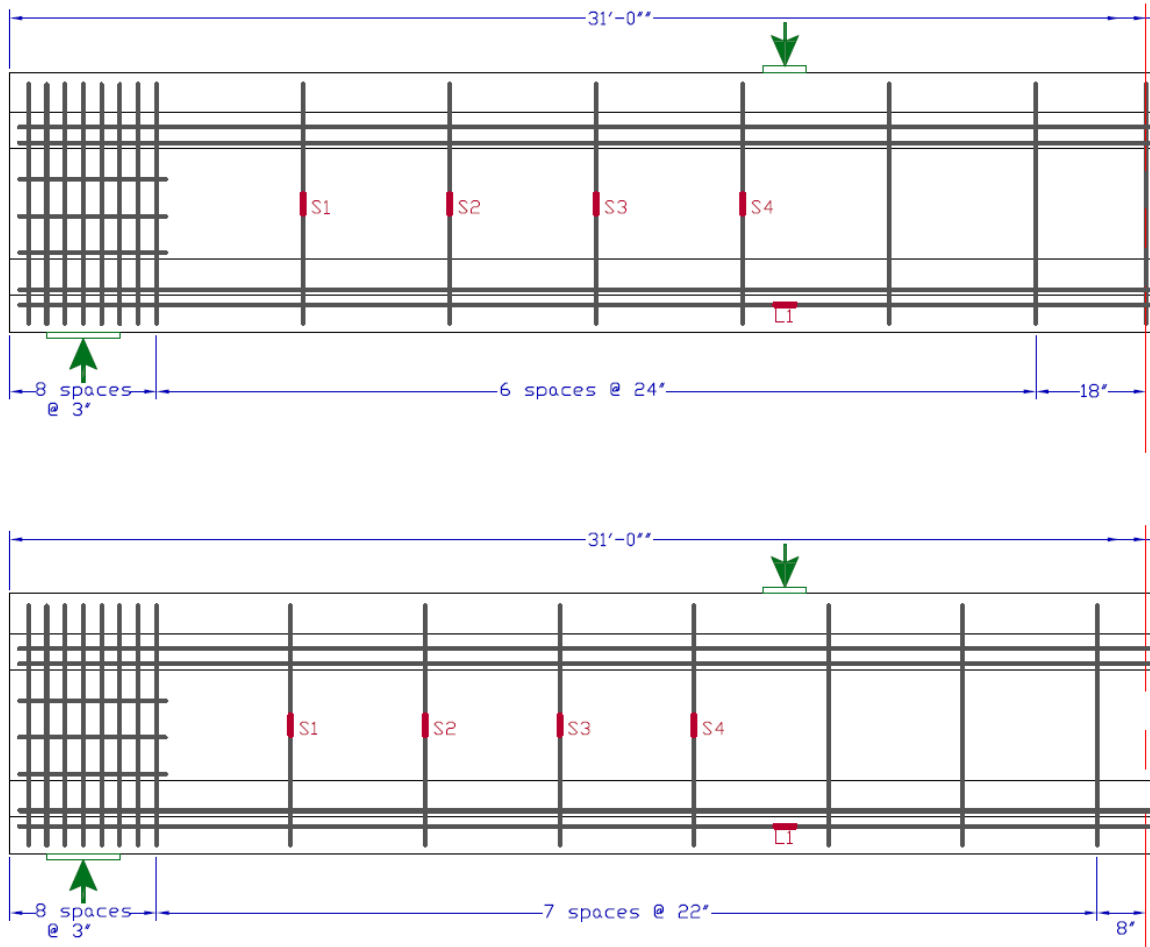
$$s \leq \frac{(2 \times 0.11 \text{ in}^2) \times 60 \text{ ksi}}{0.0316 \sqrt{10 \text{ ksi}} \times 6 \text{ in}} = 22.0 \text{ in} \quad (560 \text{ mm}) \quad \text{controls}$$

$$s \leq 24.0 \text{ in} \quad (610 \text{ mm})$$

Some of the No. 3 stirrups and No. 5 longitudinal reinforcement were instrumented with strain gages as shown in Figure 17.

As is common practice, additional longitudinal and transverse reinforcements were placed in the end regions of each girder as shown in Figure 17 and Figure 18. This consisted of six No. 3 longitudinal reinforcement of 24 inches (610 mm) long, along with No. 3 double legged stirrups spaced at every 3 inches (76 mm) over a 24 in (610 mm) region.

In addition, in order to prevent horizontal shear distress, additional interface shear reinforcement was also provided across the interface of the precast girder and cast-in-place deck slab. This consisted of additional No. 3 U-bars at each full-depth stirrup location as shown in Figure 19 and Figure 20.



Unit conversion: 1.0' = 12" = 304.8 mm

Figure 17: Details of non-prestressed reinforcement



Figure 18: Details of reinforcing bars in end region

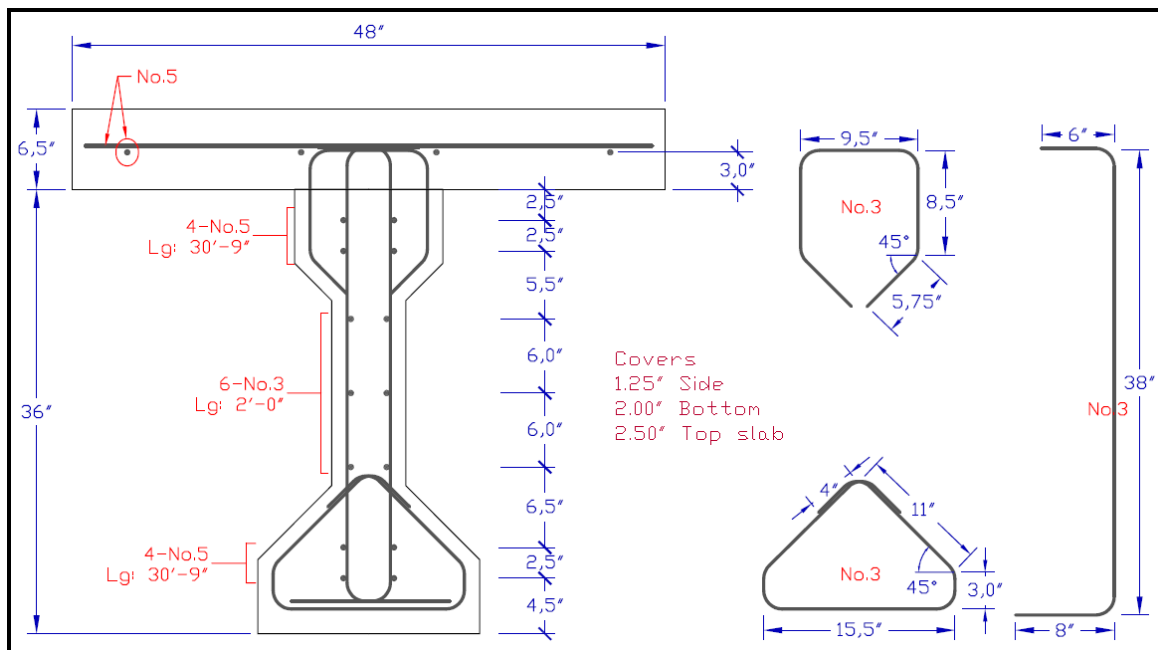


Figure 19: Details of the cross section



Figure 20: Details of stirrups and interface shear reinforcement

2.2 Instrumentation and Test Setup

2.2.1 Pretensioning operation

The pretensioning operation in the stressing bed, carried out at one end of each of the girders, was achieved using a pretensioning jacking system. Its pressure was calibrated to determine accurately the force applied to each strand. All eight strands were tensioned to a stress level corresponding to $0.7 f_{pu} = 0.7 \times 270 = 189 \text{ksi}$ (1.3 GPa). The six straight strands were tensioned first, one strand at a time, starting with the outermost strands. The two inclined were then tensioned. In order to minimize losses due to anchorage set in this relatively short stressing bed, this operation involved stressing each strand to the desired level, releasing the jack to set the anchor and then restressing it and placing steel shims under the anchorage sleeve.

Figure 21 shows the stressing operation of one of the straight strands (a), and the anchorage at the fixed end, known as “dead end” (b).



(a) Stressing of straight strand



(b) Anchorage at “dead end”

Figure 21: Jacking of 0.6 in (15.2 mm) diameter strands
(Khayat and Mitchell, 2009)

2.2.2 Casting and steam curing

Prior to casting, two vibrating wires strain gages were installed in each girder: one at mid-span, and the other 4 feet (1219 mm) from mid-span close to one of the harping points. These gages measured the concrete temperature and the concrete strain at the level of the straight prestressing strands, determining the prestress losses with time. The measured strains from the vibrating wire gages were compared to the predicted strains for the total deformation, which accounted for elastic shortening, creep, and shrinkage of the concrete. This comparison was performed by others and falls out of the scope of this thesis. Results can be found in the NCHRP report 18-12, “Self-consolidating concrete for precast, prestressed concrete bridge elements” by Khayat and Mitchell (2009).

Once the instruments and the steel cage were put in place and the strands were pretensioned, the formwork was closed and the casting of the concrete was ready to begin. Figure 22 shows the girder prior to that step.



Figure 22: Reinforcing cage in formwork prior to casting

The concrete was mixed at Unibéton's ready-mix plant in Laval and delivered to the structural laboratory of McGill University. The two HPC girders, H8 and H10, were cast using a concrete bucket and internal vibrators (Figure 23). Casting was time consuming and required the help of a big crew. The casting of the two SCC girders, S8 and S10, on the other hand, was much easier as the concrete was directly poured to the middle of the girders and required no vibration. A chute was used to deliver the concrete from the truck to the girders, at which point concrete made its way to both ends (Figure 24). A small layer of SCC was added in the top end regions of the girders to complete concreting.



Figure 23: HPC girder casting operation



Figure 24: SCC girder casting operation
(Khayat and Mitchell, 2009)

Two hours and a half and three hours after the initial contact of cement and water for the 8,000 and 10,000 psi (55.2 and 69 MPa) concrete mixtures, respectively, was initiated the steam curing process. The curing chamber consisted of sheets of Styrofoam 1.5 inch (38 mm) thick covered with 6 mil polyethylene sheets (Figure 25). Four steamers, two on each side of the girder, and an electric fan were installed inside the curing chamber to provide the steam required and allow its uniform circulation.

In order to monitor the temperature variation of each girder and that of the steam curing chamber, a total of eight thermo-couples were used. Four of them were installed inside each girder, two near the bottom and two near the top of the girder, while four others were used to determine chamber temperature.

The temperature history of the concrete was monitored during the entire steam curing process and the results are depicted in Figure 26 to Figure 29. The targeted chamber temperature for the 8,000 psi and 10,000 psi (55.2 and 69 MPa) mixtures was set at 131°F (55 °C) and 140°F (60 °C), respectively. In order to prevent the concrete temperature from exceeding 150 °F (65 °C), the volume of steam was reduced when the concrete temperature reached 122 °F (50 °C) and 131 °F (55 °C) for the 8,000 and 10,000 psi (55.2 and 69 MPa) concretes, respectively.

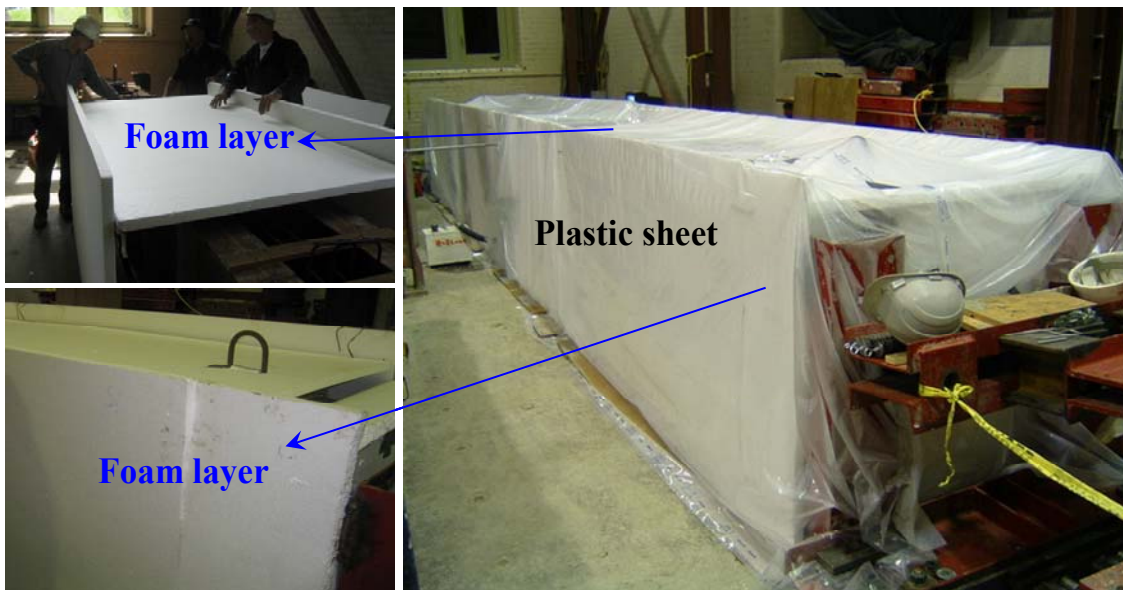


Figure 25: Steam curing chamber used for AASHTO Type II girders
(Khayat and Mitchell, 2009)

