



National Library  
of Canada

Acquisitions and  
Bibliographic Services Branch

395 Wellington Street  
Ottawa, Ontario  
K1A 0N4

Bibliothèque nationale  
du Canada

Direction des acquisitions et  
des services bibliographiques

395, rue Wellington  
Ottawa (Ontario)  
K1A 0N4

*Your file - Votre référence*

*Our file - Notre référence*

## NOTICE

The quality of this microform is heavily dependent upon the quality of the original thesis submitted for microfilming. Every effort has been made to ensure the highest quality of reproduction possible.

If pages are missing, contact the university which granted the degree.

Some pages may have indistinct print especially if the original pages were typed with a poor typewriter ribbon or if the university sent us an inferior photocopy.

Reproduction in full or in part of this microform is governed by the Canadian Copyright Act, R.S.C. 1970, c. C-30, and subsequent amendments.

## AVIS

La qualité de cette microforme dépend grandement de la qualité de la thèse soumise au microfilmage. Nous avons tout fait pour assurer une qualité supérieure de reproduction.

S'il manque des pages, veuillez communiquer avec l'université qui a conféré le grade.

La qualité d'impression de certaines pages peut laisser à désirer, surtout si les pages originales ont été dactylographiées à l'aide d'un ruban usé ou si l'université nous a fait parvenir une photocopie de qualité inférieure.

La reproduction, même partielle, de cette microforme est soumise à la Loi canadienne sur le droit d'auteur, SRC 1970, c. C-30, et ses amendements subséquents.

Canada

---

# **ADVANCES IN PULSE WIDTH MODULATION TECHNIQUES**

---

**Xiao Wang**

*B.Eng. and M.Eng.  
Tsinghua University, Beijing, China*

**A Thesis submitted to  
the Faculty of Graduate Studies and Research  
in partial fulfilment of the requirements for  
the degree of Doctor of Philosophy**

**Department of Electrical Engineering  
McGill University  
Montréal, Québec, Canada**

March 1993

© Xiao Wang, 1993



National Library  
of Canada

Bibliothèque nationale  
du Canada

Acquisitions and  
Bibliographic Services Branch

Direction des acquisitions et  
des services bibliographiques

395 Wellington Street  
Ottawa, Ontario  
K1A 0N4

395, rue Wellington  
Ottawa (Ontario)  
K1A 0N4

*Your file / Votre référence*

*Our file / Notre référence*

The author has granted an irrevocable non-exclusive licence allowing the National Library of Canada to reproduce, loan, distribute or sell copies of his/her thesis by any means and in any form or format, making this thesis available to interested persons.

L'auteur a accordé une licence irrévocable et non exclusive permettant à la Bibliothèque nationale du Canada de reproduire, prêter, distribuer ou vendre des copies de sa thèse de quelque manière et sous quelque forme que ce soit pour mettre des exemplaires de cette thèse à la disposition des personnes intéressées.

The author retains ownership of the copyright in his/her thesis. Neither the thesis nor substantial extracts from it may be printed or otherwise reproduced without his/her permission.

L'auteur conserve la propriété du droit d'auteur qui protège sa thèse. Ni la thèse ni des extraits substantiels de celle-ci ne doivent être imprimés ou autrement reproduits sans son autorisation.

ISBN 0-315-91672-9

Canada

---

## ABSTRACT

---

The phase angle control of the Two-Level Sinusoidal Pulse Width Modulation (SPWM) strategy has been studied in Part I of this thesis, and applied to a new voltage-source type PWM High Voltage Direct Current (HVDC) transmission system. The PWM-HVDC station exercises direct control over the voltage phase angle, the amplitude and the frequency at the ac terminals using the phase angle lock loop (PLL) control of the SPWM. The parallel connection of multi-terminal PWM-HVDC stations can be achieved through simple local feedback control. The feasibility studies for the system, based on laboratory experiments and numerical analysis, are reported in the thesis.

In Part II of the thesis, the Three-Level SPWM technique has been studied and applied to the controls of a 3-phase, 6-valve, current-source PWM rectifier. A new Dynamic Three-Level SPWM strategy together with its Decoupler Pre-Processor has been proposed. The strategy enables each of three phase currents of the converter to be controlled independently and linearly, so that the dynamic feedback can be channelled. The Pole Placement control method has been implemented successfully, using a real-time digital control scheme. The scheme also succeeds in active filtering. The experimental results are obtained from a 1-KVA size laboratory model with a real-time controller using three TMS320C25 DSPs. The three DSPs operating in parallel are necessary to compute the feedback algorithms with minimum delays so as to ensure sufficient frequency bandwidth.

La première partie de cette thèse fait l'étude de la commande du déphasage obtenu par la Modulation Par Largeur D'impulsion Sinusoïdale (SPWM) à Deux-Niveaux. Cette technique est implantée pour assurer l'asservissement d' HVDC de type source de tension. La station PWM Haute Tension Continu (HVDC), muni d'un contrôleur en boucle fermée du déphasage du SPWM, exerce un contrôle direct sur l'amplitude, le déphasage et la fréquence de la tension aux terminaux. On pourrait étendre ce type de commande à des stations PWM-HVDC multi-terminaux branchées en parallèle par un simple contrôle local en boucle fermée. Les études de faisabilité de ce système, basées sur des expériences de laboratoire et des analyses numériques, sont documentées dans cette thèse.

La Partie II décrit, la technique SPWM Trois-Niveaux, étudiée et appliquée à la commande d'une source de courant PWM rectificatrice 3-phases, 6-valves. On propose une nouvelle stratégie SPWM Trois-Niveaux dynamique et un Pré-Processus Découpleur associé. Cette stratégie assure à chacun des courants triphasés du convertisseur une commande indépendante et linéaire, de façon à ce que la boucle fermée dynamique puisse être canalisée. La méthode du Placement de Pôles a été appliquée avec succès en utilisant d'une part une stratégie de contrôle numérique en temps réel. Et d'autre part le filtrage actif. Les résultats expérimentaux sont obtenus d'un modèle de laboratoire d'une puissance de 1-KVA avec un contrôleur en temps réel utilisant trois DSP TMS320C25. Les trois DSP TMS320C25 opérant en parallèle sont nécessaires pour le calcul rapide des algorithmes en boucle fermée, assurant ainsi une largeur de bande suffisante.

---

## ACKNOWLEDGMENTS

---

I would like to express my sincere gratitude to Professor B.T. Ooi, my thesis supervisor, for his exceptional guidance, continuous encouragement and warm friendship throughout this research. With his kind understanding and patience, he not only contributed immensely to the direction of this work, but also made great effort to develop my abilities of study and research, and to improve my English. I would like also to thank him arranging for my financial support, from the Grant of the NSERC of Canada, throughout my graduate work in McGill.

I am grateful to Professors F.D. Galiana, H.C. Lee and Z. Wolanski for their valuable professional advices and guidance.

I am particularly indebted to my friends and colleagues in the Power Group. I have learnt a lot from many interesting discussions with J.W. Dixon, M. Tremblay, J. Liu, B.M.M. Mwinyiwiwa, N. Lujara, K. Mehrdad, J.B. Kuang, M. Huneault, F.L. Zhuang, J.A. Huang, L. Fan, L. Loud and visiting scholars S.Z. Dai and Z.C. Zhang. M. Huneault and B. Picard made an expert French translation of the Abstract. Many thanks to J. Mui and his companions in the workshop and the departmental secretaries for their kindness in helping me every time I asked for it.

My special thanks go to my parents, brother and cousin. They have extended generously their support and confidence all these years.

I wish to extend my deepest thanks to my wife and colleague, Yan, for her help, encouragement, patience and good spirits during this undertaking. She supports me with love and understanding.

---

## TABLE OF CONTENTS

---

ABSTRACT	i
RÉSUMÉ	ii
ACKNOWLEDGMENTS	iii
TABLE OF CONTENTS	iv
LIST OF ILLUSTRATIONS	viii
NOMENCLATURE	xii
 CHAPTER 1 INTRODUCTION	 1
1.1 Historical Perspective	1
1.2 Review of Previous Work on Pulse Width Modulation	8
1.3 Scope and Contributions	12
1.3.1 Bi-Logic PWM - Theory	13
1.3.2 Bi-Logic PWM - Application	13
1.3.3 Bi-Logic PWM - Implementation	14
1.3.4 Tri-Logic PWM - Theory	15
1.3.5 Tri-Logic PWM - Application	16
1.3.6 Tri-Logic PWM - Implementation	16
 CHAPTER 2 PWM HVDC TRANSMISSION SYSTEM	 18
2.1 Introduction	18
2.2 Force-Commutated Voltage-Source Converter Bridge	22
2.2.1 Switching Function $S_j$	26
2.3 Control of Voltage-Source Type PWM-HVDC Converter Station	29
2.3.1 Voltage Amplitude Control	29
2.3.2 Frequency Control	31
2.3.3 Voltage Phase Angle Control	33
2.3.4 Control Input Setting	35
	iv

2.4	Converter Station Regulation Scheme	36
2.4.1	Voltage Phase Angle Lock Loop	39
2.4.2	DC Voltage Regulator	39
2.4.3	Power Dispatcher	42
2.5	Multi-Terminal PWM HVDC Transmission System	44
2.6	Summary	47
<b>CHAPTER 3</b>	<b>EXPERIMENTAL TEST OF PWM HVDC</b>	<b>49</b>
3.1	Introduction	49
3.2	Synchronization Tests	50
3.3	Real Power Control	54
3.4	Transient Test	56
3.5	Summary	60
<b>CHAPTER 4</b>	<b>PARAMETRIC STUDY</b>	<b>61</b>
4.1	Introduction	61
4.2	System Model for Parametric Study	62
4.3	Sizing $X_L$ by AC RMS Current	66
4.4	Total Harmonic Distortion	71
4.5	V/A rating and Switching Losses	73
4.6	Summary	75
<b>CHAPTER 5</b>	<b>DYNAMIC TRI-LOGIC SPWM CONTROL OF 3-PHASE CURRENT-SOURCE CONVERTER</b>	<b>77</b>
5.1	Introduction	77
5.2	Current-Source PWM Converter and Control Difficulties	80
5.3	Dynamic Tri-Logic PWM	84
5.3.1	Tri-Logic PWM States, $Y_k(t)$	86
5.3.2	Bi/Tri-Logic PWM Translation	87
5.3.3	Single Switching Tri-Logic State Transition	91
5.3.4	Linear Signal Amplification	94
5.3.4.1	Frequency Spectrum	96



---

5.3.5	Decoupler Pre-Processing	97
5.3.5.1	<i>WYE</i> -Connected 3-Phase AC	100
5.3.5.2	<i>DELTA</i> -Connected 3-Phase AC	100
5.4	Summary	102
<b>CHAPTER 6</b>	<b>MULTI-DSP REAL-TIME CONTROL</b>	<b>103</b>
6.1	Introduction	103
6.2	Mathematical Model	105
6.3	Control Difficulties	108
6.4	Control Strategy	110
6.4.1	Discretization of System Model	111
6.4.2	Pole Placement Feedback Control	112
6.4.3	Unity Power Factor Feed-Forward Control	117
6.4.4	Frequency Bandwidth	119
6.5	Multi-DSP Control	121
6.6	Experimental Results	125
6.6.1	Active Filtering Test	127
6.6.2	Transient Test	130
6.7	Summary	131
<b>CHAPTER 7</b>	<b>CONCLUSION</b>	<b>133</b>
7.1	Advances in Pulse Width Modulation Theory	134
7.1.1	Two-Level or Bi-Logic PWM	134
7.1.2	Three-Level or Tri-Logic PWM	135
7.2	Advances in Engineering Applications	136
7.2.1	HVDC Transmission System	137
7.2.1.1	General Conclusion	138
7.2.2	Current-Source PWM Rectifier	138
7.3	Advances in The Implementation of Pulse Width Modulation Techniques	138
7.3.1	Phase Lock Loop Control	139
7.3.1.1	Real Power controlled by Phase Lock Loop	139

---

7.3.2	Multi-DSP Controlled Current-Source PWM Rectifier	139
7.3.2.1	Frequency Bandwidth and Computational Delays	140
7.3.2.2	Implementation of Dynamic Tri-Logic PWM	140
7.3.2.3	Innovative Feedback Method	140
7.4	Suggestions for Future Work	141
<b>APPENDIX A</b>	<b>IMPLEMENTATION OF VOLTAGE-SOURCE PWM CONVERTER</b>	<b>142</b>
A.1	Introduction	142
A.2	Sinusoidal Modulating Signal	143
A.3	The PLL Control	143
A.4	The VR/DISP Control	145
<b>APPENDIX B</b>	<b>IMPLEMENTATION OF DYNAMIC TRI-LOGIC PWM CONTROL</b>	<b>149</b>
B.1	Introduction	149
B.2	Converter Bridge Circuit	151
B.3	PAL Gating Logic Circuit	151
B.3.1	Bi/Tri-Logic Translation Circuit Programming	154
B.3.2	Triggering Logic Circuit Programming	154
B.4	A/D Converter Circuit	160
B.5	Voltage Sensor Circuit	160
<b>APPENDIX C</b>	<b>SOFTWARE DESIGN OF MULTI-DSP CONTROL</b>	<b>164</b>
C.1	Introduction	164
C.2	Control Task Distribution	164
C.3	Program Flow Charts and List	165
<b>REFERENCES</b>		<b>186</b>

---

## LIST OF ILLUSTRATIONS

---

CHAPTER 1:		Page
Fig.1-1	Two-Level or Bi-Logic PWM.	3
Fig.1-2	The 3-phase, voltage-source PWM power converter topology.	5
Fig.1-3	The 3-phase, current-source PWM power converter topology.	5
Fig.1-4	Three-Level or Tri-Logic PWM.	6
CHAPTER 2		
Fig.2-1	Simplified circuit topology of 3-phase, voltage-source, boost type PWM-HVDC converter bridge.	23
Fig.2-2	The equivalent circuit of voltage-source PWM converter.	24
Fig.2-3	Sinusoidal PWM strategy.	27
Fig.2-4	Schematic of voltage-source PWM-HVDC converter station with controls on voltage amplitude, frequency and phase angle.	30
Fig.2-5	Illustration of integral voltage phase angle control by frequency jogging.	33
Fig.2-6	Illustration of proportional voltage phase angle control.	34
Fig.2-7	Voltage-source PWM-HVDC converter station connected to an ac utility system.	36
Fig.2-8	Phasor diagram of Fig. 2-7.	38
Fig.2-9	Schematic of DC Voltage Regulator.	41
Fig.2-10	Schematic of Power Dispatcher.	42
Fig.2-11	Multi-area ac system united by a dc grid through parallel connections of DISP and VR.	45
CHAPTER 3		
Fig.3-1	Single line diagram of back-to-back dc link consisting a DC Voltage Regulator and a Power Dispatcher situated at mid-point	50

	of transmission line.	
Fig.3-2	Dc link voltage of DC Voltage Regulator as a function of voltage phase angle $\delta$ introduced by a phase shifting transformer between ac source and converter.	52
Fig.3-3	DC link voltage of DC Voltage Regulator as a function of frequency deviation.	53
Fig.3-4	Power output of Power Dispatcher as a function of frequency deviation.	53
Fig.3-5	DC link power versus voltage phase angle characteristics.	54
Fig.3-6	Transient waveforms in DC Voltage Regulator during power reversal.	57
Fig.3-7	Transient waveforms in multi-terminal experiment.	59
Fig.3-8	Transient in disconnection of <i>B</i> -Phase of DC Voltage Regulator.	60
<b>CHAPTER 4</b>		
Fig.4-1	Converter station connected to ac utility system and dc system used for feasibility study.	63
Fig.4-2	Phasor diagram of fundamental Fourier Series component of voltage.	65
Fig.4-3	Fundamental and <i>rms</i> converter ac current as a function of $X_L$ .	68
Fig.4-4	$V_A$ of $X_L$ as a function of $X_L$ .	70
Fig.4-5	Cost Reference Factor ( $X_L \times i_{n2rms} \times v_{max}$ ) vs $X_L$ .	70
Fig.4-6	Total DC Voltage Harmonic Distortion Factor vs $X_L$ .	72
Fig.4-7	Total DC Current Harmonic Distortion Factor vs $X_L$ .	72
Table 4-1	System parameters chosen for feasibility study.	66
<b>CHAPTER 5</b>		
Fig.5-1	Current-source PWM converter with dynamic Tri-Logic PWM trigger circuit and Decoupler Pre-Processor.	81
Fig.5-2	Generation of Tri-Logic PWM.	90
Fig.5-3	Switch state #2 and four contiguous states in 6-valve	92

	current-source PWM converter bridge.	
Fig.5-4	Contiguous states of 6-valve current-source converter.	93
Fig.5-5	Spectrum of Bi-Logic PWM signals $X_j$ ; Spectrum of Tri-Logic PWM signals $Y_k$ .	97
Fig.5-6	Decoupler Pre-Processor for <i>wye</i> -connected 3-phase ac.	99
Fig.5-7	Decoupler Pre-Processor for <i>delta</i> -connected 3-phase ac.	101
Table 5-1	Current-source PWM converter states.	87
Table 5-2	Truth table of Bi/Tri-Logic translation.	88
Table 5-3	Sequence of Tri-Logic States.	91