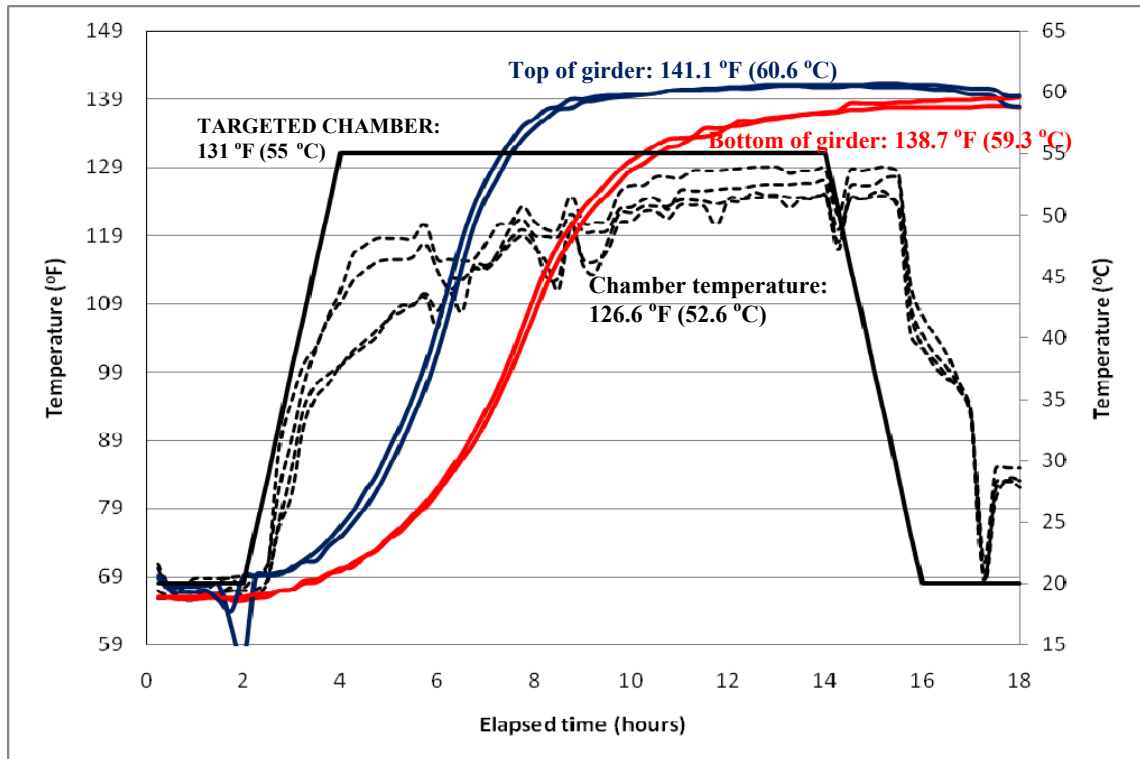


Figure 26: Temperature history of chamber and concrete during steam curing – HPC 8,000 psi (55.2 MPa)

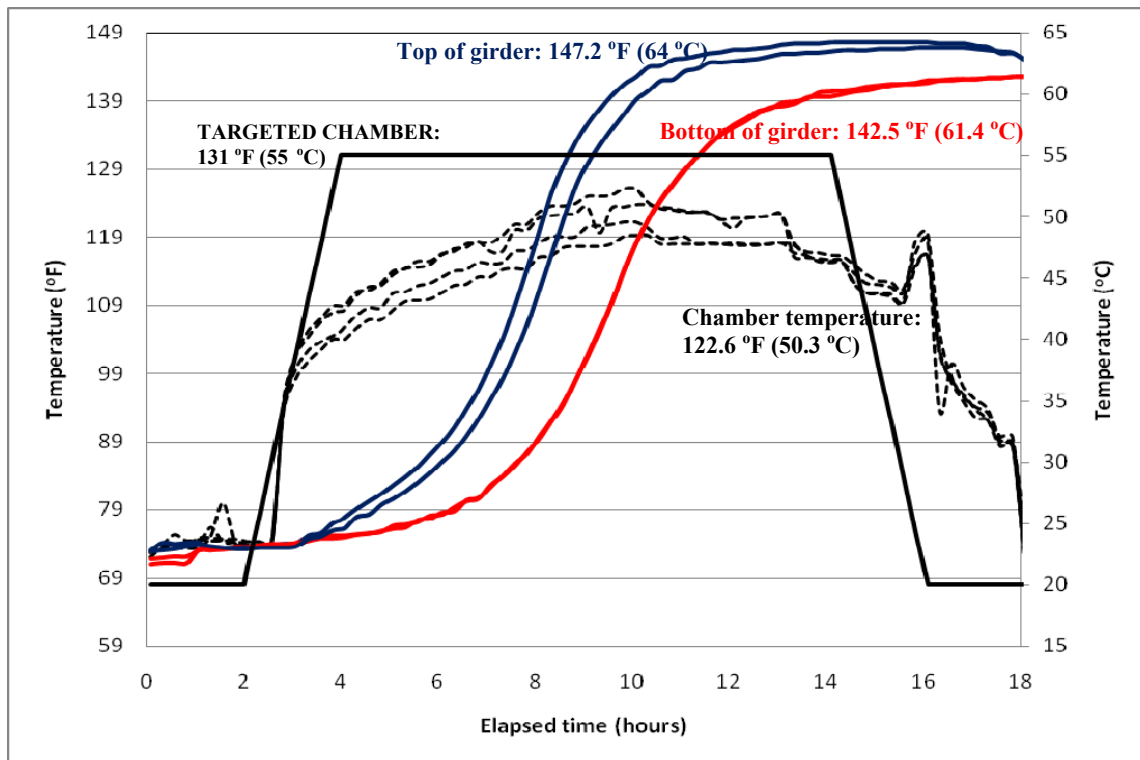


Figure 27: Temperature history of chamber and concrete during steam curing – SCC 8,000 psi (55.2 MPa)

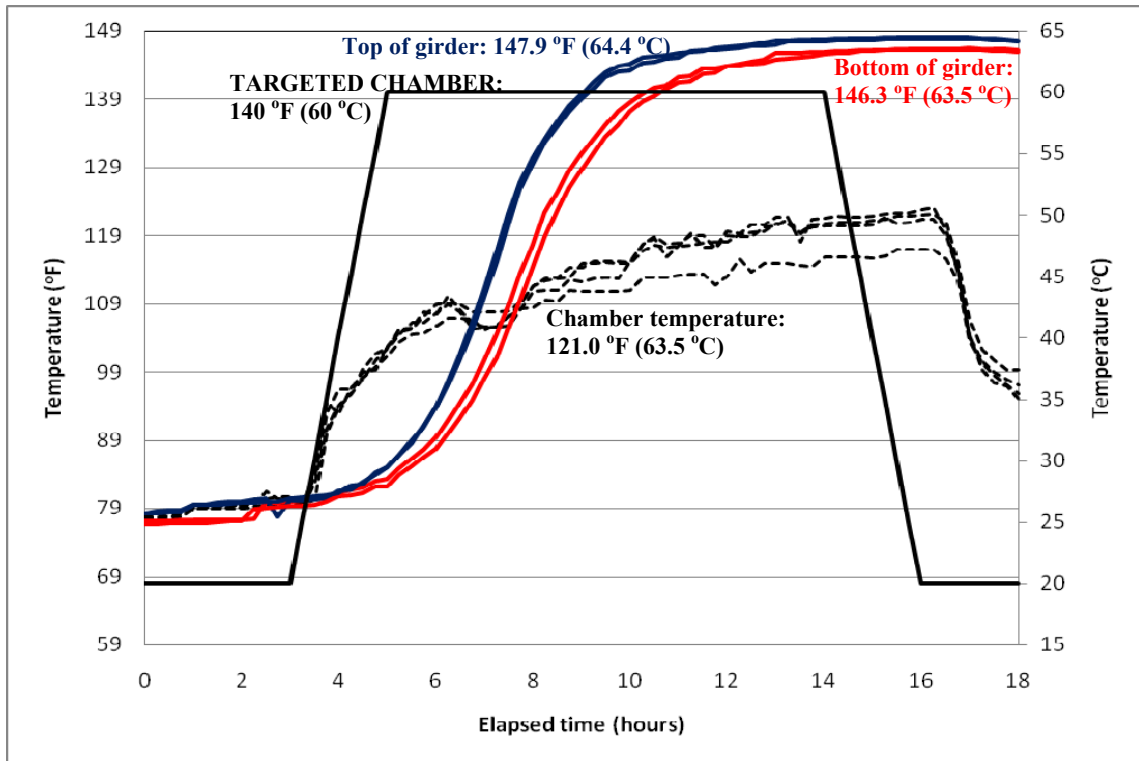


Figure 28: Temperature history of chamber and concrete during steam curing – HPC 10,000 psi (69 MPa)

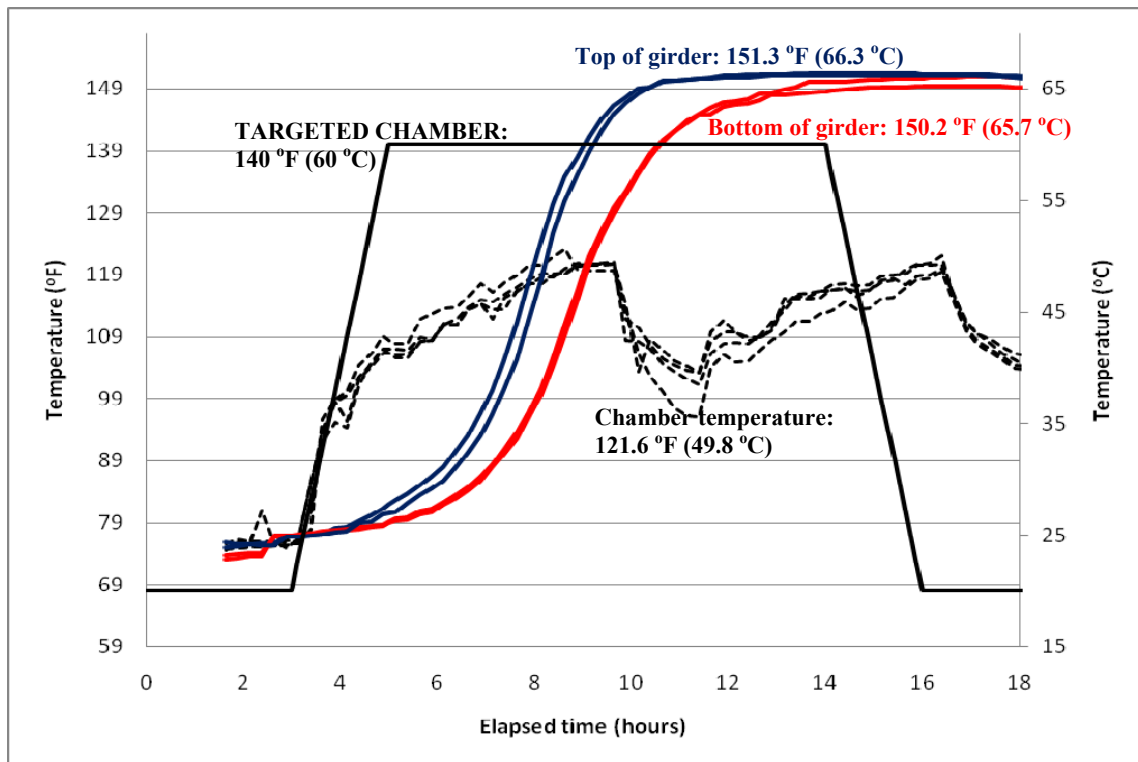


Figure 29: Temperature history of chamber and concrete during steam curing – SCC 10,000psi (69 MPa)

2.2.3 Pretensioning release

The prestressing release operation started with the release of the two hold-downs at the harping points, followed with the flame cutting of the strands at the jacking end, then on the dead end (Figure 30). The flame cutting was performed starting with the two central bottom straight strands, the two inclined strands, then working from the inner strands outwards on the remaining bottom strands.



(a) Release of bottom strand



(b) Release of inclined strand

Figure 30: Flame cutting of strands during prestress release
(Khayat and Mitchell, 2009)

2.2.3.1 Transfer length measurements

The transfer length upon release of the prestressing was estimated by measuring strains at the end of the girder. In order to measure those strains, a device was assembled consisting of a metal rod with steel disks welded to it (Figure 31). The steel disks create bond between the device and the surrounding concrete. Strain gages glued to the rod, every 4 inches (100 mm), permitted the strains to be determined at a number of locations. The devices were embedded in each end of the girders at the level of the bottom six straight strands, as shown in Figure 32.

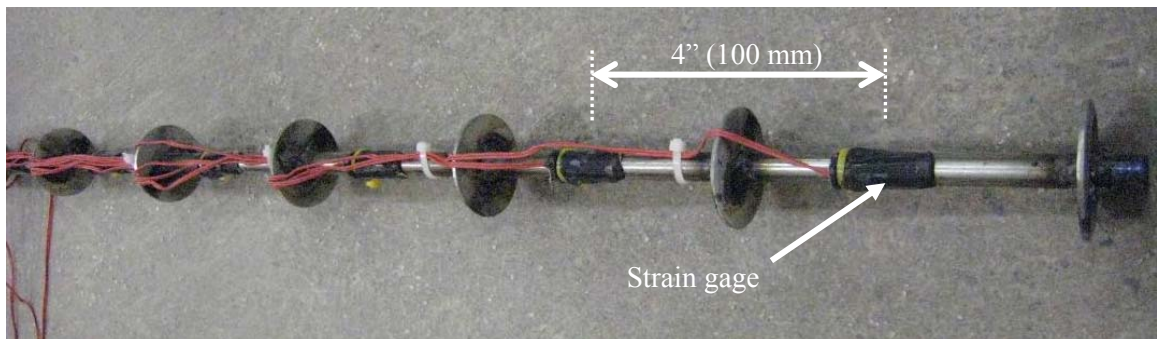
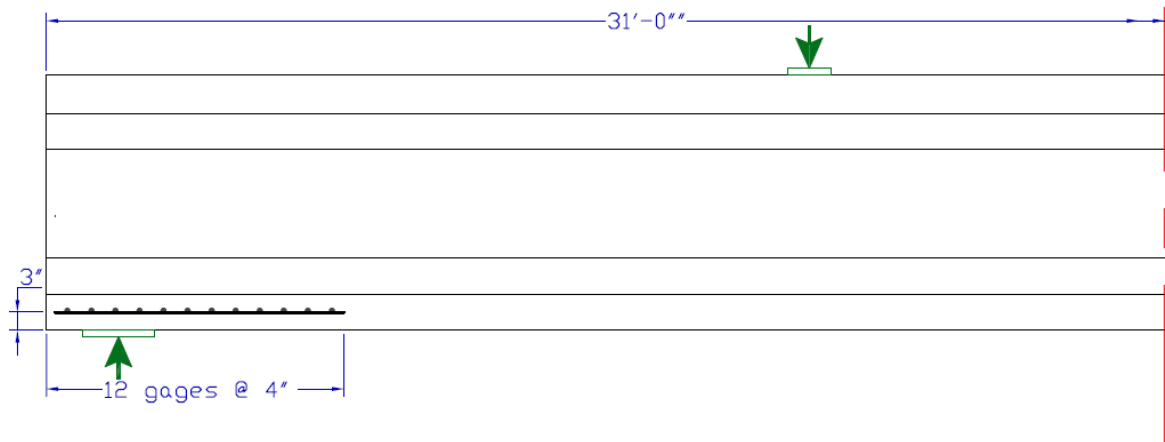


Figure 31: Transfer length measuring device



Unit conversion: $1.0' = 12'' = 304.8 \text{ mm}$

Figure 32: Locations of transfer length strain gauges

The strain readings taken by the transfer length devices upon prestress release are given in Figure 33. The procedure described by Russell and Burns (1997) was used to determine, from these readings, the transfer length. This procedure first involved computing 95% of the average strain in the strain plateau area, value known as the “95% AMS”. That value was then intersected with the measured strain profile to determine the transfer length (Khayat and Mitchell, 2009). The resulting transfer length values are shown in Figure 33 and are summarized in Table 9.

Clause 5.11.4.1 of the 2004 AASHTO Specifications estimates the transfer length to be 60 times the strand diameter equalling $60 \times 0.6 \text{ in} = 36 \text{ in}$ (914 mm). This approach is very conservative as the measured average transfer length is 12.88 inches (327 mm): a value considerably shorter than predicted.

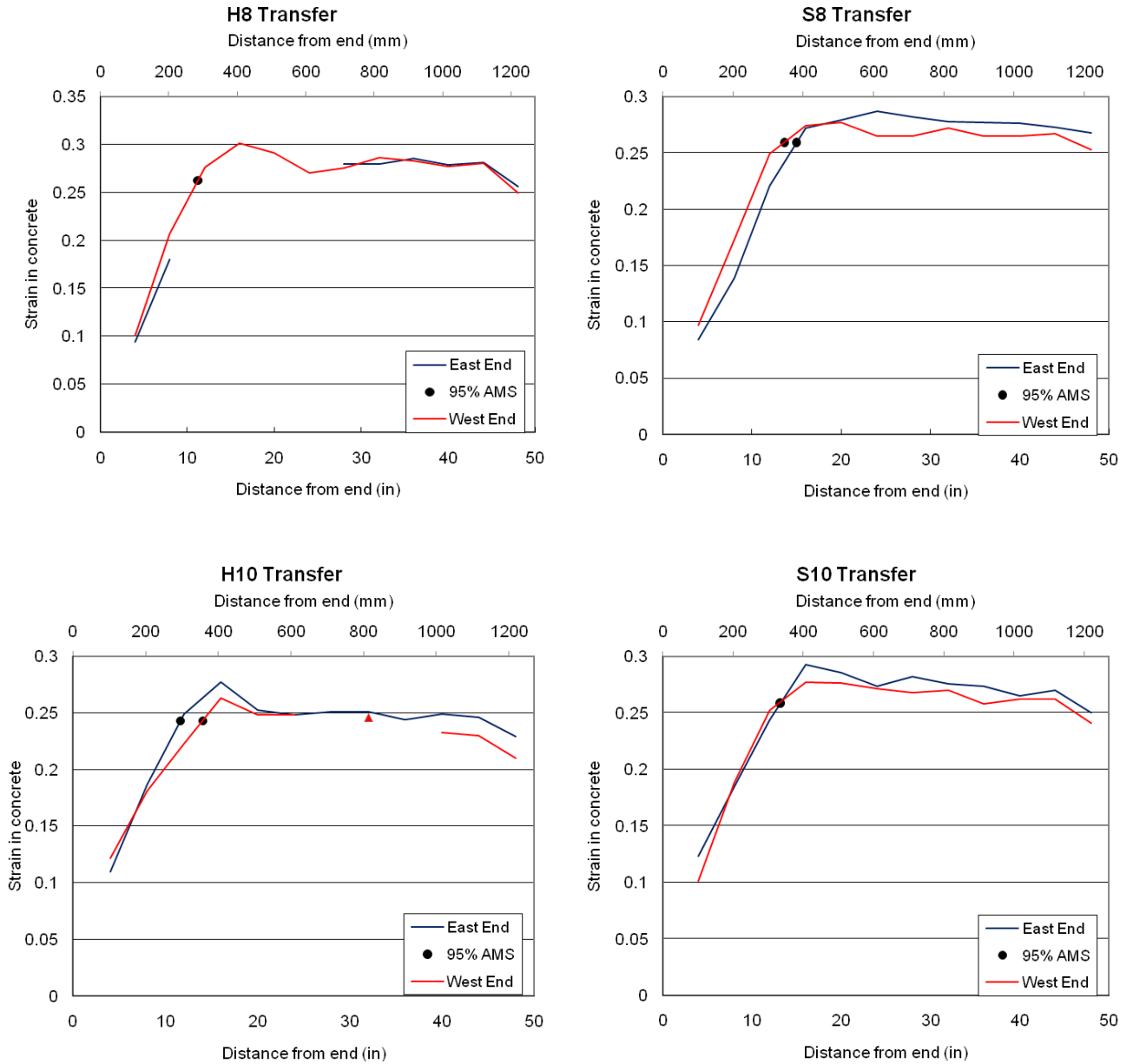


Figure 33: Measured strains used to estimate transfer length

Table 9: Summary of 95% AMS transfer lengths

Girder	Cut end <i>in (mm)</i>	Dead end <i>in (mm)</i>
H8	-	11.02 (280)
S8	15.01 (381)	13.66 (347)
H10	11.63 (295)	14.02 (356)
S10	13.21 (336)	13.10 (333)
12.88 (327)		

2.2.3.2 Strand set measurements

The strands set measurements were taken before and after prestress release using a digital caliper measuring the distance between a steel clamp and a mark on the side of the concrete (Figure 34). The difference between the values estimates the strand set for each strand at the jacking end (flame-cut release end) and at the dead end (gradual release). Table 10 gives the average values of the strand set at each end. The overall average for all four girders is 0.036 in (0.91 mm). An adjustment was made from the caliper readings to account for the strain in the strand between the concrete face and the end of the clamp.

The SCC girders were found to have slightly smaller values of strand set.

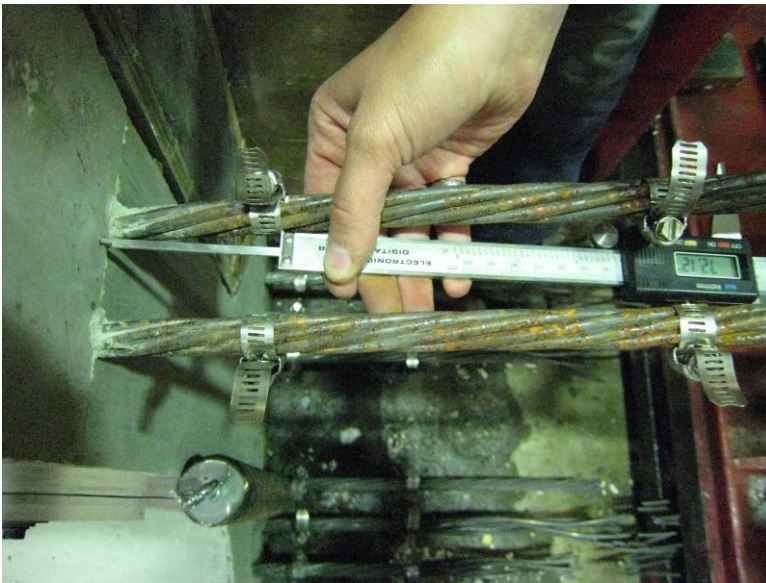


Figure 34: Measurement of strand set

Table 10: Average values of strand set

Girder	Flame-cut end Jacking end <i>in (mm)</i>	Gradual release end Dead end <i>in (mm)</i>	Average <i>in (mm)</i>
H8	0.038 (0.97)	-	0.038 (0.97)
S8	0.031 (0.79)	0.035 (0.89)	0.033 (0.84)
H10	0.033 (0.84)	0.040 (1.02)	0.036 (0.91)
S10	0.032 (0.81)	0.039 (0.99)	0.035 (0.89)
			0.036 (0.91)

If the strand stress is assumed to vary linearly over the transfer length, l_{tr} , then the theoretical strand set, Δ_{set} can be approximated as (Khayat and Mitchell, 2009):

$$\Delta_{set} = 0.5 \times \varepsilon_{pi} \times l_{tr}$$

For an average transfer length of 12.88 inches (327 mm) and a strain in the strand corresponding to a stress level of $0.7f_{pu}$, the estimated strand slip is 0.042 in (1.07). This compares reasonably well with the average measured strand set of 0.036 in (0.91 mm).

2.3 Material properties

2.3.1 Concrete material properties

2.3.1.1 Mix proportioning of HPC and SCC used for girder casting

In the attempt to get high early strength, the cement used for all four concrete mixes was of Type III. And in the attempt to get high strength concrete, the Maximum Size Aggregate (MSA) was limited to 1/2 in (12.7 mm). The HPC mixtures were proportioned with w/cm ratios of 0.38 and 0.33 to attain the two targeted 56-day compressive strengths of 8,000 and 10,000 psi (55.2 and 69 MPa), respectively. Comparably, the SCC mixtures were prepared with w/cm of 0.38 and 0.32. In order to increase the workability of concrete without increasing the w/c ratio and therefore jeopardizing the strength and permeability, HRWRA were introduced into the mixes. The proportions are summarized in Table 11.

Table 11: Mixture proportioning of SCC and HPC for girders

Mixture		HPC	SCC	HPC	SCC
56-day compressive strength level	psi (MPa)	8,000 (55.2)	8,000 (55.2)	10,000 (69)	10,000 (69)
w/cm		0.38	0.38	0.33	0.32
Cement	Type	III	III	III	III
	lb/ yd^3 (kg/m^3)	639 (379)	593 (352)	638 (379)	674 (400)
Class F fly ash	%	20	20	20	20
	lb/ yd^3 (kg/m^3)	158 (94)	148 (88)	155 (92)	169 (100)
Total CM	lb/ yd^3 (kg/m^3)	797	742	793	843

Mixture	HPC	SCC	HPC	SCC
	(473)	(440)	(470)	(500)
HRWRA demand <i>fl oz/cwt (L/100kg CM)</i>	5.7 (0.37)	12.3 (0.80)	13.1 (0.85)	21.9 (1.43)
VMA dosage <i>fl oz/cwt (L/100kg CM)</i>	0	0	0	1.54 (0.1)
Water <i>lb/yd³ (kg/m³)</i>	299 (177)	285 (169)	258 (153)	270 (160)
Sand <i>lb/yd³ (kg/m³)</i>	1233 (732)	1715 (1017)	1323 (785)	1391 (825)
Coarse aggregate <i>lb/yd³ (kg/m³)</i>	1795 (1065)	1387 (1017)	1803 (1070)	1627 (965)
MSA <i>inch (mm)</i>	0.5 (12.7)	0.5 (12.7)	0.5 (12.7)	0.5 (12.7)
Sand / Total aggregate <i>by volume</i>	0.41	0.54	0.42	0.47
Volume of coarse aggregate %	38.9	30.1	39.2	34.9
Volume of mortar %	61.1	69.9	60.8	65.1
Volume of paste %	33.8	31.9	31.4	34.6
Codification	38-797- III20%FA	38-742- III20%FA -S/A54	33-793- III20%FA	32-843- III20%FA -S/A46- VMA

2.3.1.2 Concrete's mechanical properties field testing program

For each girder, 50 – 4 × 8 inches (100 × 200 mm) cylinders and 18 - 3.9 × 3.9 × 15.7 inches (100 × 100 × 400 mm) flexural beams were prepared of which 28 cylinders and nine flexural beams were match-cured with the concrete girders. They were steam-cured for 18 hours, according to the procedure described in Section 2.2.2, then air-cured with the same conditions as their companion girder. The rest of the cylinders and flexural beam specimens were demoulded after 18 hours of air curing, then moist-cured until testing in a chamber at 100% relative humidity (RH) and 73.4°F (23 °C).

At the time of prestress release, three steam-cured and three air-cured cylinders were tested to determine the compressive strength (Table 12). Four more cylinders, two for each curing method, were also tested to determine the modulus of elasticity (Table 13). The same tests were effectuated at 7, 28, and 56 days, as well as at the age corresponding to the time of testing the girders.

Similarly, four flexural beam specimens, two for each curing method, provided data on the modulus of rupture at the time of prestressing release, at 28 days and at 56 days (Table 14).

Table 12: Concrete Compressive Strength of SCC and HPC mixes used for girders

Age	Curing		H8 psi (MPa)	S8 psi (MPa)	H10 psi (MPa)	S10 psi (MPa)
At release (18 hours)	Steam-cured for 18 hours + Air-cured with the same conditions as the girder	1	4,945 (34.1)	5,235 (36.1)	5,725 (39.5)	6,855 (47.3)
		2	4,990 (34.4)	5,270 (36.3)	6,005 (41.4)	6,970 (48.1)
		3	5,030 (34.7)	5,300 (36.5)	5,845 (40.3)	6,950 (47.9)
		mean	4,988 (34.4)	5,268 (36.3)	5,858 (40.4)	6,925 (47.7)
		COV	0.85%	0.62%	2.40%	0.89%
	Air-cured for 18 hours + Moist-cured with 100% RH	1	5,160 (35.6)	5,085 (35.1)	5,775 (39.8)	6,830 (47.1)
		2	4,700 (32.4)	4,920 (33.9)	5,705 (39.3)	6,910 (47.6)
		3	4,975 (34.3)	5,115 (35.3)	5,830 (40.2)	6,855 (47.3)
		mean	4,945 (34.1)	5,040 (34.7)	5,770 (39.8)	6,865 (47.3)
		COV	4.68%	2.08%	1.09%	0.60%
7 days	Steam-cured for 18 hours + Air-cured with the same conditions as the girder	1	6,355 (43.8)	7,095 (48.9)	7,690 (53.0)	8,600 (59.3)
		2	6,220 (42.9)	7,200 (49.6)	7,580 (52.3)	8,710 (60.1)
		3	6,180 (42.6)	7,265 (50.1)	7,775 (53.6)	8,440 (58.2)
		mean	6,252 (43.1)	7,187 (49.6)	7,682 (53.0)	8,583 (59.2)
		COV	1.47%	1.19%	1.27%	1.58%
	Air-cured for 18 hours + Moist-cured with 100% RH	1	6,295 (43.4)	7,130 (49.2)	6,980 (48.1)	8,045 (55.5)
		2	6,185 (42.6)	7,120 (49.1)	6,955 (48.0)	7,995 (55.1)
		3	6,325 (43.6)	6,990 (48.2)	7,145 (49.3)	7,780 (53.6)
		mean	6,268 (43.2)	7,080 (48.8)	7,027 (48.4)	7,940 (54.7)
		COV	1.18%	1.10%	1.47%	1.77%
28 days	Steam-cured for 18 hours + Air-cured with the same conditions as the girder	1	7,125 (49.1)	7,980 (55.0)	8,175 (56.4)	10,210 (70.4)
		2	7,200 (49.6)	7,585 (52.3)	8,305 (57.3)	9,795 (67.5)
		3	7,130 (49.2)	7,900 (54.5)	8,600 (59.3)	10,190 (70.3)
		mean	7,152 (49.3)	7,822 (53.9)	8,360 (57.6)	10,065 (69.4)
		COV	0.59%	2.67%	2.60%	2.33%
	Air-cured for 18 hours + Moist-cured with 100% RH	1	7,990 (55.1)	8,450 (58.3)	8,235 (56.8)	9,045 (62.4)
		2	7,620 (52.5)	8,295 (57.2)	8,760 (60.4)	8,630 (59.5)
		3	7,855 (54.2)	8,600 (59.3)	8,330 (57.4)	8,805 (60.7)
		mean	7,822 (53.9)	8,448 (58.2)	8,442 (58.2)	8,827 (60.9)
		COV	2.39%	1.81%	3.31%	2.36%
56 days	Steam-cured for 18 hours + Air-cured with the same conditions as the girder	1	7,760 (53.5)	8,630 (59.5)	8,875 (61.2)	9,500 (65.5)
		2	7,225 (49.8)	8,715 (60.1)	9,325 (64.3)	9,650 (66.5)
		3	7,150 (49.3)	8,470 (58.4)	8,950 (61.7)	9,515 (65.6)
		mean	7,378 (50.9)	8,605 (59.3)	9,050 (62.4)	9,555 (65.9)
		COV	4.51%	1.45%	2.66%	0.86%
	Air-cured for 18 hours + Moist-cured with 100% RH	1	8,370 (57.7)	9,660 (66.6)	9,355 (64.5)	11,100 (76.5)
		2	8,410 (58.0)	9,805 (67.6)	9,180 (63.3)	11,260 (77.6)
		3	8,105 (55.9)	9,730 (67.1)	9,500 (65.5)	11,700 (80.7)
		mean	8,295 (57.2)	9,732 (67.1)	9,345 (64.4)	11,353 (78.3)
		COV	2.00%	0.75%	1.71%	2.74%
Day of the test	Steam-cured for 18 hours +	1	7,225 (49.8)	8,105 (55.9)	9,045 (62.4)	10,235 (70.6)
		2	6,920 (47.7)	8,095 (55.8)	9,015 (62.2)	9,835 (67.8)