## CHAPTER 6

Fig.6-1	Single phase equivalent ac circuit of the current-source PWM converter.	105
Fig.6-2	Open-loop frequency response of the system showing $L$ - $C$ resonance.	109
Fig.6-3	Pole Placement control scheme.	113
Fig.6-4	Hardware configuration of current-source PWM converter with multi-DSP controller.	122
Fig.6-5	Active parallel computing times of the DSPs in each sampling period.	126
Fig.6-6	Waveforms without Pole Placement feedback control.	128
Fig.6-7	Waveforms with Pole Placement feedback control	129
Fig.6-8	Transient response of a step change in the dc link current reference when the Pole Placement state feedback control is used.	130
Table 6-1	Current-source PWM converter parameters.	125
Table 6-2	Length of active computing time for the DSPs.	127

## APPENDIX A

Fig.A-1	Sinusoidal modulating signal generator circuit.	146
Fig.A-2	Phase Lock Loop controller.	147
Fig.A-3	EPROM Address generator circuit.	148

**APPENDIX B**

Fig.B-1	Experimental set-up of the multi-DSP controlled 3-phase, current-source PWM converter system.	150
Fig.B-2	The main switching circuit of 3-phase current-source PWM converter.	152
Fig.B-3	PAL Gating Logic circuit.	153
Fig.B-4	The PAL Gating Logic circuit implementation using the speedwire board.	155
Fig.B-5	The A/D converter circuit.	161
Fig.B-6	The A/D converter circuit implementation using speedwire board.	163
Fig.B-7	The capacitor voltage sensor circuit.	163
Table B-1	The program list of PAL chip #1 design.	156
Table B-2	The program list of PAL chip #2 design.	156
Table B-3	The program list of PAL chip #3 design.	157
Table B-4	The program list of PAL chip #4 design.	158
Table B-5	The program list of PAL chip #5 design.	159
Table B-6	The program list of PAL chip #6 design.	159
Table B-7	The program list of PAL chip PAL-ADC-#2 design.	162
Table B-8	The program list of PAL chip PAL-ADC-#1 design.	162

**APPENDIX C**

Fig.C-1	The flow charts of DSP "main" programs.	167
Fig.C-2	The flow charts of interrupt service subroutines for parallel processing controls (continued on Fig.C-3).	168
Fig.C-3	The flow charts of interrupt service subroutines for parallel processing controls (continued from Fig.C-2).	169
Table C-1	The list of DSP #2 control program.	170
Table C-2	The list of DSP #3 control program.	178
Table C-3	The list of DSP #1 control program.	184

---

## NOMENCLATURE

---

### PART I (CHAPTERS 2, 3 and 4)

$v_a, v_b, v_c$	Instantaneous phase-to-neutral source voltages
$i_a, i_b, i_c$	Instantaneous ac line currents
$L$	Ac line inductance
$C_{dc}$	Dc link capacitance
$V_{dc}$	Dc link voltage
PWM	Pulse width modulation
HVDC	High voltage direct current
$I_{dc1}$	Output rectifier dc current before capacitor $C_{dc}$
$I_{dc2}$	Output dc link current after capacitor $C_{dc}$
$v_{pa}, v_{pb}, v_{pc}$	Instantaneous phase-to-neutral terminal voltages
$\bar{v}_{pa}, \bar{v}_{pb}, \bar{v}_{pc}$	Fourier Series fundamental components of voltages $v_{pa}, v_{pb}, v_{pc}$
$\bar{v}_{mREF}$	Amplitude reference of $\bar{v}_{pa}, \bar{v}_{pb}, \bar{v}_{pc}$
$\Delta v_{mc}$	Amplitude adjusting input of $\bar{v}_{pa}, \bar{v}_{pb}, \bar{v}_{pc}$
$\bar{v}_{mc}$	Amplitude control variable of $\bar{v}_{pa}, \bar{v}_{pb}, \bar{v}_{pc}$
$\omega$	Angular frequency
$\omega_{cREF}$	Frequency reference of $\bar{v}_{pa}, \bar{v}_{pb}, \bar{v}_{pc}$
$\Delta \omega_c$	Adjusting input of frequency
$\omega_c$	Control variable of frequency
$\theta_m$	Phase angle of voltage $\bar{v}_{pa}$
$\theta_{cREF}$	Reference of phase angle $\theta_m$
$\Delta \theta_c$	Adjustment input of phase angle $\theta_m$
$\theta_c$	Control variable of phase angle $\theta_m$
PLL	Phase lock loop
VR	DC voltage regulator

DISP	Power dispatcher
$v_{ir}$	Peak value of triangular carrier
$v_{ma}, v_{mb}, v_{mc}$	Instantaneous modulating signals
$S_j$	Switching function
$v_{Tn}$	Thevenin equivalent voltage of ac utility system
$i_n$	Thevenin equivalent current of ac utility system
$\theta_{Tn}$	Phase angle of voltage $v_{Tn}$
$\omega_{Tn}$	Angular frequency of voltage $v_{Tn}$
$R_{Tn}$	Thevenin equivalent resistance of ac utility system
$L_{Tn}$	Thevenin equivalent line inductance of ac utility system
$X_{Tn}$	impedance of $L_{Tn}$
$X_L$	Local impedance at converter terminal
$\epsilon_{V_{dc}}$	Error between $V_{dcREF}$ and $V_{dc}$
$P_n$	Real power passing through the converter
$P_{nREF}$	Reference value of $P_n$
$\epsilon_{P_n}$	Error between $P_{nREF}$ and $P_n$
$K_p$	Gain of proportional feedback control
$K_i$	Gain of integral feedback control
$X_{dc}$	Impedance of dc link
$R_{dc}$	Resistance of dc link
$X_{c1}$	Capacitance at dc terminal
$X_{c2}$	Capacitance after dc link inductor
$i_{n1}$	Primary current of station transformer
$i_{n2}$	Secondary current of station transformer
$v_{b1}$	Primary fundamental voltage of station transformer
$v_{b2}$	Secondary fundamental voltage of station transformer
$v_{pj}$	<i>rms</i> value of $\bar{v}_{pa}, \bar{v}_{pb}, \bar{v}_{pc}$
$\theta_{n1}$	Phase angle between $v_{Tn}$ and $v_{b1}$
$\theta_{n2}$	Phase angle between $v_{b2}$ and $v_{pj}$
$M$	Modulating index



**PART II (CHAPTERS 5 and 6)**

$C$	Ac terminal capacitance
$L$	Ac line inductance
$R$	Resistance of ac line
$L_{dc}$	Inductance of dc link
$R_{dc}$	Resistance of dc link
$I_{dc}$	Dc link current
$i_{pa}, i_{pb}, i_{pc}$	Instantaneous terminal input currents
$\bar{i}_{pa}, \bar{i}_{pb}, \bar{i}_{pc}$	Fourier Series fundamental components of currents $i_{pa}, i_{pb}, i_{pc}$
$S_{pa}, S_{pb}, S_{pc}$	Control variables of currents $\bar{i}_{pa}, \bar{i}_{pb}, \bar{i}_{pc}$
$S_{ma}, S_{mb}, S_{mc}$	Modulating signals of Bi-Logic SPWM
$S_{tra}, S_{trb}, S_{trc}$	Triangular carriers of Bi-Logic SPWM
$P_{Str}$	Peak value of triangular carrier
$Y_a, Y_b, Y_c$	Tri-Logic PWM variables
$X_a, X_b, X_c$	Bi-Logic PWM variables
$\bar{X}_a, \bar{X}_b, \bar{X}_c$	Fourier Series fundamental components of signals $X_a, X_b, X_c$
$i_u, i_v, i_w$	Instantaneous phase currents in delta-connected voltage source
$i_o$	Zero sequence current
$v_{sa}, v_{sb}, v_{sc}$	Instantaneous ac phase-to-neutral supply voltages
$v_{so}$	Magnitude of $v_{sa}, v_{sb}, v_{sc}$
$i_{sa}, i_{sb}, i_{sc}$	Instantaneous ac line currents
$i_{sao}, i_{sbo}, i_{sco}$	Steady-state operating values of currents $i_{sa}, i_{sb}, i_{sc}$
$\Delta i_{sa}, \Delta i_{sb}, \Delta i_{sc}$	Small perturbation values of currents $i_{sa}, i_{sb}, i_{sc}$
$v_{ca}, v_{cb}, v_{cc}$	Instantaneous phase-to-neutral ac capacitor voltages
$v_{cao}, v_{cbo}, v_{cco}$	Steady-state operating values of voltages $v_{ca}, v_{cb}, v_{cc}$
$\Delta v_{ca}, \Delta v_{cb}, \Delta v_{cc}$	Small perturbation values of voltages $v_{ca}, v_{cb}, v_{cc}$
$\bar{i}_{pao}, \bar{i}_{pbo}, \bar{i}_{pco}$	Steady-state operating values of currents $\bar{i}_{pa}, \bar{i}_{pb}, \bar{i}_{pc}$
$\Delta \bar{i}_{pa}, \Delta \bar{i}_{pb}, \Delta \bar{i}_{pc}$	Small perturbation values of currents $\bar{i}_{pa}, \bar{i}_{pb}, \bar{i}_{pc}$
$i_{so}$	Magnitude command of currents $i_{sa}, i_{sb}, i_{sc}$

PAL	Programmable array logic
DSP	Digital signal processor
$\Delta T$	Sampling period
$f_o$	Line frequency
$f_{tr}$	Frequency of triangular carrier
$R_{load}$	Resistance of dc load
$K_{p-dc}$	Proportional gain of dc current regulator
$K_{l-dc}$	Integral gain of dc current regulator

## INTRODUCTION

### 1.1 Historical Perspective

Power Electronics began with the vacuum tube diode which made ac to dc rectification possible [1]. The advent of thyatron [1], with the gate-turn-on capability, introduced an element of controllability. By delaying the gating pulse, it became possible to control the amount of the rectified power [2]. The turn-off of the thyatron depended on the negative half of the ac voltage cycle - or what is termed, line-commutation. An entire technology has developed around the line-commutation concept: the *Graetz* bridge [2], the line-commutated inverters [3], the *High Voltage Direct Current* (HVDC) Transmission System [2], the *Static VAR Controller* (SVC) [4,5], the cycloconverters [3].

By the mid-1960s, the solid-state thyristors, i.e., the *Silicon Controlled Rectifier* (SCR) [6] replaced the thyatrons and the mercury-arc rectifiers [1] in the line-commutated technology. Like the thyatrons, the thyristors have gate-turn-on capability but have to be turned OFF by the reversal of the anode-cathode voltage. Apart from line-commutation, this voltage reversal can also be achieved by a force-commutation circuit which turns-on an auxiliary thyristor to connect the reversed voltage from a previously charged capacitor to the principal thyristor [7, 8]. The force-commutated thyristors enable the dc-to-ac inversion to be carried out over a range of operating frequencies for variable speed ac motor drive [9, 10].

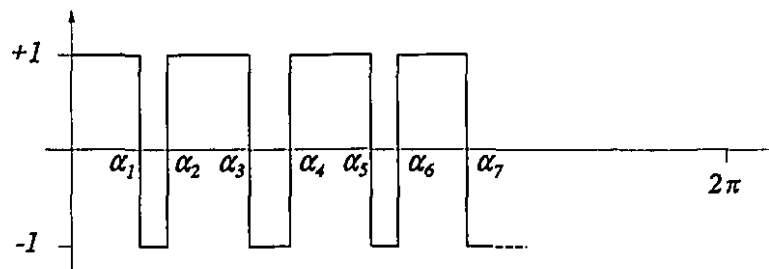
As the research in the variable speed ac motor drives progressed, it became clear that the ac voltage amplitude must be coordinated with the motor speed [11]. When the inverter source is a fixed dc voltage or dc current, the amplitude control can be achieved only by *Pulse Width Modulation* (PWM) [12], that is by controlling the relative durations of the ON and the OFF states of the force-commutated thyristors.

Originally the force-commutated thyristor circuits were slow, complex and costly. In the past 15 years, the solid-state industries have produced a range of power switches which have both gate-turn-on and gate-turn-off capabilities [13]. In this thesis, these power switches will be described under the generic term, "Valves". Some examples of these valves are: *Bipolar Power Transistors* (BJT)

[14], power *Metal Oxide Semiconductor Field Effect Transistors* (MOSFET) [15], *Insulated Gate Bipolar Transistors* (IGBT) [16], *Static Induction Transistors* (SIT) [14]. They have a broad range of switching speeds, voltage and current ratings. Tending to be slower but reaching to the higher voltage and current levels are the *Gate-Turn-off Thyristors* (GTO) [17], the *Static Induction Thyristors* (SITH) [18], the *MOS-Controlled Thyristors* (MCT) [19].

The availability of these valves has given a great impetus to the development of the PWM concepts. In addition to controlling the frequency and the amplitude of the modulating signal, the objectives have been broadened to include the control of the Fourier harmonics so as to reduce the motor torque pulsations [11,20,21]. In consequence, there is a rich literature on PWM methods [22], especially on what is described in this thesis as the Two-Level or Bi-Logic PWM [23].

Fig. 1-1 illustrates the Bi-Logic PWM. As the two logic levels are fixed at  $+1$  and  $-1$ , the degrees of freedom in the specification of the Fourier series



**Figure 1-1** Two-Level or Bi-Logic PWM.

components are left to the choice of the switching angles  $\alpha_1, \alpha_2, \dots, \alpha_N$ . A good part of the literature is concerned with different algorithms for determining the switching angles. They can be classified as the Static Types and the Dynamic Types. In the Static Type, the switching angles have been determined by optimizing a chosen criterion function. The criterion function specifies the amplitudes of the fundamental and the critical harmonics of interest. The angles are solved by off-line computation in a optimization program and then stored in EPROMs and executed in real-time in the control module of the converter [24-27]. The description "Static" is applied to this class of PWM technique because the PWM waveforms are correct only for the periodic steady-state operating regime.

In contrast, the Dynamic Type of PWM strategies can cope with the transitions from one steady-state to another steady-state operating regime. The *Sinusoidal PWM* (SPWM) method [12], which is used in this thesis, is an example of the Dynamic Type. The modulating signal is sampled, and the algorithm produces a Bi-Logic output whose "local average" of the sampled period is proportional to the sample of the modulating signal. In many aspects, the converter under SPWM control is a sampled linear amplifier.