Age	Curing		H8 psi (MPa)	S8 psi (MPa)	H10 psi (MPa)	S10 psi (MPa)
	Air-cured with the same conditions as the girder	3		7,770 (53.6)	8,710 (60.1)	9,810 (67.6)
		mean	7,073 (48.8)	7,990 (55.1)	8,923 (61.5)	9,960 (68.7)
		COV	3.05%	2.39%	2.08%	2.39%
	Air-cured for 18 hours + Moist-cured with 100% RH	1	8,610 (59.4)	10,885 (75.0)	10,610 (73.2)	12,265 (84.6)
		2	9,220 (63.6)	10,745 (74.1)	10,875 (75.0)	11,920 (82.2)
		3	9,295 (64.1)	10,775 (74.3)	10,600 (73.1)	12,195 (84.1)
		mean	9,042 (62.3)	10,802 (74.5)	10,695 (73.7)	12,127 (83.6)
		COV	4.16%	0.68%	1.46%	1.50%

The target value for the release compressive strengths, at 18-hours, for both 8,000 psi (55.2 MPa) concrete batches was 5,000 psi (34.5 MPa), while that of both 10,000 psi (69 MPa) batches was 6,250 psi (43 MPa). Based on the cylinders tests, the SCC 8,000 psi and 10,000 psi (55.2 and 69 MPa) concretes reached strengths of 5,268 (36.3 MPa) and 6,925 psi (47.7 MPa), respectively, after 18 hours of steam-curing, exceeding the target values. The HPC mixtures, on the other hand, showed values that are close but do not quite reach the target compressive strength. The cylinders tests indicated compressive strength of 4,988 and 5,858 psi (34.4 and 40.4 MPa), for the 8,000 and 10,000 psi (55.2 and 69 MPa) mixes, respectively.

The temperature, and therefore maturity, of the concrete in the girder was greater than that of the control cylinders translating into higher in-situ compressive strengths than determined.

Table 13: Elastic Modulus of SCC and HPC mixes used for girders

Age	Curing		H8 psi (MPa)	S8 psi (MPa)	H10 psi (MPa)	S10 psi (MPa)
At release (18 hours)	Steam-cured for 18 hours + Air-cured with the same conditions as the girder	1	5,280 (36.4)	5,040 (34.7)	5,485 (37.8)	5,335 (36.8)
		2	4,875 (33.6)	4,970 (34.3)	5,605 (38.6)	5,365 (37.0)
		mean	5,078 (35.0)	5,005 (34.5)	5,545 (38.2)	5,350 (36.9)
		COV	5.64%	0.99%	1.53%	0.40%
	Air-cured for 18 hours + Moist-cured with 100% RH	1	4,975 (34.3)	4,330 (29.9)	5,265 (36.3)	5,345 (36.9)
		2	4,530 (31.2)	4,905 (33.8)	5,580 (38.5)	5,075 (35.0)
		mean	4,753 (32.8)	4,618 (31.8)	5,423 (37.4)	5,210 (35.9)
		COV	6.62%	8.81%	4.11%	3.66%
7 days	Steam-cured for 18 hours + Air-cured with the same conditions as the girder	1	4,900 (33.8)	4,700 (32.4)	6,070 (41.9)	5,245 (36.2)
		2	5,090 (35.1)	4,900 (33.8)	5,455 (37.6)	5,120 (35.3)
		mean	4,995 (34.4)	4,800 (33.1)	5,763 (39.7)	5,183 (35.7)
		COV	2.69%	2.95%	7.55%	1.71%
	Air-cured for 18 hours + Moist-cured with 100%	1	4,760 (32.8)	5,170 (35.6)	5,235 (36.1)	5,510 (38.0)
		2	4,975 (34.3)	5,150 (35.5)	5,490 (37.9)	5,720 (39.4)
		mean	4,868 (33.6)	5,160 (35.6)	5,363 (37.0)	5,615 (38.7)

Age	Curing		H8 psi (MPa)	S8 psi (MPa)	H10 psi (MPa)	S10 psi (MPa)
	RH	COV	3.12%	0.27%	3.36%	2.64%
28 days	Steam-cured for 18 hours + Air-cured with the same conditions as the girder	1	5,425 (37.4)	5,795 (40.0)	5,890 (40.6)	6,250 (43.1)
		2	5,520 (38.1)	5,670 (39.1)	6,270 (43.2)	5,955 (41.1)
		mean	5,473 (37.7)	5,733 (39.5)	6,080 (41.9)	6,103 (42.1)
		COV	1.23%	1.54%	4.42%	3.42%
	Air-cured for 18 hours + Moist-cured with 100% RH	1	6,115 (42.2)	5,800 (40.0)	6,480 (44.7)	6,565 (45.3)
		2	6,015 (41.5)	6,020 (41.5)	6,480 (44.7)	6,805 (46.9)
		mean	6,065 (41.8)	5,910 (40.7)	6,480 (44.7)	6,685 (46.1)
		COV	1.17%	2.63%	0.00%	2.54%
56 days	Steam-cured for 18 hours + Air-cured with the same conditions as the girder	1	5,365 (37.0)	5,800 (40.0)	5,945 (41.0)	6,090 (42.0)
		2	5,510 (38.0)	5,655 (39.0)	6,235 (43.0)	6,090 (42.0)
		mean	5,438 (37.5)	5,728 (39.5)	6,090 (42.0)	6,090 (42.0)
		COV	1.89%	1.79%	3.37%	0.00%
	Air-cured for 18 hours + Moist-cured with 100% RH	1	6,235 (43.0)	6,235 (43.0)	6,525 (45.0)	6,670 (46.0)
		2	6,235 (43.0)	6,280 (43.3)	6,525 (45.0)	6,670 (46.0)
		mean	6,235 (43.0)	6,258 (43.1)	6,525 (45.0)	6,670 (46.0)
		COV	0.00%	0.51%	0.00%	0.00%
Day of the test	Steam-cured for 18 hours + Air-cured with the same conditions as the girder	1	-	4,715 (32.5)	5,905 (40.7)	5,580 (38.5)
		2	-	5,145 (35.5)	5,805 (40.0)	6,030 (41.6)
		mean	-	4,930 (34.0)	5,855 (40.4)	5,805 (40.0)
		COV	-	6.17%	1.21%	5.48%
	Air-cured for 18 hours + Moist-cured with 100% RH	1	5,285 (36.4)	6,340 (43.7)	6,600 (45.5)	6,645 (45.8)
		2	5,915 (40.8)	6,235 (43.0)	6,470 (44.6)	6,830 (47.1)
		mean	5,600 (38.6)	6,288 (43.4)	6,535 (45.1)	6,738 (46.5)
		COV	7.95%	1.18%	1.41%	1.94%

Table 14: Flexural Strength of SCC and HPC mixes used for girders

Age	Curing		H8 psi (MPa)	S8 psi (MPa)	H10 psi (MPa)	S10 psi (MPa)
At release (18 hours)	Steam-cured for 18 hours + Air-cured with the same conditions as the girder	1	685 (4.7)	660 (4.6)	745 (5.1)	815 (5.6)
		2	665 (4.6)	730 (5.0)	640 (4.4)	770 (5.3)
		3	660 (4.6)	720 (5.0)	730 (5.0)	825 (5.7)
		mean	670 (4.6)	703 (4.8)	705 (4.9)	803 (5.5)
		COV	1.97%	5.38%	8.06%	3.65%
	Air-cured for 18 hours + Moist-cured with 100% RH	1	585 (4.0)	680 (4.7)	685 (4.7)	730 (5.0)
		2	590 (4.1)	635 (4.4)	745 (5.1)	775 (5.3)
		3	590 (4.1)	620 (4.3)	685 (4.7)	755 (5.2)
		mean	588 (4.1)	645 (4.4)	705 (4.9)	753 (5.2)
		COV	0.49%	4.84%	4.91%	2.99%
28 days	Steam-cured for 18 hours + Air-cured with the	1	815 (5.6)	795 (5.5)	740 (5.1)	815 (5.6)
		2	740 (5.1)	795 (5.5)	950 (6.6)	865 (6.0)
		3	970 (6.7)	790 (5.4)	820 (5.7)	765 (5.3)

Age	Curing		H8 psi (MPa)	S8 psi (MPa)	H10 psi (MPa)	S10 psi (MPa)
	same conditions as the girder	mean	842 (5.8)	793 (5.5)	837 (5.8)	815 (5.6)
		COV	13.94%	0.36%	12.67%	6.13%
	Air-cured for 18 hours + Moist-cured with 100% RH	1	1,055 (7.3)	1,140 (7.9)	1,255 (8.7)	1,450 (10.0)
		2	1,155 (8.0)	1,100 (7.6)	1,235 (8.5)	1,430 (9.9)
		3	1,115 (7.7)	1,115 (7.7)	1,335 (9.2)	1,405 (9.7)
		mean	1,108 (7.6)	1,118 (7.7)	1,275 (8.8)	1,428 (9.8)
		COV	4.54%	1.81%	4.15%	1.58%
56 days	Steam-cured for 18 hours + Air-cured with the same conditions as the girder	1	975 (6.7)	880 (6.1)	860 (5.9)	860 (5.9)
		2	980 (6.8)	900 (6.2)	860 (5.9)	860 (5.9)
		3	925 (6.4)	985 (6.8)	830 (5.7)	845 (5.8)
		mean	960 (6.6)	922 (6.4)	850 (5.9)	855 (5.9)
		COV	3.17%	6.05%	2.04%	1.01%
	Air-cured for 18 hours + Moist-cured with 100% RH	1	1,100 (7.6)	1,220 (8.4)	1,260 (8.7)	1,470 (10.1)
		2	1,115 (7.7)	1,250 (8.6)	1,245 (8.6)	1,555 (10.7)
		3	1,115 (7.7)	1,260 (8.7)	1,300 (9.0)	1,530 (10.5)
		mean	1,110 (7.7)	1,243 (8.6)	1,268 (8.7)	1,518 (10.5)
		COV	0.78%	1.67%	2.24%	2.88%

2.3.1.3 Fresh properties of HPC and SCC used for girder casting

Besides determining the mechanical properties of the concrete by testing cylinders and flexural beams, a field testing program was established to determine other characteristics of the concrete such as workability and stability.

The program for the field testing of the concrete in the girders, along with the results, is presented in Table 15.

Table 15: Fresh properties of SCC and HPC mixes used for girders

Concrete behavior	Mixture, psi (MPa)		HPC 8,000 (55.2)	SCC 8,000 (55.2)	HPC 10,000 (69)	SCC 10,000 (69)	Comments
	Temperature, °F (°C)	at delivery	66.4 (19.1)	69.8 (21.0)	76.1 (24.5)	75.6 (24.2)	
		after casting	66.7 (19.3)	70.7 (21.5)	76.6 (24.8)	76.1 (24.5)	
Filling ability	Slump flow, in. (mm)	at delivery	-	26.0 (660)	-	26.0 (660)	Refer to section 1.5.2.1
		after casting	-	23.6 (600)	-	25.2 (640)	

Concrete behavior	Mixture, psi (MPa)		HPC 8,000 (55.2)	SCC 8,000 (55.2)	HPC 10,000 (69)	SCC 10,000 (69)	Comments	
	T-20, sec	at delivery	-	3.0	-	3.0		
		after casting	-	3.9	-	3.7		
	Slump, in (mm)	at delivery	5.5 (140)	-	7.5 (190)	-		
after casting		4.3 (110)	-	7.1 (180)	-			
Passing ability	J-Ring flow, in (mm)		at delivery	-	23.6 (600)	-	22.8 (580)	Refer to section 1.5.2.2
			after casting	-	21.7 (550)	-	21.3 (540)	ASTM C 1621
	L-box	sec	at delivery	-	3.9	-	4.9	Refer to section 1.5.2.3
			after delivery	-	4.5	-	5.5	
		H ₂ /H ₁	at delivery	-	0.73	-	0.70	
			after delivery	-	0.68	-	0.62	
Filling capacity	Filling capacity, %		at delivery	-	82	-	76	
			after casting	-	75	-	70	
Stability	Visual stability index		at delivery	-	0.5	-	0.5	Refer to section 1.5.2.1
			after casting	-	0.5	-	0.5	ASTM C 1611
	Column segregation index, %		1.58	4.00	-	2.65	Refer to section 1.5.2.4 ASTM C 1610	
	Max. surface settlement, % (test performed over 24 hours)		0.22	0.29	0.21	0.24	Refer to section 1.5.2.5	
	Air content, %	at delivery	2.3	2.0	1.9	1.2	AASHTO T 152	
		after casting	2.1	1.9	1.9	1.5		
Rheology: Modified Tattersall MK III rheometer	Yield stress	τ ° (Pa)	893	3	568	118	Refer to section 1.5.2.6	
	Plastic viscosity	μ _p (Pa.s)	52	253	233	189		
		R ²	0.99	0.99	0.97	0.99		

2.3.1.4 Semi-adiabatic temperature measurements

Variations of the concrete temperature under semi-adiabatic conditions are presented in Figure 35 and summarized in Table 16.