The research in the PWM strategies has been matched by research in bridge topologies. It is now recognized that the 3-phase, 6-valve bridge converter has two basic topologies: the Voltage-Source Type of Fig. 1-2 and the Current-

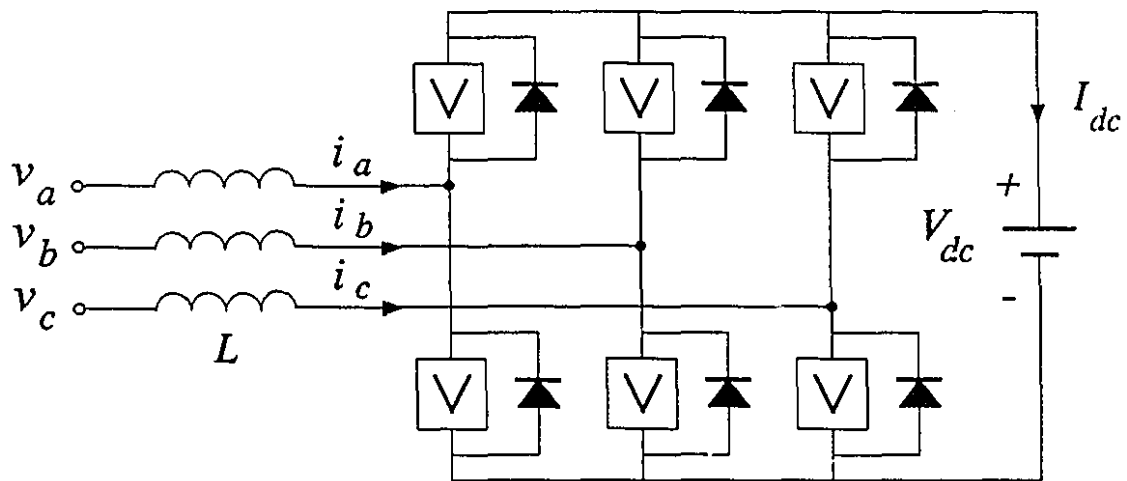


Figure 1-2 The 3-phase, voltage-source PWM power converter topology.

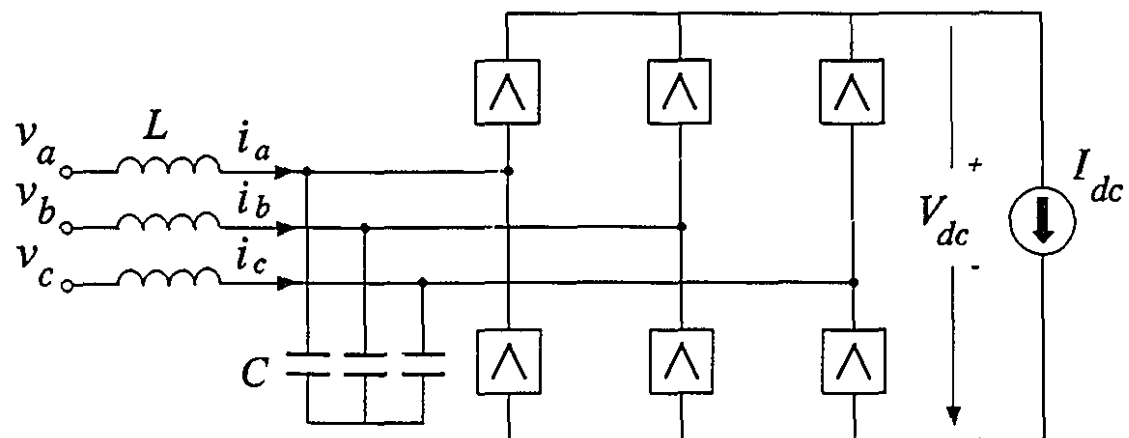


Figure 1-3 The 3-phase, current-source PWM power converter topology.

Source Type of Fig. 1-3, in which the boxed "V" represents the valve and with the arrow-head of the "V" indicating the direction of valve current flow. They are nearly (but not exactly) the circuit theory duals of each other. As such, they have almost complementary characteristics. For example power reversal on the dc side of the bridge is accomplished in the Voltage-Source Type of Fig. 1-2 by current-reversal (dc voltage unidirectional), and in the Current-Source Type of Fig. 1-3 by voltage reversal (dc current unidirectional).

In the past, the Bi-Logic PWM controls of Fig. 1-1 had been applied to control both the Voltage-Source Type (Fig. 1-2) and the Current-Source Type (Fig. 1-3) topologies. While the ac currents of the voltage-source converter came out as well-defined near sinusoidal waveforms [28-37], the valves of the current-source converter could not switch as intended [38-39]. Hombu, Ueda and Ueda [40,41] recognized the reason for the failure in the current-source topology and they have shown that instead of the Bi-Logic PWM, it is necessary to use the Three-Level or Tri-Logic PWM [23], as illustrated in Fig.1-4. The PWM Logic must have three levels:  $+I$ ,  $0$  and  $-I$ . Since then, many research groups [42-46]

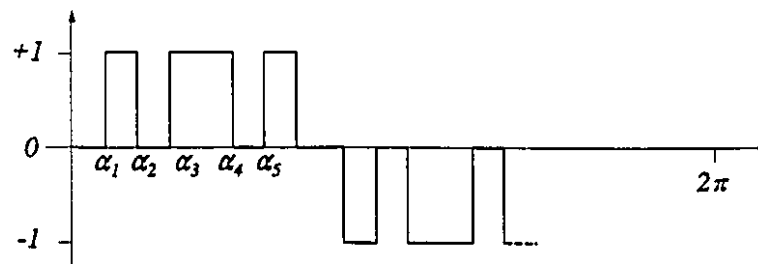


Figure 1-4 Three-Level or Tri-Logic PWM.



began researching on the Tri-Logic PWM. Up to this thesis, the Tri-Logic PWM strategies had been based on the Static Type. Because of the late start of the Tri-Logic PWM, the Current-Source Type PWM bridge converter is relatively backward with respect to its voltage-source dual.

In parallel with the research in modulation techniques and bridge topologies, there have been active interests in applying classical and modern control theories in the inverter-motor drive systems. An outstanding success here is the example of the induction motor which can now form part of a sophisticated machine tool drive because the attributes of fast controllability are conferred to it by vector control feedback [47,48].

All the historical development occurred in a period of transition from analogue to digital circuitry. To avoid the need for repeated component retuning because of their aging and thermal drifts, the trend is to digitize whenever possible. Many of the Static Type of PWM strategies have been implemented using EPROMs supervised by microprocessors [20,21,24-27]. But the early microprocessors had been too slow for the PWM converter applications and real-time digital feedback controls were reduced and limited to the "look-up table" approach. Recently, very fast Digital Signal Processors (DSPs) with facilities for parallel connection have appeared in the market. This offers the opportunity to use the computational power of the parallel DSPs to implement digital control in real-time.

The historical perspective has given a broad picture of the development of Power Electronics. The PWM principle is seen as the key element because it enables the valve to modulate the electric power while meeting harmonic constraints. For this reason, the thesis is focused on making contributions to the PWM Theory, its Applications and its Implementation.

## 1.2 Review of Previous Work on Pulse Width Modulation

The industrial success of PWM is found mainly in inverter applications in: (1) Variable Speed AC Motor Drives [49] and (2) *Uninterrupted Power Supplies* (UPS). The capability of the PWM inverter to produce variable-amplitude, variable-frequency, high quality voltage/current waveforms has been put to use in sophisticated drives, the notable example of which is the vector control [47,48]. The high quality UPS with closely regulated voltage and frequency is now indispensable for many critical loads such as computer systems and robotic systems [50-53].

Because most of the problems associated with the PWM inverter have been solved, researchers have recently turned their attention to PWM rectifiers. The early research on PWM rectifiers based on the Graetz bridge, began around the end of the 1970s [9,10,54-57]. As the gate-turn-off valves were then not available, the force-commutation of the thyristors were achieved by auxiliary commutation circuits.

Around the mid-1980s, German [28,29] and Chinese [30] researchers, and McGill University initiated research on the PWM rectifier based on the Voltage-Source Topology of Fig. 1-2.

The PWM rectifiers of McGill University were initially implemented using hysteresis-band control of the voltage-source bridge [31-37]. Both the 3-phase and the single-phase rectifiers were studied. These stand-alone rectifiers were capable of: (1) unity power factor operation, (2) near sinusoidal current waveforms, (3) regulated dc voltage, (4) fast response, and (5) bi-directional power transfer. The series of studies identified the design parameters with respect to: (i) waveform distortion limit, (ii) loss of waveform control limit and (iii) instability limit.

Recognizing that the well-known SPWM technique can produce the same quality of waveform at a lower switching rate than hysteresis current control, the research group at McGill University redesigned the rectifier based on the SPWM strategy. Incidentally, this redesign also brought a return in the form of the cost savings of the three high quality current sensors needed in hysteresis current control. In the absence of the information concerning the instantaneous line currents, the redesign needed a feedforward path so as to compute the converter ac terminal voltages required for the line current to be in phase with the ac voltages - so as to operate at unity power factor. The first iteration of the redesign [58] was not entirely successful because the stable operating region was found to be restrictive. The reason for the limited stability region was that the

dynamic term involving a  $Ldi/dt$  voltage was left out in the feedforward path. On restoring the missing term in the second iteration [59] of redesign, the stability region was equivalent to that of the hysteresis control.

This experience high lighted the importance that the PWM controller must be a virtual linear amplifier having the frequency bandwidth to channel control information signals, be it feedforward, feedback or active filtering signals.

In anticipation that higher voltage and current ratings will always be asked of the successful PWM rectifier, research towards meeting the higher ratings was pursued based on series and parallel connections of the bridge modules [52,53]. The initial studies based on hysteresis controlled PWM rectifiers have demonstrated, through simulations and experiments, that multi-module connections are feasible [60]. A later study based on the SPWM technique have shown that by phase shifting of the triangular carrier signals, harmonic elimination improves the waveform quality [61]. This is viewed as a significant finding because it will be possible to achieve high quality ac waveforms even when the very slow valves such as GTOs are used in the individual bridge module. By the technique of phase shifting in a large number of bridge modules, the harmonic cancellations remove the low order switching harmonics of the GTOs, while retaining the broad frequency bandwidth of the modulating signal. In fact, this important research conclusion crosses a hurdle giving justification for initiating the study of the PWM High Voltage Direct Current (HVDC) Transmission System in Part I of this thesis.

The existing HVDC Transmission System is based on the line-commutated thyristor technology [2,62,63]. After several decades of research and development, it has become a mature engineering science with applications in under-water transmission links, back-to-back asynchronous links and in very long distance transmission. Many researchers had been alert to the benefits which GTOs and force-commutation could bring to HVDC, especially the capability to operate at leading power factor [64-68]. Their bridge topology was based on the Graetz bridge which is the current-source topology of Fig. 1-3. Since the research pre-dated the work of Hombu, Ueda and Ueda [40,41], it would have failed in practice for want of the Tri-Logic PWM.

In fact, many of the PWM inverters for variable speed drives, which were claimed to be the Current-Source Type, also failed for the same reasons. After Hombu, Ueda and Ueda discovered that the Tri-Logic PWM of Fig. 1-4 had to be used, many Tri-Logic PWM schemes were synthesized [42-46]. These were of the Static Type and were obtained by the optimization of a criterion function which specifies the desired harmonic composition of the steady-state waveform.

In McGill University, following the successful research and development of the Voltage-Source Type PWM rectifiers, work was initiated with the objective of realizing a Current-Source Type PWM rectifier. The research followed a one-to-one equivalencing of Voltage-Source Type PWM rectifier to its circuit theory dual [69-72]. The three parallel legs of the six valves in the bridge of Fig. 1-2 have their equivalents in the form of three series-connected single-phase (4-valve)

bridges. As each single-phase bridge can operate with the Bi-Logic PWM strategy, no serious difficulty has been encountered. Following the successful implementation of the conceptual current-source PWM rectifier, the next challenge is to reduce the three series-connected single-phase bridges (involving 12 valves) to the more economical three parallel 6-valve bridge of Fig. 1-3 [73]. The PWM rectifier based on Fig. 1-3 requires a Tri-Logic PWM strategy. But it cannot be a Static Type. This is because it must be able to implement feedforward and feedback signals so as to operate at unity power factor and regulate the dc side current. Recognizing this challenge, Part II of this thesis is concerned with developing a Dynamic Type, Tri-Logic PWM to operate the 3-phase, 6-valve, current-source type PWM rectifier.

### 1.3 Scope and Contributions

The objectives of the research, reported in this thesis, are to make contributions to the PWM techniques as applied to Power Electronics in: (1) theory, (2) applications and (3) implementations. The contributions have been made against the background described in the **Historical Perspective** and the **Review of Previous Work**.

In describing the scope and the contributions, the thesis is organized in two parts:

Part I, Chapters 2, 3 and 4, Two-Level or Bi-Logic PWM,

Part II, Chapters 5 and 6, Three-Level or Tri-Logic PWM.

## **PART I CHAPTERS 2, 3 and 4**

### **1.3.1 Bi-Logic PWM – Theory**

In both the Historical Perspective and the Review of Previous Work, mention has been made that the Bi-Logic PWM and the Voltage-Source Type bridge have received considerable research attention especially in inverter drives which employ amplitude and frequency controls. For this reason, the Bi-Logic PWM theory is already at a mature level and this thesis adopts the Sinusoidal Pulse Width Modulation (SPWM) for its own use, because it is the Dynamic Type and it is easy to implement in the laboratory.

The unexplored avenue of research in this thesis is in the third control attribute of SPWM, namely the phase angle control. The phase angle control and the frequency control are not entirely independent because frequency is the time derivative of angle. In the highly inductive, electric power utility environment, the phase angle control is the lever for controlling the real ac power.

### **1.3.2 Bi-Logic PWM – Application**

The application of the phase angle and frequency controls forms the bulk of Part I which is essentially a feasibility study [74-76] of a next generation HVDC Transmission System based on the Voltage-Source Type PWM converter of Fig. 1-2. The phase angle and the frequency controls play a pivotal role in the synchronization, the power dispatch through the converter stations and the voltage

regulation of the PWM-HVDC Transmission System.

As the existing thyristor HVDC Transmission System is based on the Current-Source Type topology, the contributions to the conceptual designs in **Chapter 2** are significant, since the Voltage-Source Topology is a revolutionary departure and there is a little in the way of precedents to follow. Tests using 1-KVA size laboratory modules (reported in **Chapter 3**) have proven the soundness of the concepts. The experimental research is followed by the parametric studies [77] of **Chapter 4** which demonstrate that the sizes and ratings of the components of the PWM-HVDC station are comparable to those used in the existing thyristor station and therefore the voltage-source PWM-HVDC station is economically not infeasible.

The research has used laboratory-size modules to prove the superior performance characteristics of the Voltage-Source Type PWM-HVDC over that of the existing thyristor line-commutated HVDC. Its proven capability for multi-terminal operation with local controls only cannot be equalled by the thyristor HVDC which requires centralized control and, in consequence, vulnerable remote communication links.

### **1.3.3 Bi-Logic PWM – Implementation**

The conceptual design at the system level (multi-terminal PWM-HVDC) can be successful only when the designs at the sub-system level and the hardware



implementations are successful in the first place. The innovative contribution at the hardware implementation level, in the form of the *Phase Lock Loop* (PLL) controller of Fig. 2-4 and **Appendix A**, is necessary to synchronize the PWM converter to the nominal standard frequency of the utility system. The Phase Lock Loop controller includes channels for introducing phase angle (proportional) feedback and frequency (integral) feedback. At the sub-system level, minor modifications based on the choice of the feedback error signals make the converter station into either the *DC Voltage Regulator* or the *Power Dispatcher*, which are the two building blocks of the Voltage-Source PWM-HVDC Transmission System.

## **PART II CHAPTERS 5 and 6**

### **1.3.4 Tri-Logic PWM – Theory**

The Tri-Logic PWM theory is at such an early stage of its development that the existing methods are the Static Type.

**Chapter 5** presents the first definitive Dynamic Type [78]. It is based on a linear transformation of the Bi-Logic PWM signals. Since the specific Bi-Logic PWM is the Dynamic Type, Sinusoidal PWM, it follows that the Tri-Logic PWM is also a Dynamic Type. **Chapter 5** also presents a *Decoupler Pre-Processor* stage, which enables the output signals of the Tri-Logic PWM to be considered as three decoupled linear amplifier outputs, one for each of the three phases.

As all the transformations are linear operations, all the harmonic properties can be predicated from those of the Sinusoidal PWM.

### 1.3.5 Tri-Logic PWM – Application

The Dynamic Tri-Logic PWM is applied to the realization of the 3-phase, 6-valve, current-source PWM rectifier [73], in **Chapter 6**. The rectifier requires the "linear amplifier capability" of the Dynamic Tri-Logic PWM because it has a feedforward path to implement unity power factor operation, an outer feedback loop for dc current regulation and inner feedback loops for active filtering and fast response performance.

### 1.3.6 Tri-Logic PWM - Implementation

An important goal of the research is to implement digitally,

- (a) the Dynamic Type Tri-Logic PWM strategy and the Decoupler Pre-Processor,
- (b) the feedforward and the feedback controls of the Current-Source PWM rectifier.

The hardware components are the 6-valves (Bipolar transistors), their base drives, the associated snubbers, the ac capacitors, the dc inductor of the Current-Source PWM Bridge Converter.

The additional hardware of the controls are:

- (i) Programmable Array Logic (PAL) chips, whose outputs are the logic

commands of the base drives and whose inputs come from a multi-DSP platform.

- (ii) a multi-DSP platform consisting of three Digital Signal Processors (Texas Instrument TMS320C25s) capable of concurrent computation. This multi-DSP platform has been built by a colleague and Ph.D. candidate Ms. Y. Guo.

From the assembly of hardware components, the goal is to use software programming to realize a versatile range of performance characteristics.

The experiences sought in the research work are:

- (1) programming of the PAL chips to implement the Dynamic Tri-Logic PWM and the Decoupler Pre-Processor. The details are described in **Appendix B**.
- (2) real-time programming of the Multi-DSP platform to control the hardware as a Current-Source PWM Rectifier. (see **Chapter 6**)
- (3) implementation of a "pole-placement" strategy in real time for fast response and active filtering. (see **Chapter 6**)

The implementation has also given opportunity for the exploration of an innovative feedback scheme which has been proved experimentally as very promising in **Chapter 6**.

## PWM-HVDC TRANSMISSION SYSTEM

### 2.1 Introduction

There are three attributes in the sinusoidal waveform:

- (1) the frequency,
- (2) the phase angle,
- (3) the amplitude.

When the waveform consists of two levels ( $+1$ ,  $-1$ ), the three attributes are encoded in the pulse widths. So far, the *Pulse Width Modulation* (PWM) concepts, as exploited in Power Electronics, have been concentrated on only two of the three attributes, namely: frequency and amplitude. This is a reflection of the industrial interests in perfecting the variable frequency inverter for variable speed ac motor drives [11].

This chapter is concerned with the contributing to the advances of PWM methodology by demonstrating how all the three attributes can be brought to bear to solve significant engineering problems. The application example chosen here is the *High Voltage Direct Current* (HVDC) Transmission. In including the third attribute, namely: phase angle, into consideration, one needs to be reminded that it is not an entirely independent quantity. This is because the angle is the time integral of the frequency. Also, the phase angle has meaning only in the context of a reference sinusoidal waveform at a common frequency. Thus, the pulsed waveform must be synchronized to the common frequency so that the phase angle can be varied with respect to the reference.

The discussion of the three attributes of the sine wave brings to mind the turbo-generator stations which have to be synchronized to the utility system. Once in synchronism, the Governor-Frequency control shifts the voltage-angle in meeting the power demands [79]. The Field Exciter System adjusts the voltage amplitude in meeting the reactive power demands [79].

This reminder suggests that if the converter stations of the HVDC transmissions can operate with PWM and if PWM can control the frequency and the phase angle, then the real power can be controlled in the same manner as by the turbo-generator stations. As a matter of fact, the power electronic control response would be much faster than the sluggish Governor and Field Exciter controllers [80].

The generator voltage of the turbo-generator is an "active" voltage induced by the rotation of the magnetic flux from the field excitation. The ac voltage of the voltage-source PWM-HVDC converter station is likewise "active" in the sense that it is supported by the dc link voltage. The dc link voltage comes from the electric charge residing across the dc link capacitances. In fact, at least one of the voltage-source PWM-HVDC converter stations is assigned the function of regulating the dc voltage and is the DC Voltage Regulator of Section 2.4.2. Starting from the high quality regulated dc voltage source, the switching of the converter valves using the *Sinusoidal Pulse Width Modulation* (SPWM) strategy assures that the ac voltage is also a high quality ac active voltage.

Just as the field excitation control can be used to vary the ac voltage amplitude of the generator, the amplitude control of the SPWM strategy can be used by the PWM-HVDC converter station in its ac voltage amplitude control. In both situations, the amplitude controls the reactive power. As amplitude control in the SPWM strategy is already well known, this thesis focuses on the phase angle and the frequency control.

The PWM-HVDC converter station is capable of bi-directional power transfer. To complete the analogy, it is worth while mentioning that although in general, the turbo-generator stations are ac power sources only, in the pump-storage application they are also capable of bi-directional power transfer, using Kaplan turbines as reversible "prime-mover" power [79]. The "prime-mover"

power in the PWM-HVDC converter is the dc power. When the voltage-source PWM-HVDC converter station operates as a rectifier/inverter, the ac power is converted to/from the dc power.

The all important characteristic of the voltage-source converter is that the dc voltage is unidirectional so that the bi-directional power reversibility appears as the reversal in the direction of the dc current flow. This property makes the voltage-source PWM-HVDC converters ideally suited for multi-terminal connections as the converter stations can be connected in parallel at their dc sides.

This Chapter is organized as follows:

Section 2.2 describes the voltage-source converter and shows how the dc link voltage produces on the ac side terminals, pulsed voltage waveforms, whose fundamental Fourier Series harmonic are analogous to the generator voltages.

Section 2.3 describes the implementation of the controls of: (1) the frequency, (2) the phase angle and (3) the amplitude of the SPWM.

Section 2.4 describes the feedback control configurations required to make the voltage-source PWM-HVDC converter stations into two basic types of stations in a HVDC system. They are: (1) the DC Voltage Regulator and (2) the Power Dispatcher.

Section 2.5 describes the multi-terminal application in which the voltage-source topology has distinct advantage because each station requires local control only.

## 2.2 Force-Commutated Voltage-Source Converter Bridge

In the present HVDC transmission system, the converter station consisting of the Graetz bridge [2] mentioned in Chapter 1, depends on line-commutation principle which requires an external ac voltage source, typically the ac utility line, for the negative ac voltage to drive the commutation process. The thyristor valve, like its mercury-arc predecessor, can be turned on with a delay phase angle. It is properly turned off only after its current has fallen to zero with reverse bias voltage across its anode-cathode. Thus the valve switching frequency is constrained by the ac line supply. Near square waveform currents at the same line frequency are drawn from the ac line sources under lagging power factor. The improvement of line harmonics and power factor requires expensive filters. In weak ac systems, the back-to-back rectifier/inverter stations may have to be supplied with leading reactive power. The controls may require additional static VAR compensator [64-68].

The above inconveniences can be removed by employing force-commutation of the thyristors or semiconductor switch devices with gate turn-off capability, such as the GTO (*gate-turn-off thyristor*), which provides one more degree of freedom in control to overcome the limitations in the existing converter station. The force-commutation technique permits the valves of converter to be turned ON and OFF many times during each cycle of the ac line supply. The external ac source voltage is no longer necessary for the proper switching



operations.

Fig. 2-1 shows a simplified circuit diagram of the 3-phase, voltage-source (boost) type PWM converter bridge which is proposed here as the basic model of the new PWM-HVDC converter station in this thesis. In Fig. 2-1, the force-commutated semi-conductor valve is represented by the boxed "V" with the arrow-head of "V" indicating the direction of valve current flow. Each valve has an anti-parallel diode. The inductances,  $L$ , on the ac side are important because they contribute to the "boost" action which enables rectification to take place. The

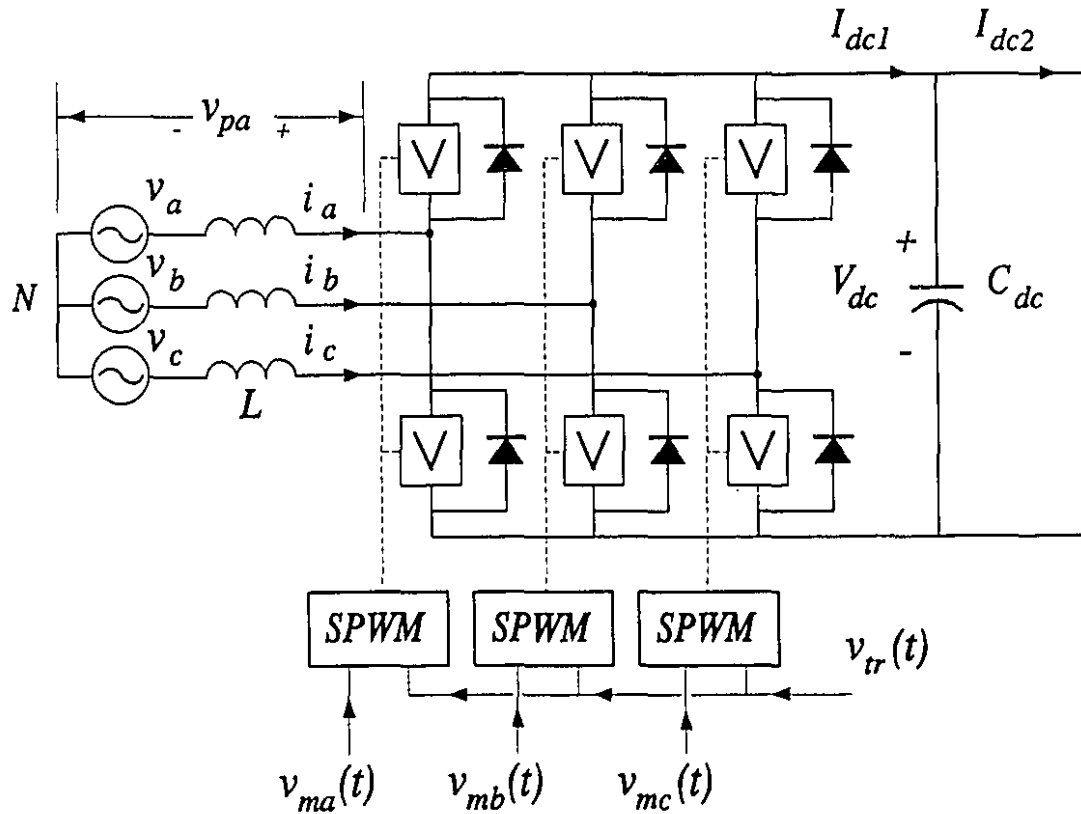


Figure 2-1 Simplified circuit topology of 3-phase, voltage-source, boost type PWM-HVDC converter bridge.

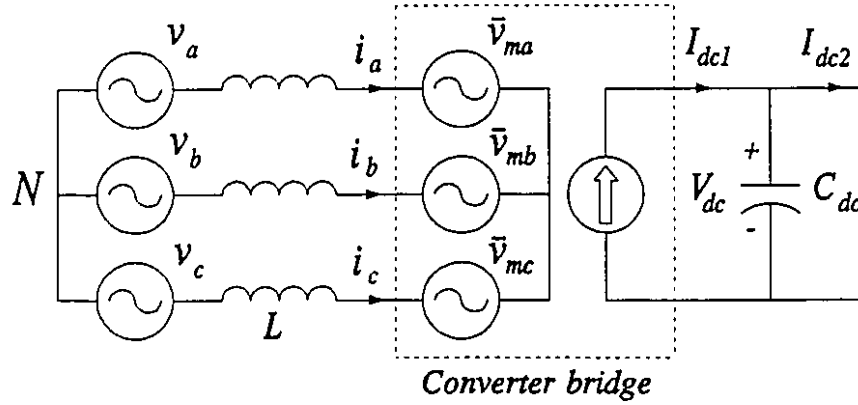


Figure 2-2 The equivalent circuit of voltage-source PWM converter.

power from the ac side is first converted to magnetic energy in the inductances during the ON states of the valves. When the valves are turned OFF, the  $Ldi/dt$  voltages of the inductances cause the anti-parallel diodes on the opposite side of the branches to conduct, thus admitting the stored magnetic energy to the dc side.

The converter operates with a unidirectional dc link voltage,  $V_{dc}$ , across on the dc capacitor,  $C_{dc}$ . For proper switching operation, the voltage  $V_{dc}$  should be kept large enough to ensure that all the anti-parallel diodes are normally reversed biased and conduction occurs only through the "boost" action [32,37]. The change of the direction of power flow is achieved by the reversal of the direction of the local average dc link current,  $I_{dc1}$ . The converter station is viewed as a current source from the dc side, shown by the equivalent circuit of Fig. 2-2.

Compared with the line-commutation technique, the following significant

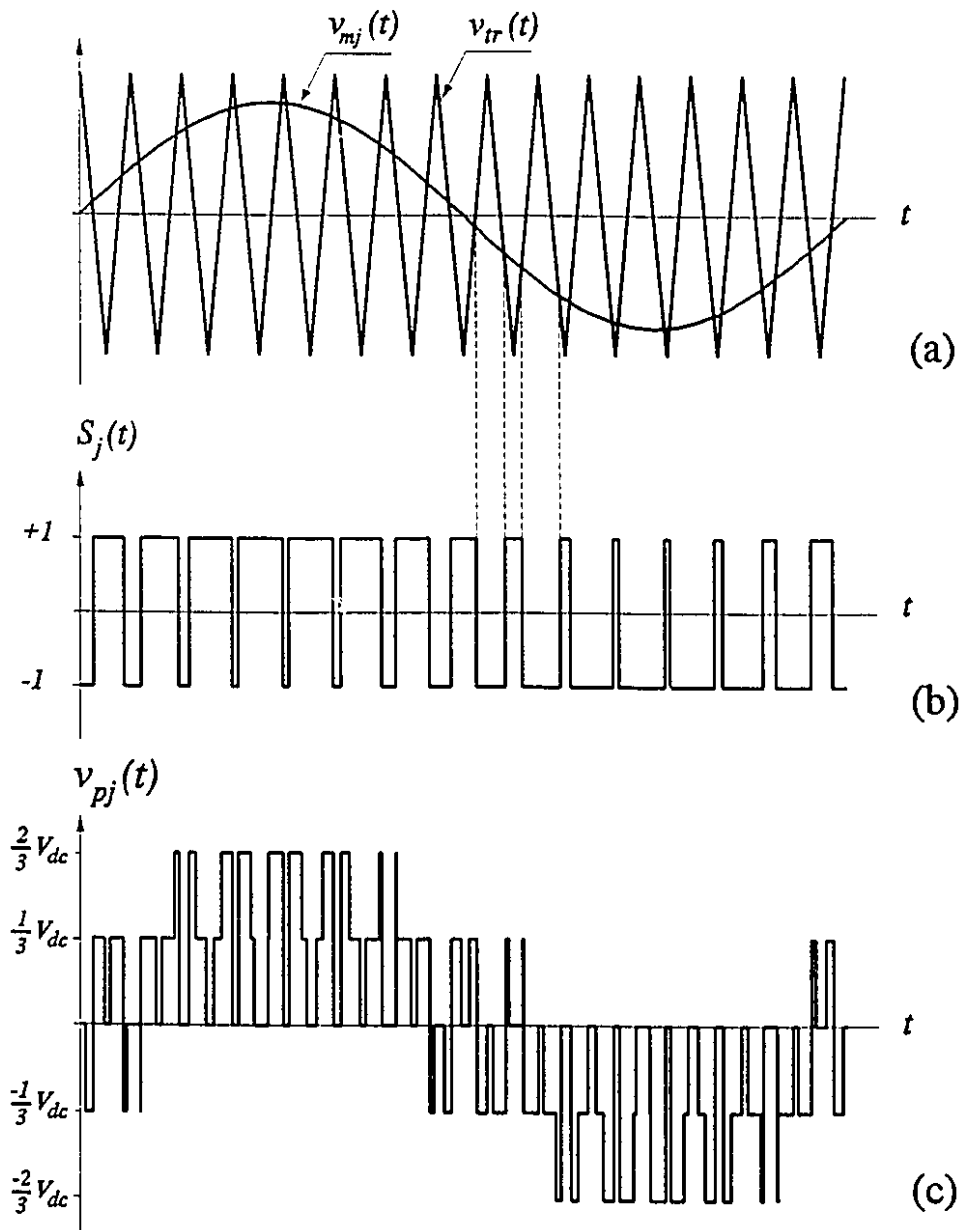
features in the force-commutated voltage-source PWM converter station are worthy of note:

- (i) The ac fundamental terminal voltage  $\bar{v}_{pf}(t)$  is an active voltage supported by the dc link voltage. This contrasts sharply with the conventional HVDC which does not provide active ac voltage support at their terminals. Thus in the case where the ac transmission line is long, the voltage drop across the large line impedance results in severe voltage droop at the conventional HVDC terminal.
- (ii) The power factor angle can be varied over the  $360^\circ$  range [32,35]. Operation with unity power factor, even leading power factor is not a problem.
- (iii) The PWM technique suppresses low order harmonics ac currents. The residual harmonics are in the high frequency end of the spectrum where harmonic filters for them are relatively cheap. The dc output current,  $I_{dcl}$ , consists of high frequency pulses which can be filtered out efficiently by the dc link capacitor,  $C_{dc}$ . As the current pulses are at high frequencies the capacitor required for filters is relatively cheap. The problem regards to telephone interference of the dc transmission line may not be serious.
- (iv) On the dc link side, the converter station operates with a unidirectional voltage, power reversal is accomplished by reversal in the direction of dc link current flow. This property favours parallel connection of several converter stations across a dc bus.