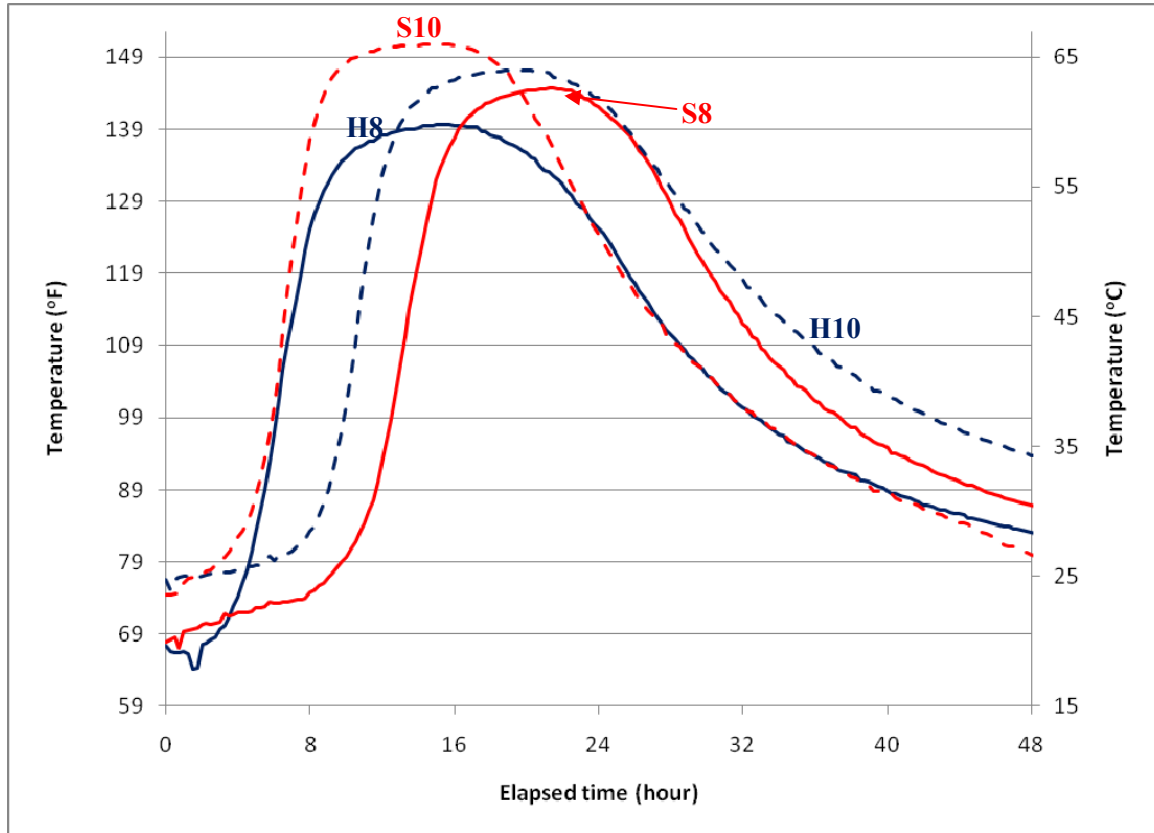


Figure 35: Temperature rise of concrete under semi-adiabatic conditions

Table 16: Concrete temperature under semi-adiabatic conditions

		H8	S8	H10	S10
Peak temperature	$^{\circ}F (^{\circ}C)$	139.6 (60)	144.6 (62.5)	147.1 (64)	150.7 (66)
Elapsed time	hours	15.5	16.8	15.0	16.9

It can be noted that the two 10,000 psi (69 MPa) concrete mixtures, H10 and S10, developed higher peak temperatures than both 8,000 psi (55.2 MPa) concrete mixtures, H8 and S8. They however took longer times to reach those peaks. Moreover, for a given compressive strength, the SCC mixtures reached temperatures similar but higher than their companion HPC mixtures. Consequently, the SCC mixtures had longer elapsed times to reach peak temperatures compared to their companion HPC mixtures. This can be due to the higher HRWRA dosage.

2.3.1.5 Mechanical properties of deck slab concrete

All four deck slabs were to have the same concrete properties. They were to simulate a cast-in-place deck slab with conventional air-entrained concrete of regular compressive strength of 5,000 psi (34.5 MPa), with Type I cement.

Table 17 summarizes the concrete proportions used in the production of the ready-mix concrete delivered to the structural laboratory of McGill University from Unibéton's plant, while

Table 18 presents the fresh properties of each batch of concrete, as two were required.

Table 17: Mixture proportioning and fresh properties of deck slab concrete for all four girders

Mixture	Deck slab
Compressive strength <i>psi (MPa)</i>	5,000 (34.5)
<i>w/cm</i>	0.42
Cement <i>Type</i>	I
<i>lb/yd³ (kg/m³)</i>	639 (380)
Water <i>lb/yd³ (kg/m³)</i>	269 (160)
Sand <i>lb/yd³ (kg/m³)</i>	1189 (707)
Coarse aggregate <i>lb/yd³ (kg/m³)</i>	1822 (1083)
Retarder <i>oz/yd³ (ml/m³)</i>	17.7 (684)
Air entraining agent <i>oz/yd³ (ml/m³)</i>	8.8 (342)

Table 18: Fresh properties of the deck slab concrete

Deck Slab	H8 and S8	H10 and S10
Initial concrete temperature <i>°F (°C)</i>	77.9 (25.5)	80.6 (27)
Slump <i>in (mm)</i>	3.74 (95)	3.74 (95)
Air content %	6.1	7.6
Average compressive strength at 28 days <i>psi (MPa)</i>	5030 (34.7)	4690 (32.3)
Elastic modulus at 28 days <i>psi (MPa)</i>	4590 (31.6)	4280 (29.5)
Average compressive strength at 38 days <i>psi (MPa)</i>	5250 (36.2)	5090 (35.1)

2.3.2 Reinforcing steel and prestressing steel properties

2.3.2.1 Reinforcing steel

The girders contained two different sizes of reinforcing bars: No. 3, for the stirrups and interface shear reinforcement and No. 5, for the longitudinal bars. Figure 36 shows the typical stress-strain

relationships for each one of these non-prestressed reinforcing bars. Their mechanical properties, such as the average values of the yield stress, f_y , the ultimate stress, f_u , the strain at strain hardening, ϵ_{sh} and the ultimate strain, ϵ_u , are summarized in Table 19.

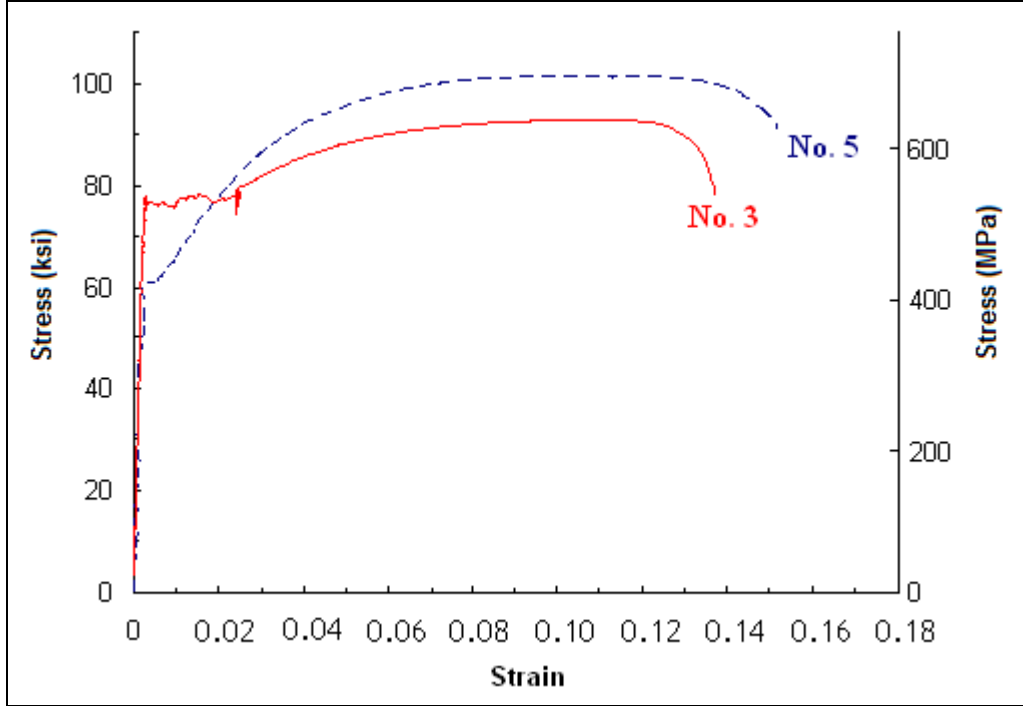


Figure 36: Typical stress-strain relationships for reinforcing No. 3 and No. 5 bars (Khayat and Mitchell, 2009)

Table 19: Average mechanical properties of reinforcing bars

	A_s in^2 (mm^2)	E_s ksi (GPa)	f_y ksi (MPa)	ϵ_y	f_u ksi (GPa)	ϵ_{sh}	ϵ_u
No. 3	0.11 (71)	29,000 (200)	76.3 (526)	0.00263	92.5 (638)	0.0240	0.127
No. 5	0.31 (200)	29,000 (200)	60.9 (42)	0.00210	101.1 (697)	0.0057	0.152

2.3.2.2 Prestressing steel

Each of the four girders contained eight Grade 270 seven-wire low-relaxation prestressing strands of 0.6 in (15.2 mm) diameter. Figure 37 shows the typical stress-strain relationship of such strands and Table 20 summarizes their mechanical properties.

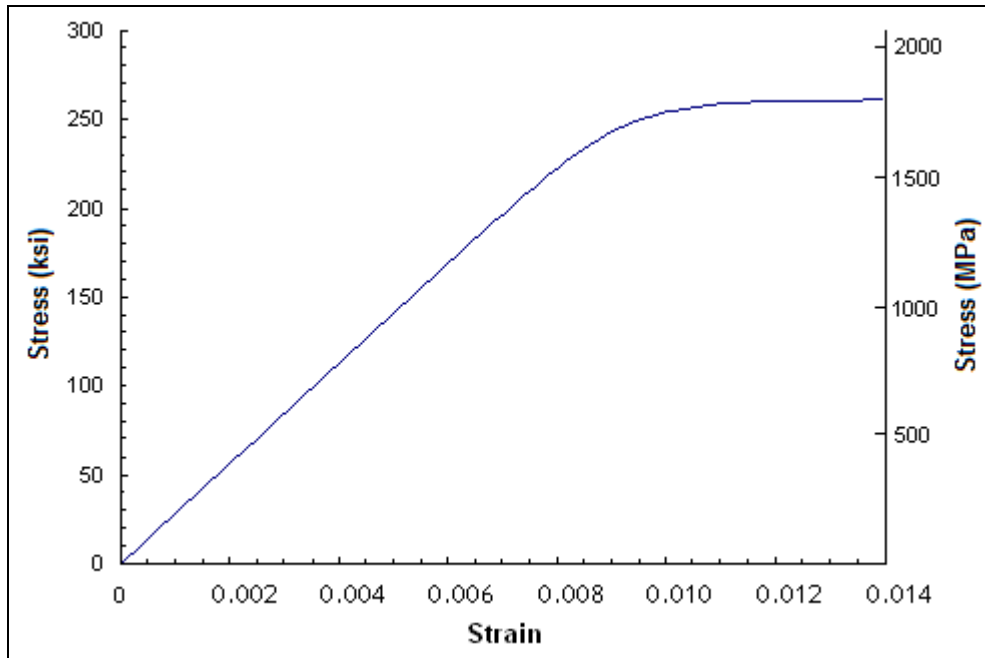


Figure 37: Typical stress-strain relationship for 0.6 in (15.2 mm) diameter strand
(Khayat and Mitchell, 2009)

Table 20: Typical mechanical properties of prestressing strand

	A_{ps} in^2 (mm^2)	E_{ps} ksi (GPa)	0.2% offset stress ksi (GPa)	Stress at 1% strain ksi (GPa)	f_{pu} ksi (GPa)	ϵ_{pu}
Seven-wire strand of 0.6 in (15.2 mm) diameter	0.217 (140)	28,100 (194)	259 (1.78)	254 (1.75)	278.1 (1.92)	0.072

2.4 Test procedure

The testing of the composite precast pretensioned girder and deck slab was conducted at least 28 days after the deck slab was cast on the girder.

Prior to testing, the specimen was positioned, as shown in Figure 38, on neoprene bearing pads at its ends, and was instrumented with linear voltage differential transducers (LVDTs) to measure displacements and to determine average strains. For each girder, two LVDTs monitored the compression of the neoprene pads, two others measured the deflections under the loading points, and one measured the deflection at mid-span. Moreover, 12 LVDTs, six on each end of the girder,

were placed in a rosette shape to record elongations, over a specific length, of the region prone to shear failure. The LVDTs were attached to the girders by threaded rods epoxied into holes drilled in the concrete on the back face of the specimen. During the testing, the LVDT and strain gage readings were taken every 0.5 second.

As shown in Figure 39, the loading was done using a structural steel loading beam which provided two equal line loads 115" (2.9 m) from the centerline of the supports. That steel beam was loaded using a 2,580 kip (11,414 kN) capacity computer-controlled MTS testing machine. The loading for all four specimens followed the same procedure. The total load was first applied to the structural loading beam in "load control" at a rate of 11 kips/min (50 kN/min). After the development of the first flexural cracking, the loading was altered to "deflection control" at a rate of 0.06 in/min (1.5 mm/min) until failure. The loading was stopped at key load stages to allow detailed measurements of the crack widths and to take photographs.