### 2.2.1 Switching Function $S_j$

By choosing the switching ON-OFF durations to follow some particular timing pattern, one can control the fundamental and the harmonic components of the ac terminal pulse waveform voltages. Many different kinds of switching control methods have been applied to generate the switching timing pattern [22]. As mentioned before, the Two-Level or Bi-Logic Sinusoidal PWM (SPWM) strategy [23] has been selected here. Fig. 2-3(a) shows the conventional technique of generating SPWM switching control signal using a triangular carrier waveform  $v_{tr}(t)$  and a sinusoidal modulating signal  $v_{mj}(t)$  ( $j=a, b, c$  for the three phases). The intersection points of the two waveforms are used as the instants for sending the ON-OFF gating signals to the Upper and the Lower valves on one of the branches of the 3-phase bridge.

When the modulating signal is higher than the triangular carrier, the switching function  $S_j$  is defined as  $S_j = +1$  in Fig. 2-3(b), and gating signal is sent to the Upper Valve so that the Upper Valve or Diode is conducting. Similarly, when the modulating signal is lower than the triangular carrier, corresponding to the switching function  $S_j = -1$ , the Lower valve or diode will be conducting. Each branch has only TWO possible conducting states. Fig. 2-3(c) shows the terminal voltage waveforms,  $v_{pj}(t)$ , with respect to the neutral point  $N$ . It can be expressed as a function of the dc link voltage,  $V_{dc}(t)$ , and the three phase switching functions,  $S_j(t)$ :



**Figure 2-3** (a) Sinusoidal PWM strategy.  
 (b) Switching function.  
 (c) Line-to-neutral ac terminal pulse waveform voltage.

$$v_{pj}(t) = \frac{1}{6} \left( 3 S_j(t) - \sum_k^{a,b,c} S_k(t) \right) V_{dc}(t) , \quad j = a, b, c \quad (2.1)$$

Note that  $S_k$  ( $k=a, b, c$ ) describe the switching states of the other valves in the other branches. Since the dc link voltage can be normally considered as constant, the fundamental Fourier Series component of the ac terminal voltage  $\bar{v}_{pj}(t)$  will be determined by the fundamental Fourier Series component of the switching functions, which is linearly proportional to the magnitude of the sinusoidal modulating signal waveform  $v_{mj}(t)$ . It is well known [81] that for the case of balanced three phase sinusoidal modulating signals, the fundamental Fourier Series component of the pulsed voltage of the  $j$ th phase will be:

$$\bar{v}_{pj}(t) = 0.5 \frac{v_{mj}(t)}{V_r} V_{dc} , \quad j = a, b, c \quad (2.2)$$

$V_r$  is the peak value of the triangular carrier waveform. The important feature is that the ac fundamental terminal voltages,  $\bar{v}_{pj}(t)$ , have the same frequency and phase angle as the sinusoidal modulating signals  $v_{mj}(t)$ . Thus for constant  $V_r$  and  $V_{dc}$ , the voltages  $\bar{v}_{pj}(t)$  can be seen as the outputs of a 3-phase linear power amplifier with the modulating signals  $v_{mj}(t)$  as input signals.

As shown in Fig. 2-1, the blocks labelled "SPWM" handle the gating functions for the valves of the converter bridge with the input modulating signals of  $v_{ma}(t)$ ,  $v_{mb}(t)$  and  $v_{mc}(t)$ .

## 2.3 Control of Voltage-Source Type PWM-HVDC Converter Station

Based on the voltage-source type PWM converter bridge Fig. 2-1, Fig. 2-4 adds the control schematic by which the voltage amplitude, the frequency and the phase angle of the fundamental component of the ac terminal pulse waveform voltages can be fully adjusted by the three command signals  $\bar{v}_{mc}$ ,  $\omega_c$  and  $\theta_c$ , respectively.

In Fig. 2-4, the basic sinusoidal waveform templates of the three phases are stored in binary digits in the *A*, *B*, and *C Electronically Programmable Read Only Memories* (EPROM's). In the laboratory implementation, the angular period  $0-2\pi$  is divided into  $2^9=512$  segments. Corresponding to the binary address  $K$ , the  $K$ th memories of the *A*, *B*, and *C* EPROM's contain the values of  $\sin(2\pi[K/512])$ ,  $\sin(2\pi[(K/512)-(2/3)])$  and  $\sin(2\pi[(K/512)+(2/3)])$ , respectively. As the counter number (modulo 512) increases from  $K=0$  to  $K=511$ , the contents of the EPROM's are passed through the *Digital-to-Analog* (D/A) converters. Their analog outputs generate fine stepped approximations of the basic balanced 3-phase sinusoidal waveforms.

### 2.3.1 Voltage Amplitude Control

Since the dc link voltage  $V_{dc}$  is regulated at its constant reference value in the PWM-HVDC transmission system, based on Eq. (2.2), the amplitudes of the ac terminal voltages are adjusted by varying of the amplitudes of the modulating

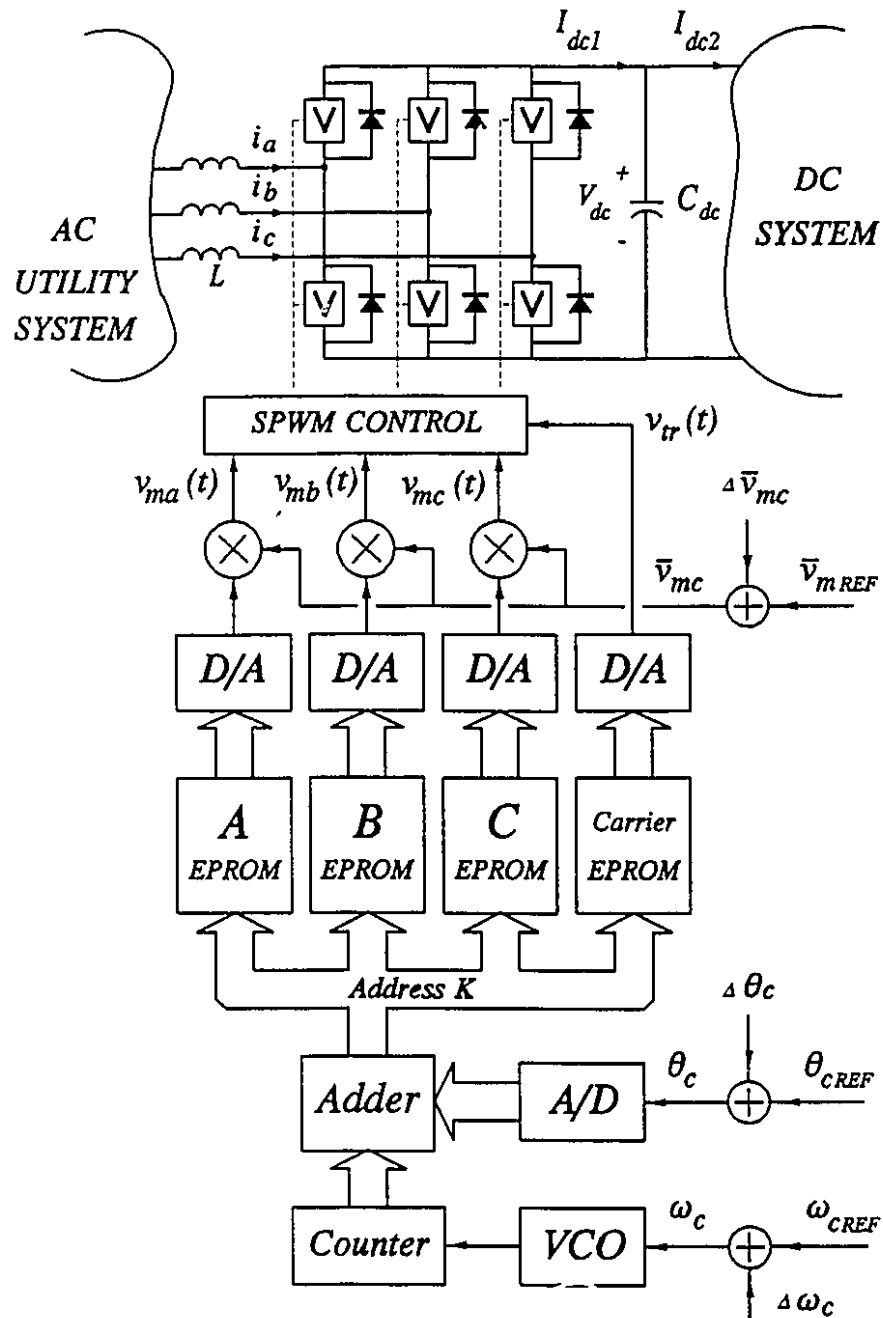


Figure 2-4 Schematic of voltage-source PWM-HVDC converter station with controls on voltage amplitude, frequency and phase angle.



signals in the SPWM functions. The amplitudes of the modulating sinusoidal signals are introduced by multiplying the outputs of the D/A converter from the  $A$ ,  $B$ , and  $C$  EPROM's by the amplitude command signal,  $\bar{v}_{mc}$ , through the electronic multipliers. The modulating waveforms are compared with the triangular carrier waveform which is also generated by the D/A output of the triangular carrier EPROM with a constant peak value. In the laboratory implementation, the carrier EPROM contains the discretized form of 18 isosceles triangles in the same period of 512 counts.

### 2.3.2 Frequency Control

The four EPROM's are addressed simultaneously by the number  $K$ . As shown in Fig. 2-4, the number  $K$  is the sum of two binary numbers. The binary number contained in the binary counter (modulo 512), receiving the pulse from the *Voltage Controlled Oscillator* (VCO), belongs to the channel in which the frequency is controlled. When the frequency command signal  $\omega_c$  increases or lowers the pulsing rate of the VCO, the basic sinusoidal waveforms generated by the EPROM's will be cycled at a higher or a lower frequency.

The PWM-HVDC converter station should be able to generate the voltage whose frequency is identical to that of the ac utility system in Fig. 2-4. The frequency control signal  $\omega_c$  provides this degree of independent control.

Since the address number  $K=0, 1, 2 \dots 511$ , corresponding to the period

$\theta=0-2\pi$  of the sinusoidal modulating signals, the counting rate of the number  $K$  is associated with the angular frequency  $\omega$ . The binary counter performs the function of an *integrator*. The phase angle  $\theta_m$  of the waveforms generated by the EPROM's of Fig. 2-4 is related to signal  $\omega_c$  by:

$$\theta_m(t) = \theta_m(0) + \int_0^t \omega_c(\tau) d\tau \quad (2.3)$$

To synchronize with the utility system, not only must the converter station have the same frequency, but it must also bear a constant voltage phase angle with respect to the Thevenin voltage equivalent representing the remainder of the utility. From Eq. (2.3), one sees that the frequency control  $\omega_c$  is an indirect controller by which the constant phase angle can be secured.

Fig. 2-5 illustrates the situation when the converter station and the utility system are initially synchronized, i.e., both initially have the same frequency  $\omega_c = \omega_{Tn}$  in Fig. 2-5(a) and the same voltage phase angle  $\theta_m = \theta_{Tn}$  in Fig. 2-5(b).  $\omega_{Tn}$  and  $\theta_{Tn}$  are the frequency and phase angle of the voltages of the utility system. The voltage phase angle graphs of Fig. 2-5(b) are essentially the integral of the frequency graphs of Fig. 2-5(a). One sees that by momentarily increasing or decreasing the frequency of the VCO, the voltage phase angle can be advanced or retarded with respect of the utility's. At the end of the jogging, the frequencies are identical and the voltage phase angle remains constant.

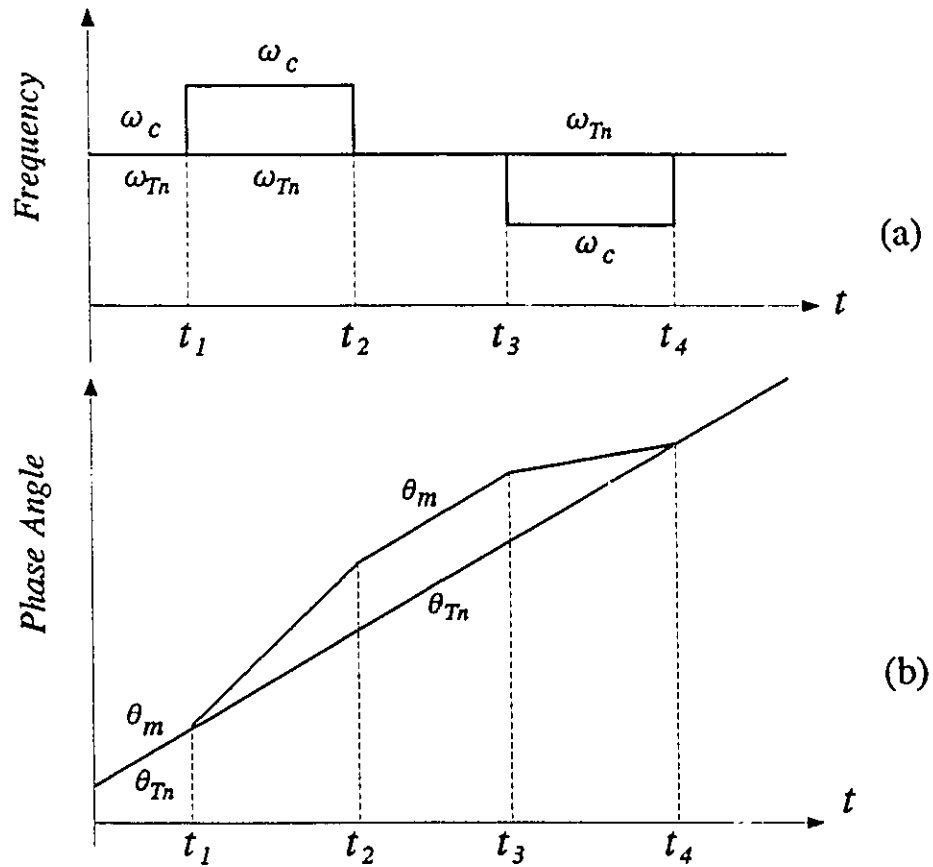


Figure 2-5 Illustration of integral voltage phase angle control by frequency jogging. (a) frequency versus time, (b) phase angle versus time.

### 2.3.3 Voltage Phase Angle Control

The other component of the binary address  $K$  in Fig. 2-4 comes from the direct phase angle shift control. The voltage phase angle shift command signal,  $\theta_c$ , is translated into binary number by an *Analog-to-Digital* (A/D) converter, then added to the contents of the binary counter of the VCO. A change in the address number  $K$  can be made proportionally to the signal  $\theta_c$ , thus providing a

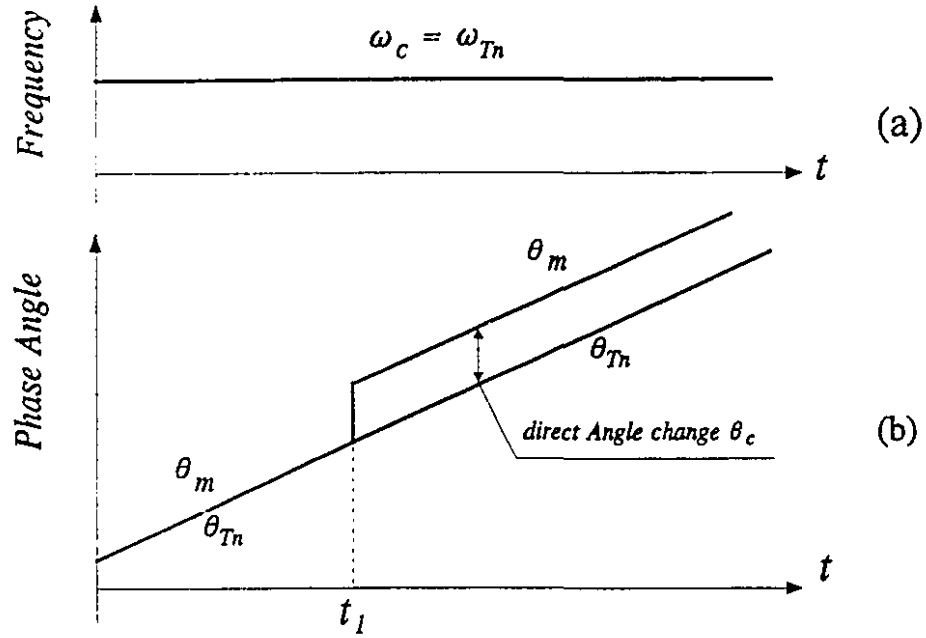


Figure 2-6 Illustration of proportional voltage phase angle control.

(a) frequency versus time, (b) phase angle versus time.

*proportional* control channel for the voltage phase angle regulation.

Fig. 2-6 illustrates the initial states of the converter station and the utility after synchronization. A step input  $\theta_c$  is then introduced in the converter while keeping  $\omega_c$  constant. The phase angle  $\theta_m$  of the sinusoidal waveforms generated by the EPROM's is shifted instantly. Together with Fig. 2-5, one sees that the  $\omega_c$  and  $\theta_c$  are two independent channels of integral and proportional controls for the phase angle  $\theta_m$ :

$$\theta_m(t) = \theta_c(t) + \theta_m(0) + \int_0^t \omega_c(\tau) d\tau \quad (2.4)$$

### 2.3.4 Control Input Settings

As shown in Fig. 2-4, each of the signal inputs to the voltage amplitude, the frequency and the phase angle controls, consists of a reference value setting terminal and an additional terminal by which a feedback signal can be added. The reference signals are  $\bar{v}_{mREF}$ ,  $\theta_{cREF}$  and  $\omega_{cREF}$  and the feedback signals are  $\Delta\bar{v}_m$ ,  $\Delta\theta_c$  and  $\Delta\omega_c$  so that:

$$\begin{aligned}\bar{v}_{mc} &= \bar{v}_{mREF} + \Delta v_{mc} \\ \omega_c &= \omega_{cREF} + \Delta\omega_c \\ \theta_c &= \theta_{cREF} + \Delta\theta_c\end{aligned}\tag{2.5}$$

$\bar{v}_{mREF}$  is the reference setting by which the amplitude of the fundamental terminal voltage of the converter station is adjusted so as to be equal to the utility line voltage.  $\omega_{cREF}$  is set at the nominal synchronizing frequency (60 or 50 Hz). Initially, the frequency difference is introduced through the terminal  $\Delta\omega_c$  to synchronize the converter station to the utility prior to closing the circuit breakers.  $\theta_{cREF}$  is initially set equal to zero. The synchronization condition is achieved through the amplitude and frequency adjustments. The circuit breakers are closed when the voltages across the breakers are zero. Once the circuit breakers are closed, the  $\Delta\theta_c$  and  $\Delta\omega_c$  terminals are used as the *Proportional* and *Integral* (P-I) feedback channels.

The 3 degrees of controllability over the ac terminal fundamental voltages provide the PWM-HVDC converter station with the same attributes of the

*Generator station* [79]. For example, the voltage phase angle can be used for real power control as is done by the *Automatic Governor System* [79]. The voltage amplitude can be used in reactive power control as is done by the *Field Excitation System* [80]. In addition, the duties of *Power System Stabilizer* [79] for dynamic enhancement can also be incorporated through the feedback terminals. In fact, the converter station should surpass the performance of the generation station because that it is not encumbered by the long time constants of the governor and field excitation systems.

## 2.4 Converter Station Regulation Scheme

Fig. 2-7 shows, on a single line diagram, the voltage-source PWM-HVDC converter station connected to an ac utility system which is represented by a

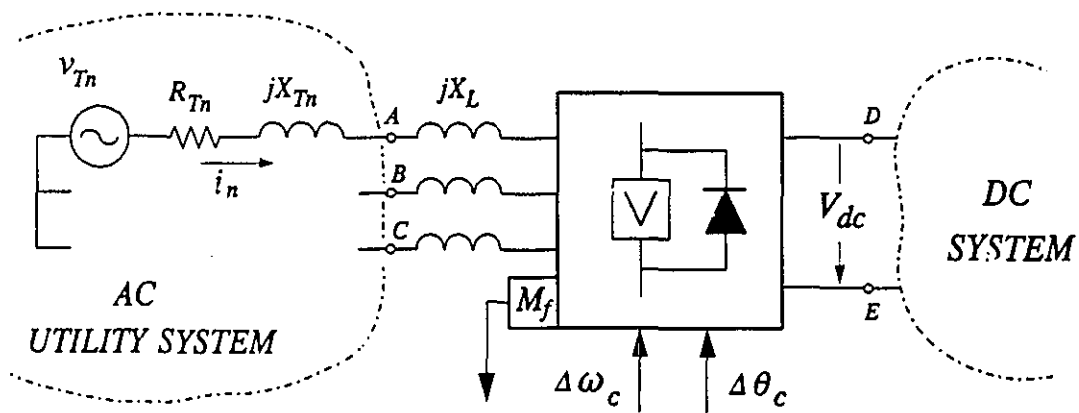


Figure 2-7 Voltage-source PWM-HVDC converter station connected to an ac utility system.

Thevenin equivalent voltage  $v_{Tn} \angle \theta_{Tn}$  and the Thevenin equivalent impedance  $R_{Tn} + jX_{Tn}$ . A black box with the control inputs  $\Delta\theta_c$  and  $\Delta\omega_c$  and a feedback measurement box labelled  $M_f$  is now used to represent the more detailed schematic of the PWM-HVDC converter station of Fig. 2-4. The ac terminals are  $A$ ,  $B$  and  $C$ , and the dc terminals are  $D$  and  $E$ . The impedance  $jX_L$  is the local inductance, i.e., the leakage inductances of transformer and some additional inductance, at the ac terminals of the PWM-HVDC converter station. As the  $R_{Tn}$  and the  $jX_L$  are usually very small compared to the  $jX_{Tn}$ , they are neglected to simplify the mathematical equations. It is assumed that the dc side has a sustained dc voltage  $V_{dc}$ , which as will be shown in Section 2.4.2, will be regulated.

Because of the large inductive reactance in the utility circuits, the real power transferred by the converter station is must effectively handled through varying the voltage phase angle  $\theta_n = \theta_{Tn} - \theta_m$ , while keeping the ac terminal voltage amplitude  $\bar{v}_{pj}$  constant by simply fixing the reference setting  $\bar{v}_{mREF}$ . This is illustrated through the phasor diagram of Fig. 2-8, where the voltage amplitude of the PWM-HVDC converter station  $\bar{v}_{pj}$  is made equal to the amplitude of the Thevenin voltage  $|v_{Tn}|$ . Assuming  $R_{Tn} = 0$  and  $jX_L = 0$ , the voltage drop  $jX_{Tn}|i_n|$  is the closing side of the voltage triangle subtended by the phase angle  $\theta_n$ . The current  $i_n$  makes an angle  $\theta_n/2$  between the two voltage phasors. It is well known that the power transferred and subsequently converted from ac to dc is:

$$P = \frac{3 |v_{Tn}| |\bar{v}_{pj}|}{X_{Tn}} \sin(\theta_{Tn} - \theta_m) \quad (2.6)$$

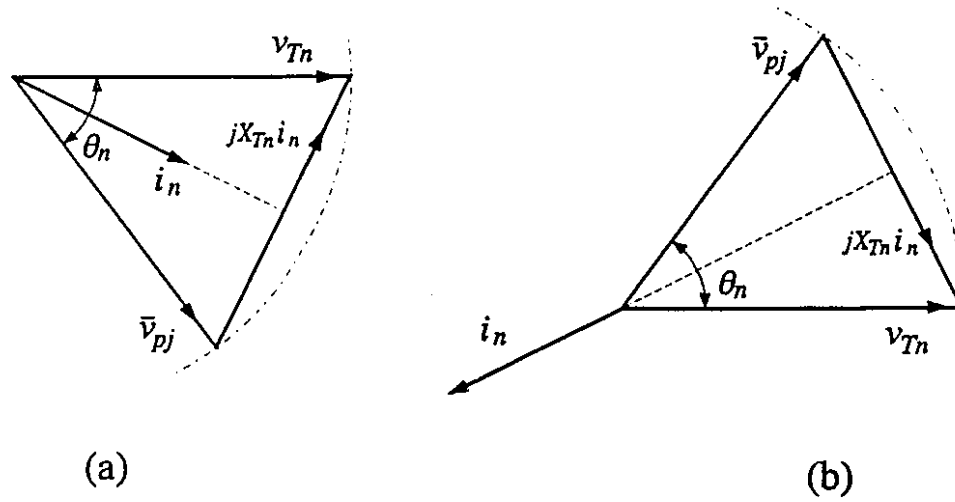


Figure 2-8 Phasor diagram of Fig.2-7. (a) rectifier operation, (b) inverter operation.

Thus the power can be simply regulated by varying the voltage phase angle  $\theta_m$ . Figs. 2-8(a) and (b) show that for negative and positive values of  $\theta_n = \theta_{Tn} - \theta_m$ , the PWM-HVDC converter station is operating as a rectifier and an inverter respectively.

Because the ac utility system is an integrated pool of a large number of generator stations and loads which are changing dynamically,  $v_{Tn} \angle \theta_{Tn}$  and the Thevenin equivalent impedance are fluctuating in time. Although the frequency reference setting is assigned at the standard 50 or 60 Hz, there is a slow and very small but finite drift. In addition, the VCO characteristics and the tolerances in the circuit component parts in the schematic of Fig. 2-4 are also prone to drift.



### 2.4.1 Voltage Phase Angle Lock Loop

In order for the PWM-HVDC converter station to operate in a dynamic environment of fluctuating frequency and voltage phase angle of the utility system, it must have a *Voltage Phase Angle Lock Loop* (PLL) which ensure that the ac system and the dc system will hang together. Negative feedback is a classical method of designing against sub-system fluctuations and drifts. The design philosophy is based on using the voltage phase angle to control the real power. As has been mentioned previously, the voltage phase angle can be controlled directly through  $\theta_c$  and indirectly after integration through  $\omega_c$ . Thus the terminals  $\Delta\theta_c$  and  $\Delta\omega_c$  in Fig. 2-4 will be used for introducing the proportional feedback and integral feedback respectively. Based on the design objective, the feedback loops can be configured to make the converter station into either a power dispatcher or a dc voltage regulator.

### 2.4.2 DC Voltage Regulator

It has been tacitly assumed previously that the dc link voltage  $V_{dc}$  exists which is obtained by charging the dc capacitor,  $C_{dc}$ , connected on the dc link in Fig. 2-4. It is because the dc link voltage exists, that the active ac terminal voltage  $v_{pj}(t)$  is supported and guaranteed. For this reason, at least one of the PWM-HVDC converter stations connected on the dc link has to be assigned to the function of *DC Voltage Regulator* (VR).

From Fig. 2-4, the capacitor charging current is:

$$C_{dc} \frac{d}{dt} V_{dc}(t) = I_{dc1}(t) - I_{dc2}(t) \quad (2.7)$$

where  $I_{dc2}(t)$  is the dc load current and  $I_{dc1}(t)$  is the dc pulse waveform output current of the PWM-HVDC converter station. Integrating this equation:

$$V_{dc}(t) = V_{dc}(0) + \frac{1}{C_{dc}} \int_0^t (I_{dc1}(\tau) - I_{dc2}(\tau)) d\tau \quad (2.8)$$

where  $V_{dc}(0)$  is the voltage evaluated at  $t=0$ , due to charging from an earlier period:

$$V_{dc}(0) = \frac{1}{C_{dc}} \int_{-\infty}^0 (I_{dc1}(t) - I_{dc2}(t)) dt \quad (2.9)$$

The dc voltage regulation loop is shown in Fig. 2-9(a). It is based on measuring the dc link voltage  $V_{dc}(t)$  and after comparing it with the voltage reference  $V_{dcREF}$ , the error:

$$\epsilon_{V_{dc}}(t) = V_{dcREF} - V_{dc}(t) \quad (2.10)$$

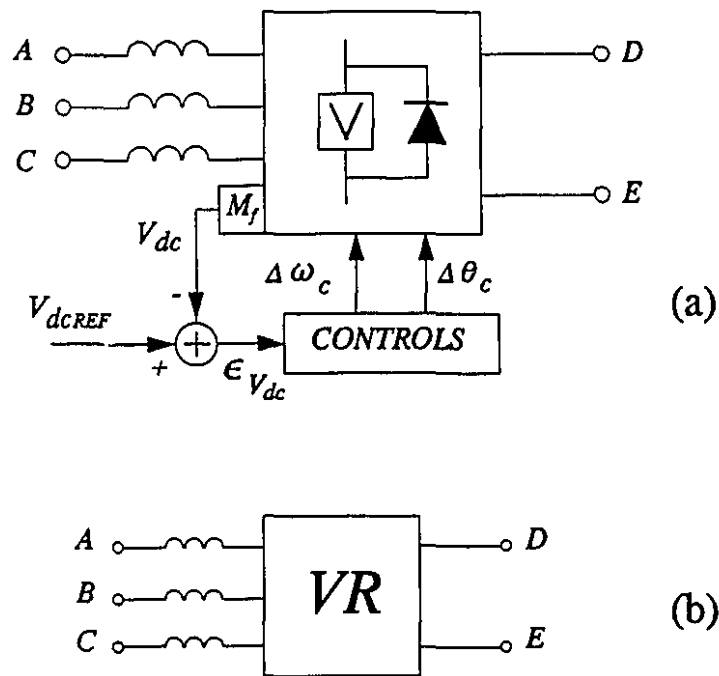
is used as a negative feedback signal to control the voltage phase angle directly and indirectly through the inputs  $\Delta\theta_c$  and  $\Delta\omega_c$  so as to null the error  $\epsilon_{V_{dc}}(t)$ .