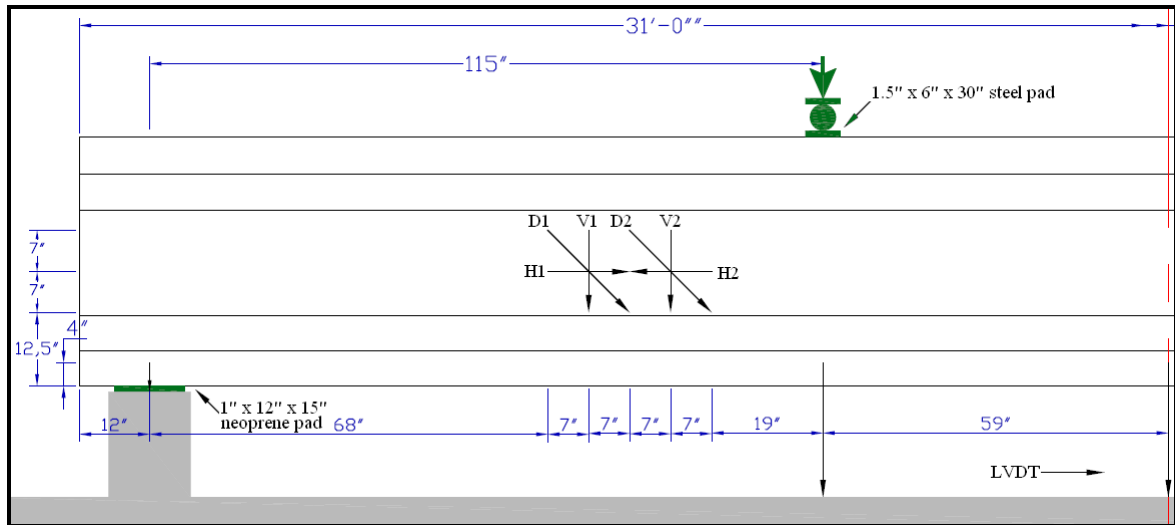


Figure 38: Test setup and locations of LVDTs



Figure 39: Specimen before testing

Chapter 3: Experimental Results

3.1 Flexural Behaviour

3.1.1 Camber measurements

Figure 40 shows the variation of the camber at mid-span with time. The camber was measured using a piano wire attached to both ends of the specimen subjected to constant tension. Readings were taken at mid-span by sighting against a mirrored scale to minimize parallax. Prior to the prestress release, which took place at an age of about 18 hours after casting, the camber was at zero.

At least 28 days after the prestressing release, the deck slab was cast on top of each girder. The sudden reduction in camber that occurred soon after is due to the removal of the formwork for the deck slab.

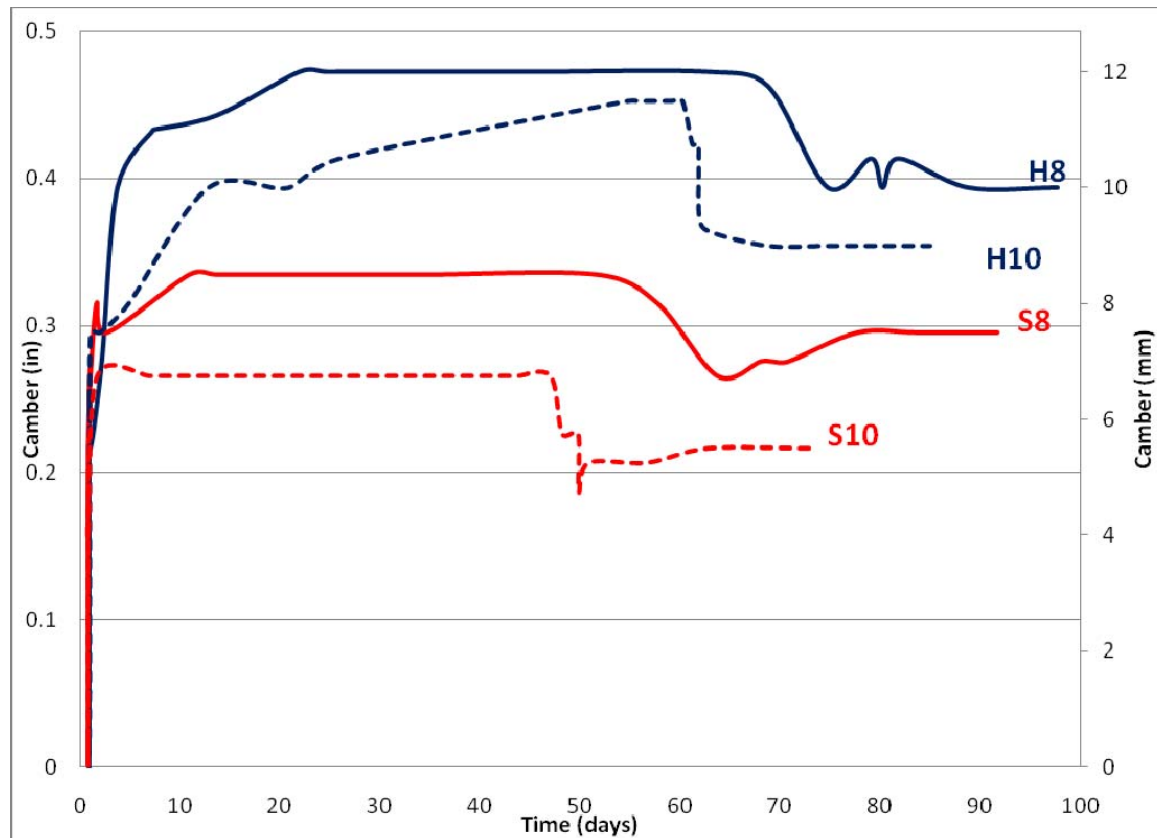


Figure 40: Variation of camber with time

The specimens with target compressive strengths of 8,000 psi (55.2 MPa) had larger cambers than their companion specimens made with 10,000 psi (69 MPa) concrete. Moreover, both specimens made of HPC (H8 and H10) experienced larger cambers than specimens made of SCC (S8 and S10).

3.1.2 Overall response in flexure

Figure 41 to Figure 44 show the moment versus central deflection responses of specimens H8, S8, H10 and S10, respectively. Table 21 displays the important results such as the moment at first flexural cracking, M_{cr} , the maximum moment achieved, M_{max} , and the maximum deflection reached before failure, Δ_{max} . Note that all the moments include the self weight of the girder.

The first flexural crack observed in each of the specimens was hairline in width. Prior to failure, flexural cracks reached widths up to 0.012 inch (0.3 mm). They extended into the top flange. Some hairline cracks were also seen on the bottom of the deck slab.



Figure 41: Moment versus central deflection – Specimen H8

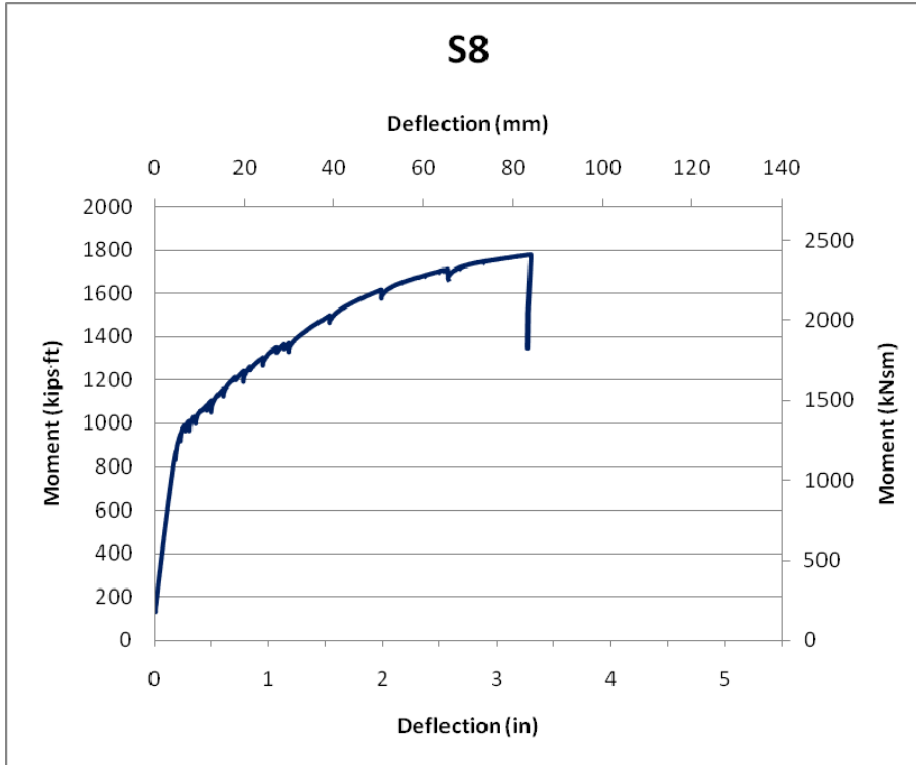


Figure 42: Moment versus central deflection – Specimen S8

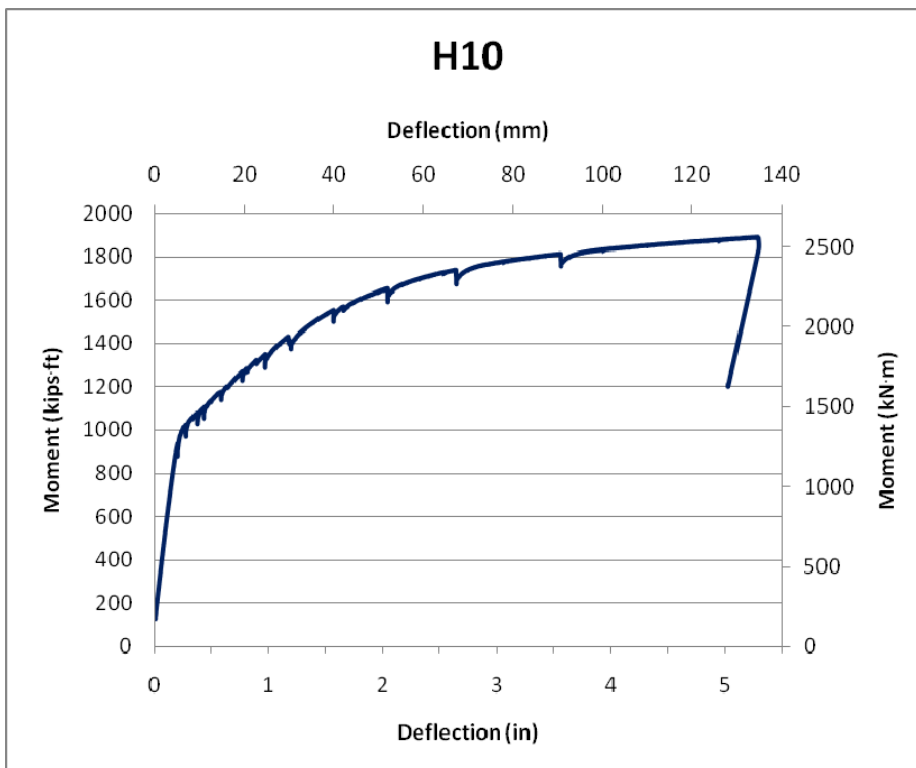


Figure 43: Moment versus central deflection – Specimen H10

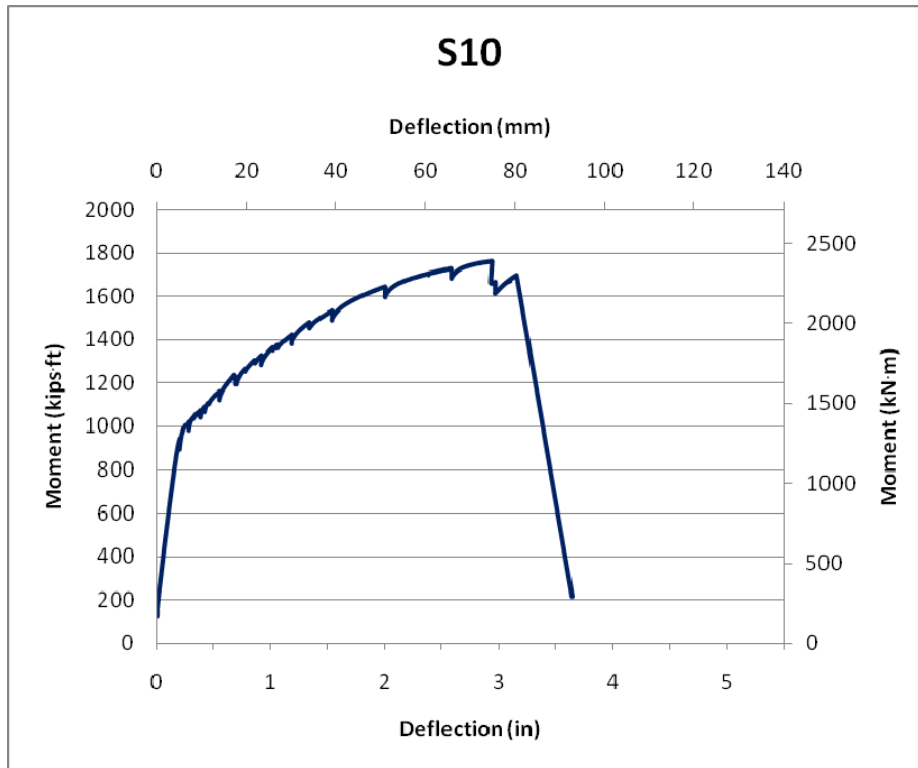


Figure 44: Moment versus central deflection – Specimen S10

Table 21: Flexural responses of the specimens

	H8	S8	H10	S10
M_{cr} <i>kips · ft (kN · m)</i>	902 (1223)	870 (1180)	939 (1273)	944 (1280)
M_{max} <i>kips · ft (kN · m)</i>	1816 (2462)	1781 (2415)	1889 (2561)	1762 (2390)
Δ_{max} <i>inches (mm)</i>	4.43 (113)	3.30 (84)	5.29 (134)	3.15 (80)

Figure 45 shows the moment versus the strain responses for each of the specimens. Those strains were obtained from the two vibrating wire gages, one at the centre of the span and the other 4 feet (1.22 m) from mid-span close to one of the loading points. The high strains that were recorded indicate that the flexural reinforcement had yielded and had strains beyond strain hardening.