In order to maintain the dc link voltage at the constant reference value  $V_{dcREF}$ , it is required that the DC Voltage Regulator has to be able to convert the same amount of real power to replace the power which has been drained by other converter stations placed across the dc link so as to ensure that the local average

current  $I_{dc1}$  is balanced with the load current  $I_{dc2}$  :

$$I_{dc1} = I_{dc2} \quad (2.11)$$

This means that the phase angle of the ac terminal voltage  $\theta_m$  is adjusted by the negative feedback until the power from the ac utility satisfies the power demand  $V_{dc}I_{dc2}$ , so that the charge across the dc link capacitor is remains constant at the desired level. Otherwise the dc link capacitor would be overcharged or discharged. The ac power converted to dc power (or vice versa) is always just sufficient to make up for the dc output power leaving (or entering) the dc terminals. Thus when the PWM converter station is made into a DC Voltage



**Figure 2-9** (a) Schematic of DC Voltage Regulator (VR), (b) block diagram representation of (a).

Regulator, it is automatically a power slack. The right amount of ac power is converted by the DC Voltage Regulator to satisfy the power requirements of other converter stations connected on the dc link. When all the other converter stations are assigned to rectifier function, the DC Voltage Regulator automatically assumes its role of an inverter.

### 2.4.3 Power Dispatcher

Fig. 2-10(a) shows the feedback loop configuration for the implementation of a *Power Dispatcher* (DISP). The converter station is assigned the duty of

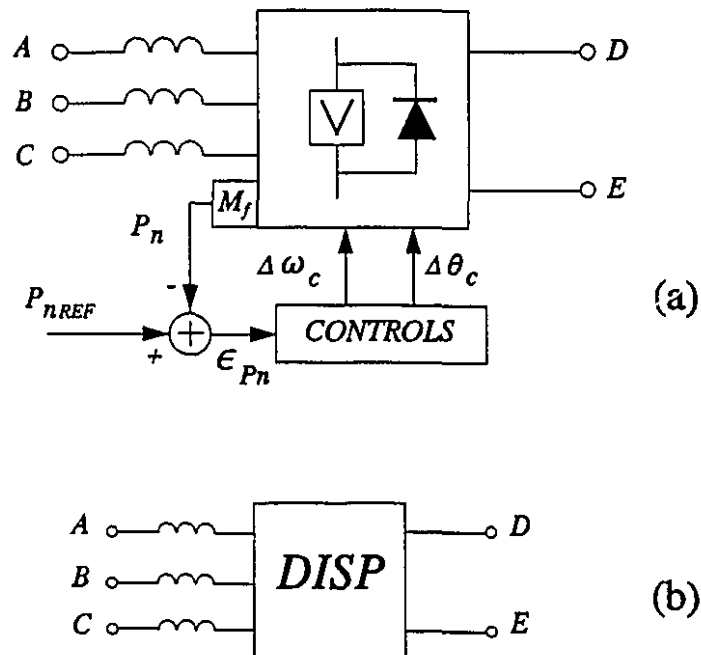


Figure 2-10 (a) Schematic of Power Dispatcher (DISP), (b) block diagram representation of (a).

converting a fixed amount of real power,  $P_{nREF}$ . Rectifier or inverter role is designated by the positive or negative sign in  $P_{nREF}$ . The real power  $P_n$  passing through the converter station is measured by the transducer of box  $M_f$  in Fig. 2-10(a) and after comparing it with the reference, the error:

$$\epsilon_{Pn} = P_{nREF} - P_n \quad (2.12)$$

is used as a negative feedback signal to the proportional input of  $\Delta\theta_c$  and the integral input of  $\Delta\omega_c$  to increase or to decrease the terminal voltage phase angle  $\theta_m$  until the error  $\epsilon_{Pn}$  is nulled.

During the power regulation, the dc link voltage is kept at desired level by the DC Voltage Regulator mentioned above. As in the DC Voltage Regulator, the Power Dispatcher is regulated by changing the voltage phase angle only while keeping the terminal voltage amplitude constant.

As the frequency reference setting  $\omega_{cREF}$  is set near to the 60 or 50 Hz of the ac utility system, the feedback loop in the Power Dispatcher of Fig. 2-10(a) or the DC Voltage Regulator of Fig. 2-9(a) automatically locks the frequency of the converter station to that of the ac system. This is because the VCO (*Voltage Controlled Oscillator*) in the feedback loop tracks the system frequency through the voltage phase angle lock loop (PLL) action.

## 2.5 Multi-Terminal PWM-HVDC Transmission System

Since the voltage-source type PWM converter stations maintain unidirectional voltage in the face of bidirectional power flow, their dc terminals can be connected in parallel to a pair of voltage buses to form a multi-terminal dc network. Based on the feedback control configurations of Sections 2.4.2 and 2.4.3, two building blocks:

- (1) the DC Voltage Regulator (VR) in Fig. 2-9(b),
- (2) the Power Dispatcher (DISP) in Fig. 2-10(b),

are used to construct a multi-terminal HVDC system, as in the example shown in Fig. 2-11. The *D* and *E* terminals of the PWM converter stations are connected in parallel to a dc grid. A number of ac utility system can be integrated through the dc grid. As illustrated in Fig. 2-11, four ac systems (which may be at different frequencies) are interconnected by the dc grid through five converter stations. The ac system ("Z") is integrated at two points through stations #4 and #5.

The dc link voltage is regulated by the DC Voltage Regulator (*VR*), station #1. Since the dc link voltage is the sine-qua-non of the system, any short circuit fault across the dc lines must be isolated by the circuit breakers. The strong point in this multi-terminal system is that, in Fig. 2-11, each of the converter stations can invert or rectify power. The two building blocks, the Power Dispatcher and the DC Voltage Regulator, enable inter-system power exchanges, requiring only

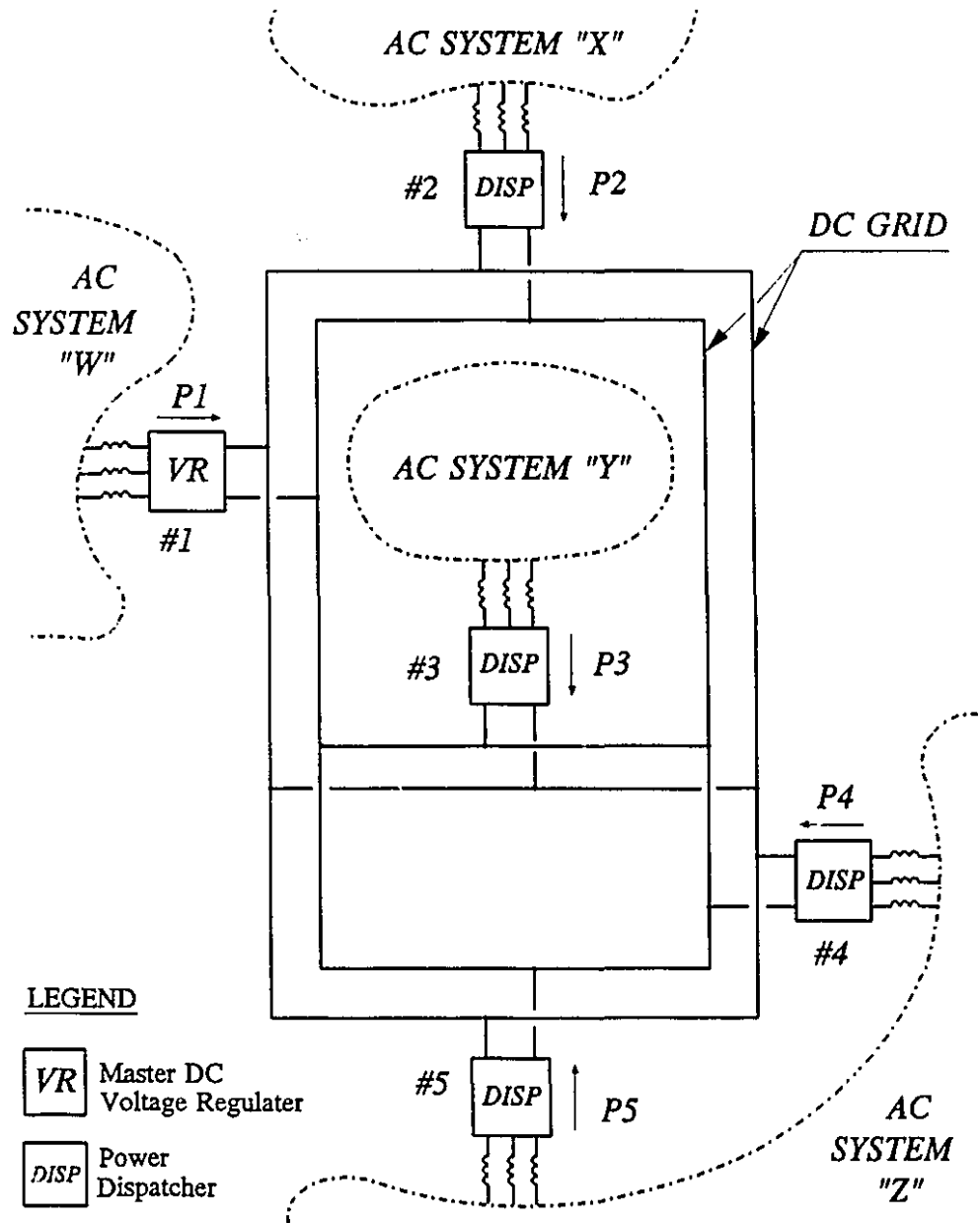


Figure 2-11 Multi-area ac system united by a dc grid through parallel connections of DISP and VR.

the local controls of the feedback loops discussed in Sections 2.4.2 and 2.4.3.

Converter stations #2, #3, #4 and #5 in the example of Fig. 2-11 are Power Dispatcher units. It is assumed that ac systems "X", "Y", and "Z" have decided to sell or purchase fixed schedules of power  $P_2$ ,  $P_3$ ,  $P_4$  and  $P_5$  at these converter stations. Rectification or inversion are respectively represented by the positive or negative sign in the power designation.

The four ac systems "W", "X", "Y" and "Z" can exchange power through the five converter stations through the dc grid. The power balance (neglecting ohmic losses) is always satisfied:

$$P_1 + P_2 + P_3 + P_4 + P_5 = 0 \quad (2.13)$$

As already mentioned, the DC Voltage Regulator is a power slack. In maintaining the assigned reference voltage, it delivers (as a rectifier) or absorbs (as an inverter) the left-over power of the other stations in the grid, so that Eq. (2.13) is satisfied at all times.

The dc voltages at the  $D$  and  $E$  terminals of the Power Dispatchers, differ from those of the DC Voltage Regulator by the voltage drops across the dc line resistances. The capacitors across the  $D$  and  $E$  terminals of each DISP station filter out the current ripples. The charge across the capacitor of each DISP station also supports the dc voltage which through the PWM switching of the valves becomes the active 3-phase voltages on the ac terminals of the converter station.



## 2.6 Summary

A new PWM-HVDC transmission system has been presented in this chapter. It is based on the voltage-source (boost) type PWM converter station with a control scheme which incorporates the voltage phase angle lock loop (PLL) technique.

On the ac side, the PWM-HVDC converter station has direct and independent control over the fundamental Fourier Series component of its ac line voltages as regards to the amplitude, the phase angle and the frequency. This enables the converter station to interact with the utility system in the same way as a generator station. On the dc side, the PWM converter stations are connected in parallel. Through simple local PLL feedback control, the converter station is made into one of two building blocks: either as a Power Dispatcher (DISP) or as a DC Voltage Regulator (VR). The local feedback is sufficient to co-ordinate HVDC power assignments.

The next chapter will present experimental results from  $1\text{-kVA}$  size laboratory models which show that the concepts of the PWM-HVDC transmission system are realizable and that the characteristics are worthy of attention.

It should be pointed out that this thesis has focused on the voltage phase angle control only. In consequence, Part I has been preoccupied with the management of the real power. In the power utility environment, the voltage

amplitude control is important for the management of the reactive power. While reactive power control is a subject for research, it has not been pursued because this thesis is concerned with Advances in PWM Techniques.

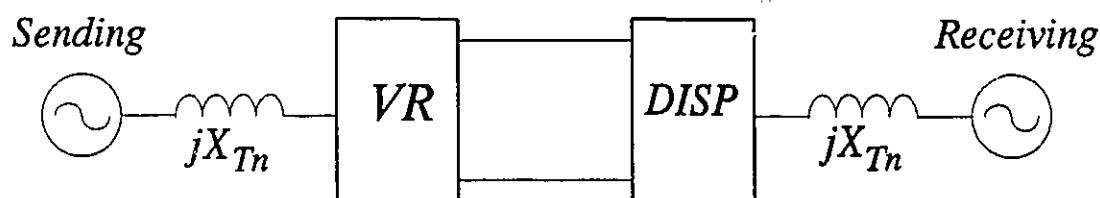
## **EXPERIMENTAL TESTS OF PWM-HVDC**

### **3.1 Introduction**

In the previous chapter, the concepts of the multi-terminal HVDC transmission system based on the voltage-source type PWM converter station have been presented. This chapter describes the experimental work which have been pursued to demonstrate that these concepts of the PWM-HVDC transmission system are technically sound and that the voltage-source (boost) type PWM converters have certain operational characteristics which are impossible to achieve in the conventional line-commutated thyristor HVDC transmission system.

The tests were performed on two identical  $1\text{-kVA}$  size, bipolar transistor laboratory models of the voltage-source type PWM converter bridges, each of which was fitted with the controls of Fig. 2-4 in Chapter 2. One converter had

the feedback of Fig. 2-9 so that it operated as a DC Voltage Regulator (VR) and the other was made into a Power Dispatcher (DISP) of Fig. 2-10. The two units were connected as a back-to-back asynchronous tie at the mid-point of a transmission line between two 3-phase voltage sources as shown in Fig. 3-1. The transmission lines were represented by lumped impedances  $jX_{Tn}$ . The effect of the length of the transmission line was studied by varying the values of the inductive reactance  $jX_{Tn}$ . The dc link voltage was set at 110 Vdc by the reference control  $V_{dcREF}$ , in the DC Voltage Regulator. The power was varied by changing the power reference setting,  $P_{nREF}$ , in the Power Dispatcher.



**Figure 3-1** Single line diagram of back-to-back dc link consisting a DC Voltage Regulator (VR) and a Power Dispatcher (DISP) situated at mid-point of transmission line.

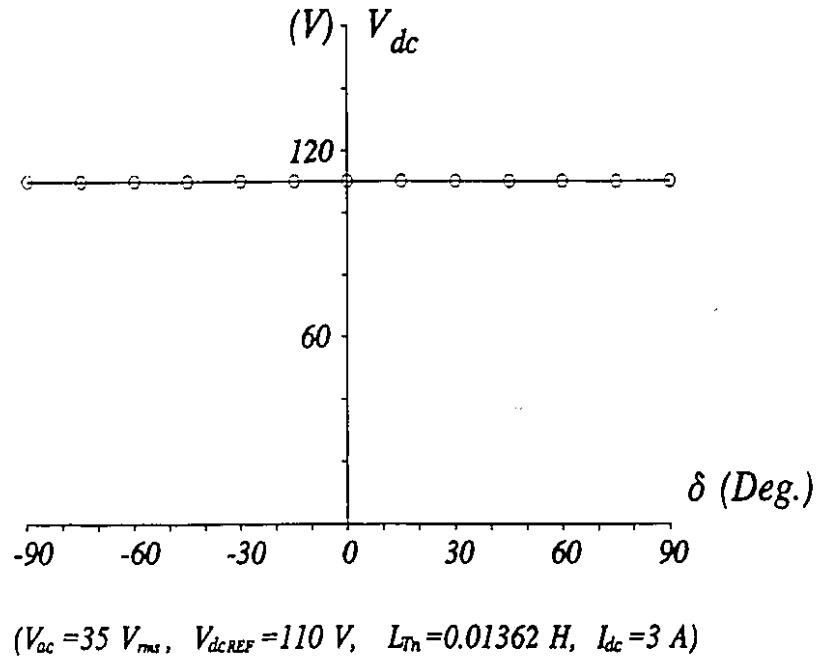
### 3.2 Synchronization Tests

The union of the converters in Fig. 3-1 to the ac sources is possible only when the voltage phase angle lock loop (involving VCO in Fig. 2-4) of each converter station makes its autonomous frequency synchronize with the frequency

of the ac utility system. The load and network topology changes in the ac utility system are modelled as variations in its Thevenin equivalent voltage and the Thevenin equivalent impedance at the ac terminals of the converter station. The voltage phase angle lock loops in Fig. 2-9 and Fig. 2-10 are intended to keep the converters synchronized in spite of the slow drifts in voltage phase angle and frequency.