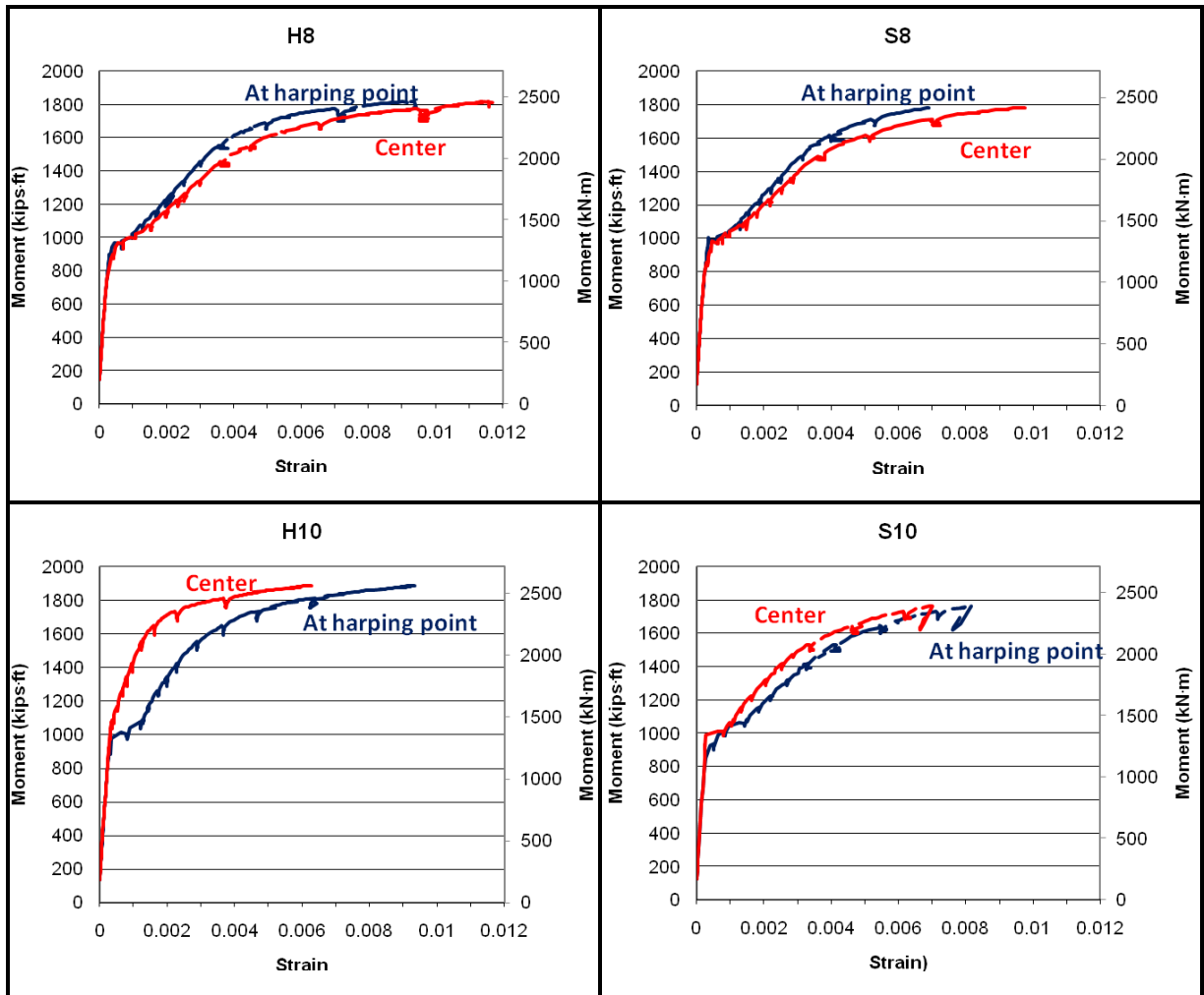


Figure 45: Moment versus longitudinal strain response at the level of the straight strands

3.2 Shear Behaviour

Figure 46 to Figure 49 show the shear versus deflection response for the side of each specimen that experienced shear failure. The shear was determined at the inner face of the neoprene bearing pads, 18 inches (457 mm) from the side. The deflection plotted is at the location of the loading point.



Figure 46: Shear versus deflection at load point – Specimen H8



Figure 47: Shear versus deflection at load point – Specimen S8



Figure 48: Shear versus deflection at load point – Specimen H10

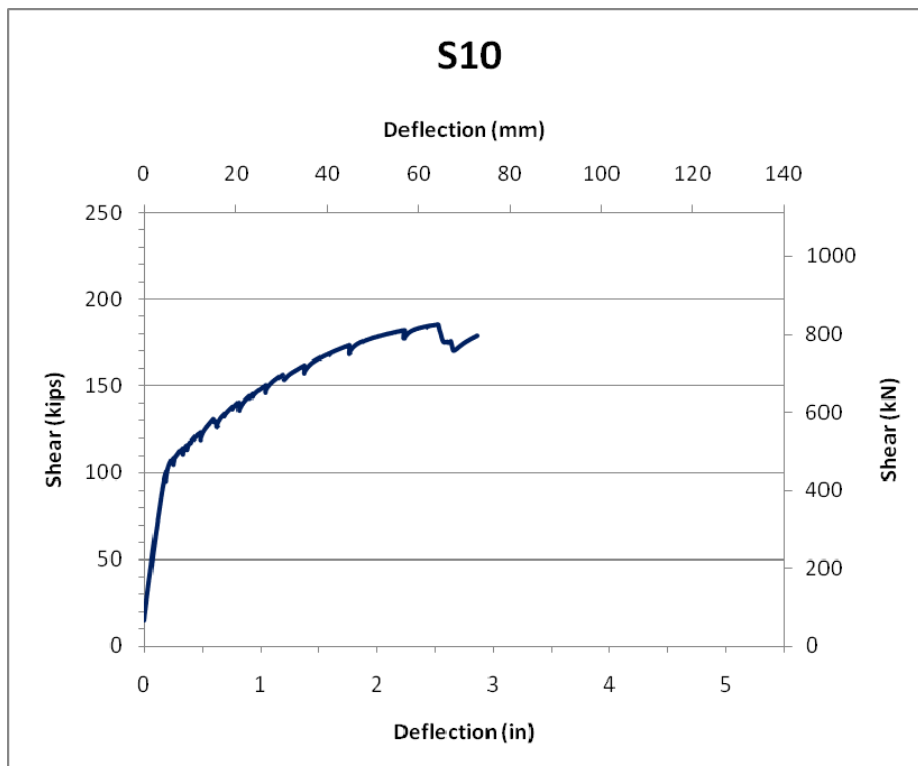


Figure 49: Shear versus deflection at load point – Specimen S10

Table 22 displays the important results such as the shear force at first shear cracking, V_{cr} , the shear force at the first stirrup yield, V_y , the maximum shear achieved, V_{max} , and the maximum deflection reached at the loading point, Δ_{max} .

Table 22: Shear responses of the specimens

		H8	S8	H10	S10
V_{cr}	<i>kips</i> (kN)	115 (511)	109 (485)	117 (520)	116 (516)
V_y	<i>kips</i> (kN)	130 (578)	136 (605)	150 (667)	156 (694)
V_{max}	<i>kips</i> (kN)	191 (850)	188 (836)	199 (885)	186 (827)
Δ_{max}	<i>in</i> (mm)	3.88 (99)	2.92 (74)	4.28 (109)	2.86 (73)

Figure 50 shows the variations in the average vertical strains obtained from the LVDT rosette readings for all of the specimens on the end that failed in shear. The strains obtained from the vertical LVDT readings are average strains determined over the 14 in (356 mm) gage length. These strains were found to be more representative of the stirrup strains than the reading obtained from the stirrup strain gages. LVDTs V1 and V2 are located at distances of 40 (1016 mm) and 26 in (660 mm), respectively from the loading point (Figure 38). As can be seen from this figure the stirrups experienced strains well above their yield strain of 2.63×10^{-3} .

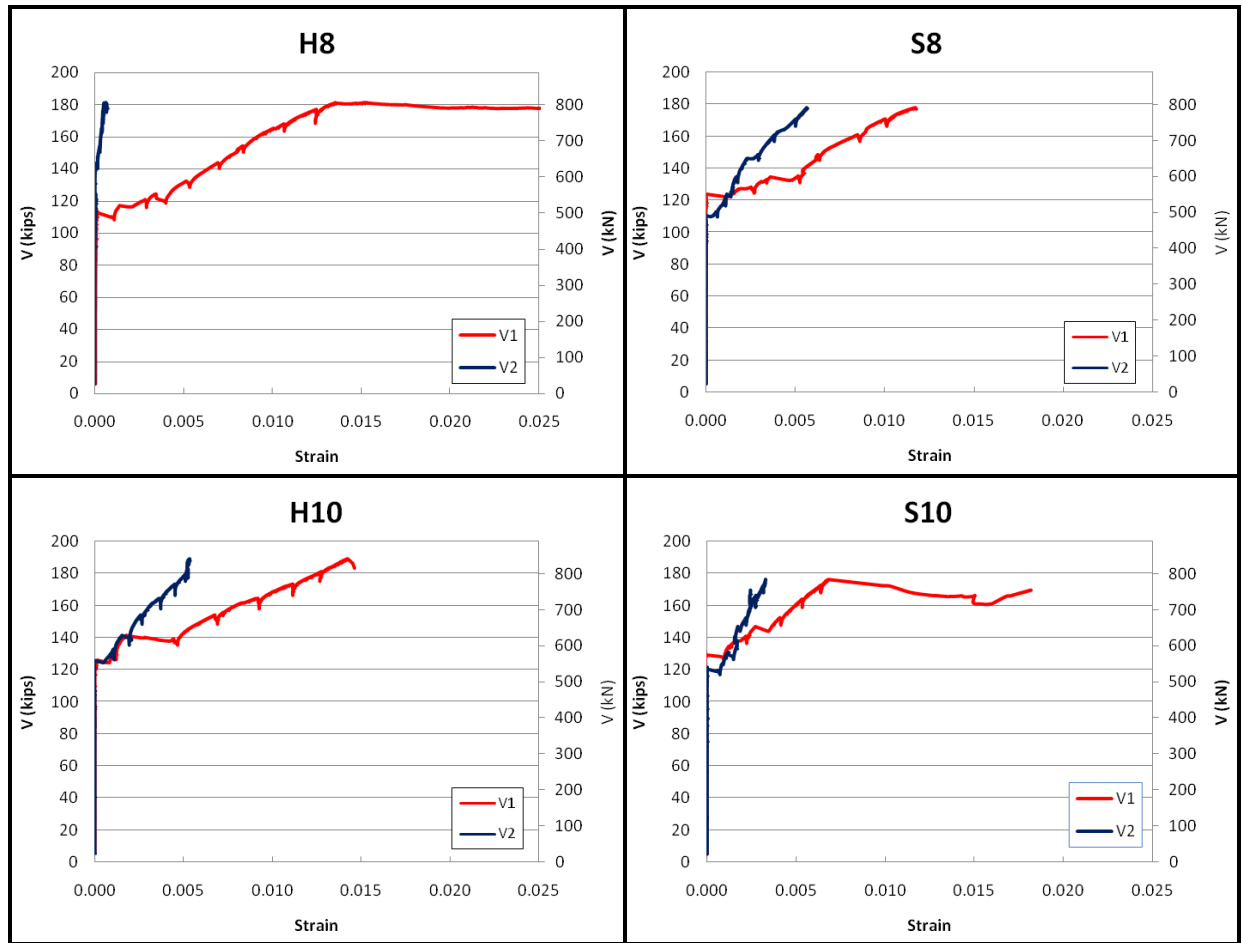
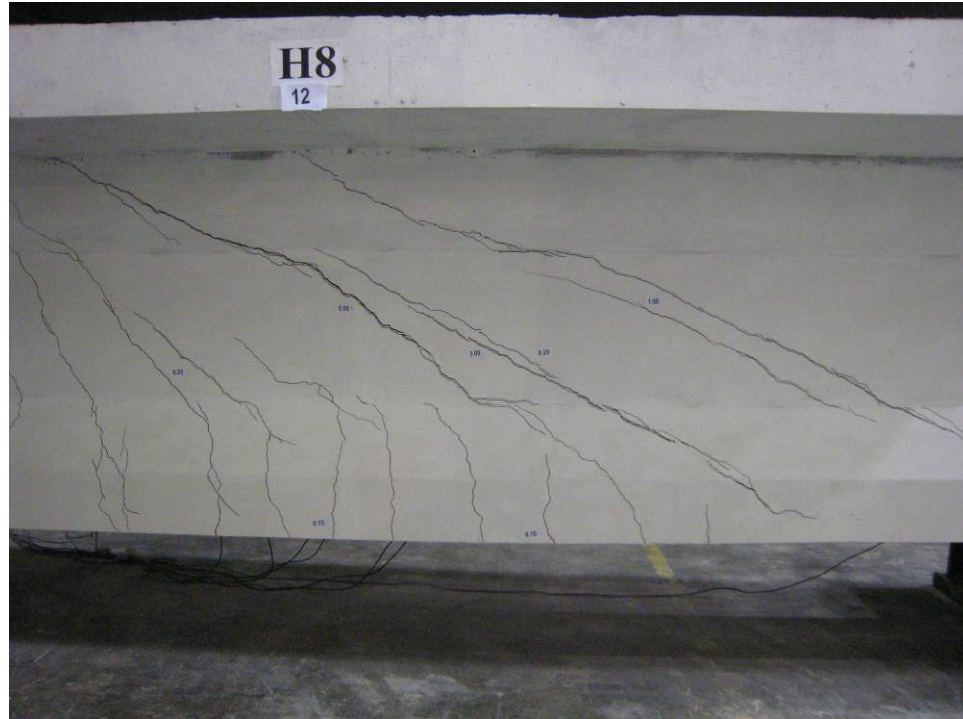


Figure 50: Variation in the average vertical strains obtained from the LVDT rosette readings on the end that failed in shear

Figure 51 to Figure 54 show the four specimens just before and right after shear failure on the ends that failed in shear.



a) Just before



b) Right after

Figure 51: Specimen H8 just before (a) and right after (b) failure



a) Just before



b) Right after

Figure 52: Specimen S8 just before (a) and right after (b) failure



a) Just before



b) Right after

Figure 53: Specimen H10 just before (a) and right after (b) failure



a) Just before



b) Right after

Figure 54: Specimen S10 just before (a) and right after (b) failure

Chapter 4: Analysis and comparison

4.1 Flexural Response

4.1.1 Prediction using AASHTO LRFD Bridge design specifications

The 2004 AASHTO evaluates the nominal flexural resistance of a member as:

$$M_n = A_{ps} f_{ps} \left(d_p - \frac{a}{2} \right) + A_s f_y \left(d_s - \frac{a}{2} \right) - A'_s f'_y \left(d'_s - \frac{a}{2} \right) + 0.85 f'_c (b - b_w) \beta_1 h_f \left(\frac{a}{2} - \frac{h_f}{2} \right)$$

AASHTO Clause 5.7.3.2

Where:

A_{ps} = Area of prestressing steel, in^2 (mm^2)

A_s = Area of nonprestressed tension reinforcement, in^2 (mm^2)

A'_s = Area of compression reinforcement, in^2 (mm^2)

b = Width of the compression face of the member, in (mm)

b_w = Web width, in (mm)

f'_c = Specified compressive strength of concrete, ksi (MPa)

f_{ps} = Average stress in prestressing steel at nominal bending resistance, ksi (MPa)

$$= f_{pu} \left(1 - k \frac{c}{d_p} \right), \text{ where } k = 2 \left(1.04 - \frac{f_{py}}{f_{pu}} \right)$$

f_y = Specified yield strength of reinforcing bars, ksi (MPa)

f'_y = Specified yield strength of compression reinforcement, ksi (MPa)

d_p = Distance from extreme compression fiber to the centroid of prestressing tendons, in (mm)

d_s = Distance from extreme compression fiber to the centroid of nonprestressing tensile reinforcement, in (mm)

$d'_s =$ Distance from extreme compression fiber to the centroid of compression reinforcement, *in (mm)*

$M_n =$ Nominal flexural resistance, *kip · in (N · mm)*

$a = c\beta_1 =$ Depth of the equivalent stress block, *in (mm)*

$\beta_1 =$ Stress block factor

$h_f =$ Compression flange depth of an I or T member, *in (mm)*

Table 23 shows the predicted values for each of the four girders, M_n . It also shows the concrete strengths for the girders and the deck slab used to predict the nominal flexural resistances of each of the girders.

Table 23: Comparison of flexural responses of four specimens

	H8	S8	H10	S10
M_{cr} <i>kips · ft (kN · m)</i>	902 (1223)	870 (1180)	939 (1273)	944 (1280)
M_{max} <i>kips · ft (kN · m)</i>	1816 (2462)	1781 (2415)	1889 (2561)	1762 (2390)
Δ_{max} <i>inches (mm)</i>	4.43 (113)	3.30 (84)	5.29 (134)	3.15 (80)
$f'_{c \text{ girder}}$ <i>ksi (MPa)</i>	7.378 (50.87)	8.605 (59.33)	9.050 (62.40)	9.555 (65.88)
$f'_{c \text{ slab}}$ <i>ksi (MPa)</i>	5.250 (36.20)	5.250 (36.20)	5.090 (35.09)	5.090 (35.09)
M_n <i>kips · ft (kN · m)</i>	1748 (2370)	1748 (2370)	1745 (2366)	1745 (2366)

Comparing the predicted flexural capacity, M_n , obtained from the AASHTO LRFD Clause 5.7.3.2, to the experimental the maximum moment achieved, M_{max} , shows that the AASHTO approach is conservative. In fact, all four beams achieved greater flexural resistances than predicted before failing in shear.

4.1.2 Comparison between the flexural behaviour of SCC and HPC concrete

The flexural response of all four beams is somewhat comparable with values exceeding those predicted. The SCC girders, however, achieved lower maximum moments, M_{\max} , than their companion HPC girders. They also experienced smaller deflections at mid-spans.

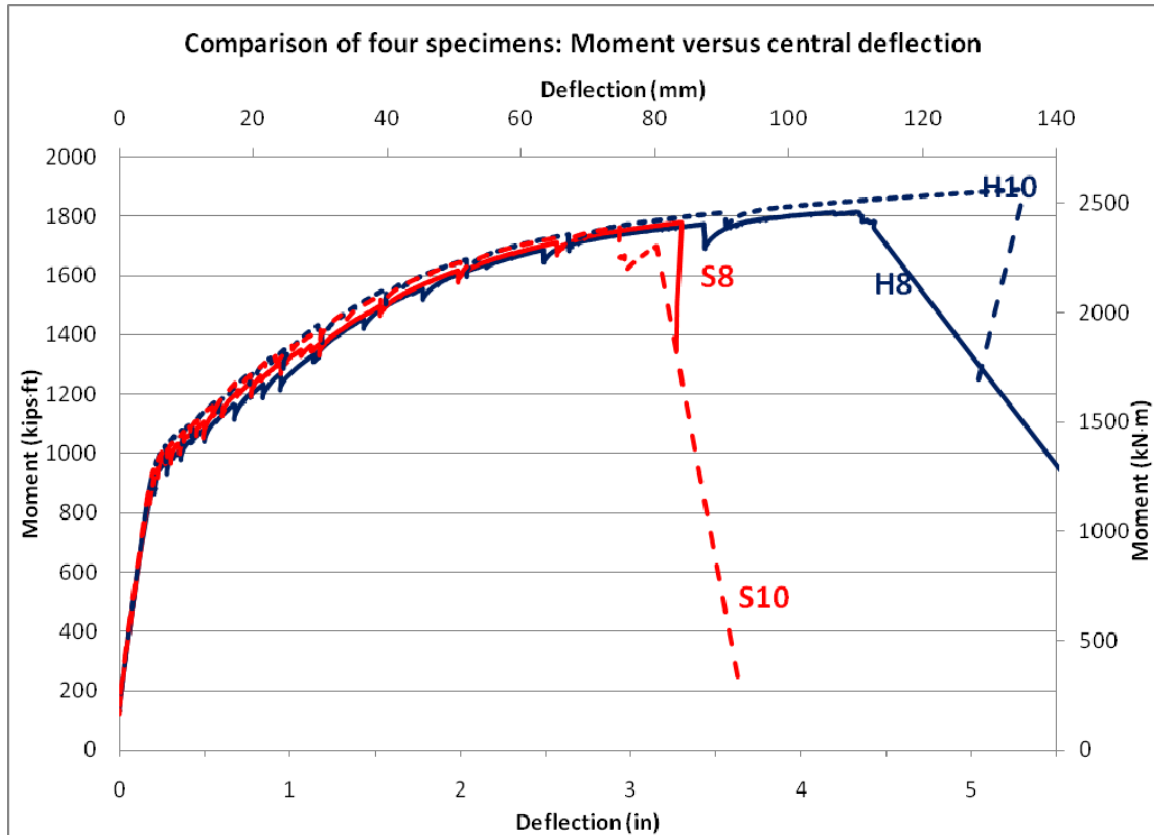


Figure 55: Comparison of moment versus central deflection responses for the four specimens

4.2 Shear Response

4.2.1 Prediction using AASHTO LRFD Bridge design specifications

The approach used by the 2004 AASHTO LRFD to evaluate the shear resistance of a member is presented in Section 1.2.3.

Table 24 shows the predicted nominal shear resistances for each of the four girders, V_n , along with the concrete strengths for the girders and the deck slabs used to predict them. The predicted values were computed using the measured properties of the reinforcing bars (Table 19) and prestressing steel (Table 20).

Table 24: Comparison of shear responses of four specimens

		H8	S8	H10	S10
V_{cr}	<i>kips (kN)</i>	115 (156)	109 (148)	117 (159)	116 (157)
V_y	<i>kips (kN)</i>	130 (176)	136 (184)	150 (203)	156 (211)
V_{max}	<i>kips (kN)</i>	191 (259)	188 (255)	199 (270)	186 (252)
Δ_{max}	<i>inches (mm)</i>	3.88 (98.55)	2.92 (74.17)	4.28 (108.71)	2.86 (72.64)
f'_c girder	<i>ksi (MPa)</i>	7.378 (50.87)	8.605 (59.33)	9.050 (62.40)	9.555 (65.88)
f'_c slab	<i>ksi (MPa)</i>	5.250 (36.20)	5.250 (36.20)	5.090 (35.09)	5.090 (35.09)
V_n	<i>kips (kN)</i>	113 (153)	115 (156)	118 (160)	119 (161)

It is noted that the experimentally determined maximum shears are considerably higher than the predicted nominal shear resistance. There are several reasons for the conservative predictions:

- The tensile strengths obtained from the flexural beam tests indicate that the corresponding code values are very conservative for the HPC and SCC concretes. In fact, clause 5.4.2.6 of the 2004 AASHTO evaluates the tensile strength for normalweight concrete as $0.24\sqrt{f'_c}$, where f'_c is in ksi. Table 25 allows a comparison between the experimental and predicted values of the concrete at 56 days cured with the same conditions as the girders.

Table 25: Tensile strengths at 56 days

Steam cured for 18 hours + Air-cured with the same conditions as the girders		H8	S8	H10	S10
Concrete compressive strength	<i>psi (MPa)</i>	7,378 (50.87)	8,605 (59.33)	9,050 (62.40)	9,555 (65.88)
Experimental tensile strength	<i>psi (MPa)</i>	960 (6.62)	922 (6.36)	850 (5.86)	855 (5.9)
Theoretical tensile strength	<i>psi (MPa)</i>	662 (4.56)	704 (4.85)	722 (4.98)	742 (5.12)
Ratio		1.45	1.31	1.18	1.15

As noted, the AASHTO underestimates the resisting capacity of the concrete in tension, therefore lowering the predicted values.

- During the testing it was evident that the strength and stiffness of the top and bottom flanges of the specimens considerably increased the shear strengths, with shear cracks of width 0.28 inch (7.1 mm) observed in the webs before shear failure occurred. In fact, looking at the LVDT readings shown in Figure 50 demonstrate that the specimens were able to withstand loads even after the stirrups had yielded: a point at which the girder is expected to fail. Cracks were widening in the web but the concrete in the thick bottom flange had not yet fully cracked.

Comparing the nominal shear resistance, V_n , to the yield resistance, V_y , shows predictions that are also are met.

4.2.2 Comparison between the shear behaviour of SCC and HPC concrete

When compared to their companion girders, the SCC girders were found to have a smaller shear force at the first shear cracking, V_{cr} ; a bigger shear force at the first stirrups yielding, V_y ; but a smaller maximum shear capacity, V_{max} . SCC girders also deflected less under the loading point.

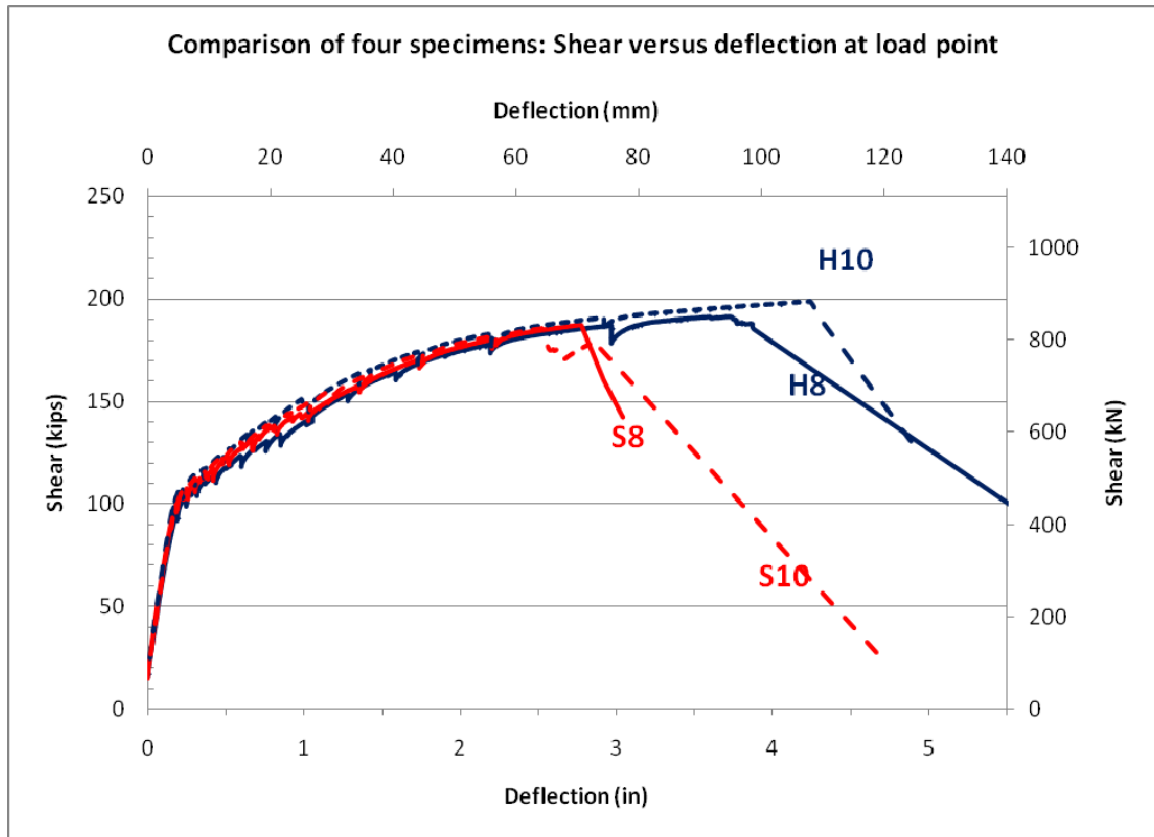


Figure 56: Comparison of shear versus deflection at loading point responses for the four specimens

Chapter 5: Conclusions

The following conclusions arise from the construction and testing of the precast pretensioned girders:

- The placement of the SCC mixture was successful: with casting only from one location at mid-span of the girders, the concrete made its way to both ends without leaving any voids even in areas of congested reinforcing steel. Moreover, there were fewer “bug holes” in the SCC concrete than the HPC.
- There was no visible segregation of the concrete in all four specimens.
- During the steam-curing operation, the target chamber temperatures of 131 °F (55 °C) and 140 °F (60 °C) for both 8,000 and both 10,000 psi (55.2 and 69 MPa) concrete mixture, respectively, was not achieved. The maximum concrete temperature reached, however, was below the maximum temperature allowed of 150 °F (65.6 °C).
- The target compressive strengths at 18-hours, required for the prestress release, of both SCC mixtures were met. The HPC mixtures showed values below but were very close to their target strengths.
- The transfer lengths found for all four concrete types and mixtures were similar. Moreover, they were all considerably shorter than values predicted by the ACI 318-08 Code and the 2004 AASHTO Specifications.
- The cracking moments were similar for the SCC girders and their companion HPC girders. The uncracked and cracked stiffnesses for all four girders were similar, although the SCC girders experienced slightly lower maximum moments.
- The HPC girders experienced flexural resistances which exceeded the predicted nominal resistance using the 2004 AASHTO Specifications. For the 8,000 and 10,000 psi (55.2 and 69 MPa) concrete girders, the experimental flexural resistances exceeded the predicted resistances by 3.8% and 8.3%, respectively.
- The SCC girders also experienced flexural resistances which exceeded the predicted nominal resistance using the 2004 AASHTO Specifications. For the 8,000 and 10,000 psi (55.2 and 69 MPa) concrete girders, the experimental flexural resistances exceeded the predicted ones by 1.9% and by less than 0.1%, respectively.

- All four girders failed in shear after developing a significant number of wide shear cracks. The maximum shear crack widths before failure were greater than 0.24 inch (6.1 mm). The stirrups developed significant strains, beyond strain hardening, with the stirrups rupturing at failure.
- The cracking and maximum shears were similar for all four girders, although the SCC girders experienced slightly lower resistances.
- The HPC and SCC girders experienced failure shears which exceeded the predicted nominal resistance using the 2004 AASHTO Specifications. The experimental shear failures exceeded the predicted values by 56% to 69%. This increased shear resistance was probably due to the strength and stiffness of the top and bottom flanges of the AASHTO girders.
- The HPC girders experienced higher deflections and hence higher ductilities than their companion SCC girders.
- The lower shear resistance and lower ductility experienced by the SCC girders is probably due to the lower volume of coarse aggregate, which reduces aggregate interlock and results in a lower energy absorption capability on the sliding shear failure plane.

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