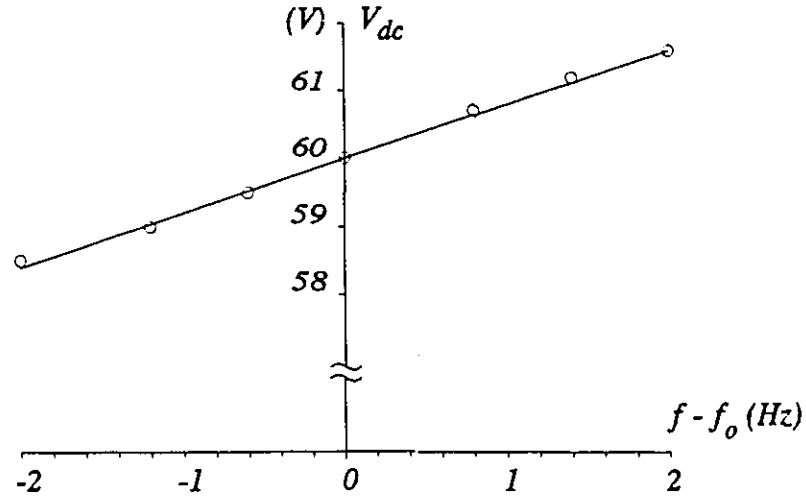
The voltage phase angle drift of the ac utility system was simulated by interposing a 3-phase phase-shifting transformer between the ac voltage source and the transmission line impedance  $jX_{Tn}$  in Fig. 3-1. Measurements of dc link voltage across the Voltage Regulator were plotted, shown in Fig. 3-2, against the phase angle drift,  $\delta$ , introduced by the phase shifting transformer. There was no change in  $V_{dc}$ . Similar results were obtained when the phase angle shifting transformer was transferred to the Power Dispatcher side. The power remained constant in spite of the voltage phase angle changes. Referring to Fig. 2-8, one concludes that when the phase angle of voltage  $v_{Tn}$  is changed the converter voltage  $v_{pj}$  will follow it in order to maintain a fixed phase angle  $\theta_n$ . This insensitivity to the voltage phase angle drift of the ac utility system is a property of the feedback through the frequency  $\omega_c$  channel which essentially is an integral feedback loop.

The effect of frequency deviation on the Power Dispatcher (DISP) and DC Voltage Regulator (VR) is depicted in Fig. 3-3 and Fig. 3-4 respectively. The



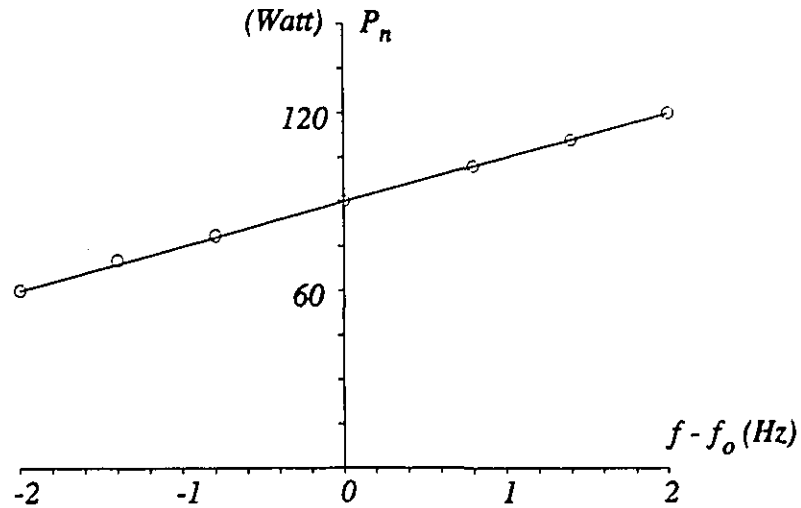
**Figure 3-2** DC link voltage of DC Voltage Regulator (VR) as a function of voltage phase angle  $\delta$  introduced by a phase shifting transformer between ac source and converter.

frequency deviation may arise from the gradual but minor drifts of the ac utility system or from the parameter changes with respect to temperature of the components in Fig. 2-4 itself. In the experimental tests, the utility's 60 Hz was unaltered. The frequency deviation was introduced by adjustment of the frequency reference setting,  $\omega_{cREF}$ , in Fig. 2-4. Fig. 3-3 and Fig. 3-4 show that when a frequency difference exists, the converter continues to remain synchronized by virtue of a non-zero feedback voltage  $\Delta\omega_c$ . This implies that the error in the regulator loop cannot be zero and this is confirmed by the sloped



( $V_{ac}=20 V_{rms}$ ,  $V_{dcREF}=60 V$ ,  $L_{Th}=0.01362 H$ ,  $I_{dc}=1.9 A$ ,  $K_p=0.2$ ,  $K_i=8.3$ )

Figure 3-3 DC link voltage of DC Voltage Regulator (VR) as a function of frequency deviation.



( $V_{ac}=20 V_{rms}$ ,  $V_{dcREF}=60 V$ ,  $L_{Th}=0.01362 H$ ,  $I_{dc}=1.5 A$ ,  $K_p=0.1$ ,  $K_i=25$ )

Figure 3-4 Power output of Power Dispatcher (DISP) as a function of frequency deviation.

straight lines in Fig. 3-3 and Fig. 3-4.

The  $K_p$  and  $K_i$  given in Fig. 3-3 and Fig. 3-4 are proportional and integral feedback gains in the  $\Delta\theta_c$  and  $\Delta\omega_c$  channels respectively.

### 3.3 Real Power Control

The DC Voltage Regulator was assigned a constant reference control voltage,  $V_{dcref}=110$  Vdc. The power was varied through the reference setting,  $P_{nREF}$ , of the Power Dispatcher. The dc power and the voltage phase angle were measured experimentally. Fig. 3-5 shows the dc link power plotted against the voltage phase angle of the DC Voltage Regulator. The theoretical lines are based

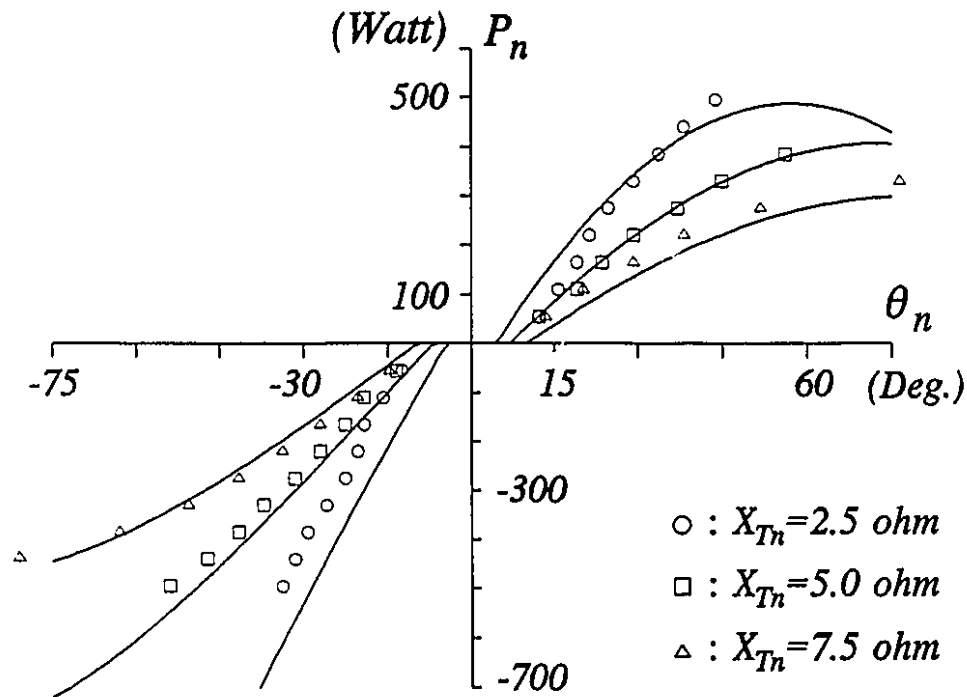


Figure 3-5 DC link power versus voltage phase angle characteristics.



on the well known formula of the real power, Eq. (2.6), when the transmission line impedance, the sending and receiving end voltage magnitudes and phase angle are known. The switching losses of the valves account for the zero power output between  $-10$  and  $+10$  degrees in Fig. 3-5. The estimated switching losses are deducted from the theoretical curves. The theoretical curves and the experimental points show reasonable agreement.

The following features have been demonstrated by the experimental results:

- (1) Real power control is accomplished by the voltage phase angle control. (This follows the same practice as in the ac generator station.)
- (2) The changeover from rectifier to inverter operation is achieved by changing the voltage phase angle from positive to negative value. On the dc side, the dc link voltage remains constant and it is the flow of the local average dc link current  $I_{dcl}$  that reverses direction.
- (3) The Dc Voltage Regulator is a power slack. In order to ensure that the capacitor voltage is charged at the present reference voltage, the DC Voltage Regulator converts the power necessary to replace the amount taken by the Power Dispatcher.
- (4) There are active ac voltages at the terminals of the converter which are supported by the dc link voltage from the capacitor charges, and therefore there is no voltage droop or collapse as in conventional HVDC.

- (5) As the ac transmission distance increases,  $jX_{Tn}$  increases. From Fig. 3-5 one sees that in order to transmit same power it is necessary to increase the voltage phase angle. The steady-state stability limits are defined by the extremum points in the curves. For  $jX_{Tn}=7.5$  ohm, one sees that  $\pm 75$  degrees have been recorded as experimental points which lie within the steady-state stability limit.

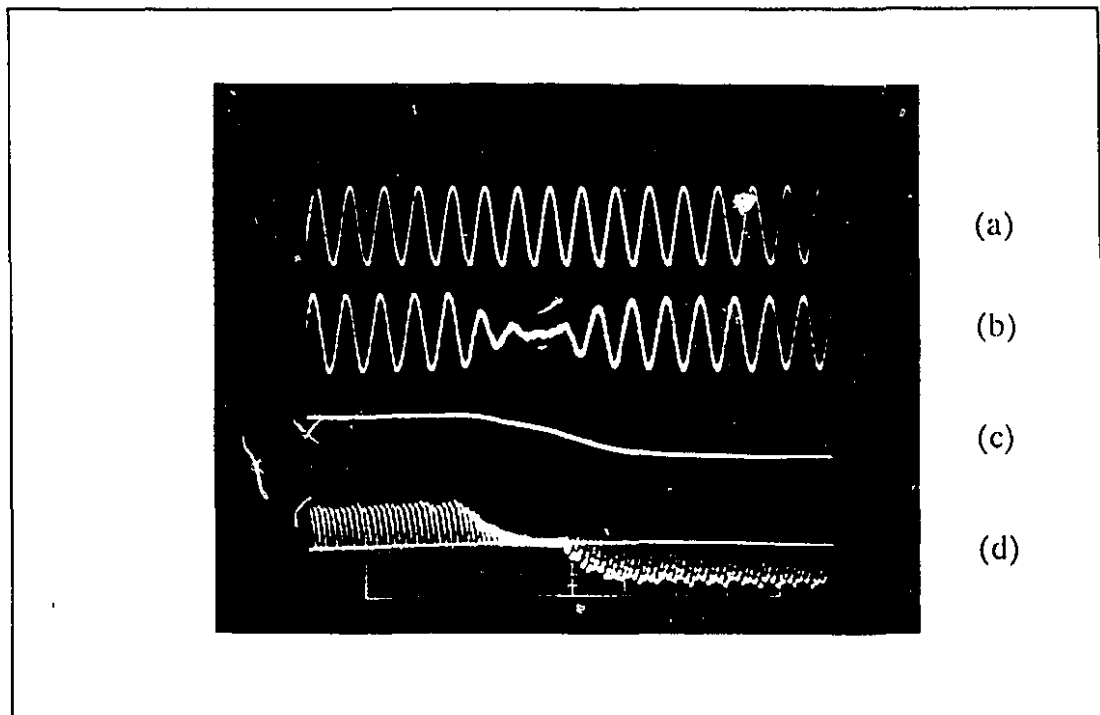
By situating the back-to-back PWM-HVDC link midway between the sending and receiving ends of a long weak ac transmission system, it is possible to double the power capability of the ac lines. The experimental points at  $\pm 75$  degrees for  $jX_{Tn}=7.5$  ohm in Fig. 3-5 demonstrate this as a fact. The total transmission reactance is 15 ohm, with 7.5 ohm between the sending-end and DC Voltage Regulator and another 7.5 ohm between the Power Dispatcher and receiving-end. The total voltage phase angle between the sending-end and the receiving-end is  $75^\circ + 75^\circ = 150^\circ$ , which exceeds the stability limit of 90 degrees.

### 3.4 Transient Tests

A number of tests were conducted to prove that the Power Dispatcher (DISP) and DC Voltage Regulator (VR) coordinate their functions during transients using their local feedback controls only.

Fig. 3-6 is the photograph of the oscillogram taken at the DC Voltage Regulator, when a step reversal of demand from a negative (inverter) to a positive

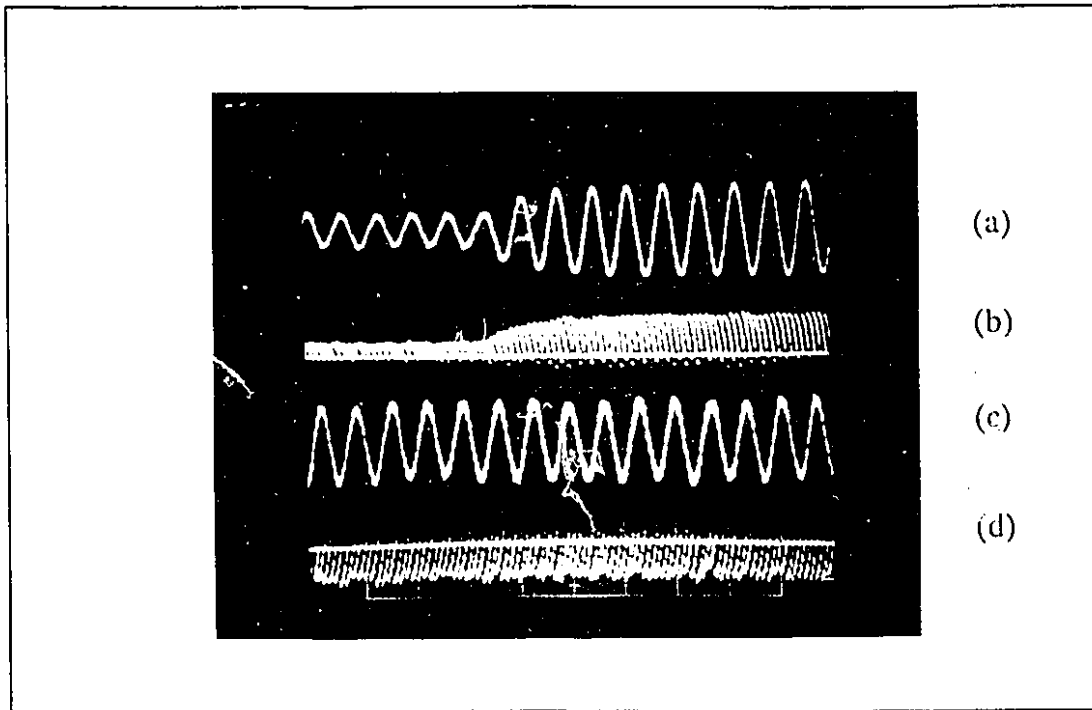
(rectifier) value was applied to the power reference setting,  $P_{REF}$ , of the Power Dispatcher. Initially the DC Voltage Regulator operated as a rectifier (positive dc link current  $I_{dc}$ ) and then it changed to inverter operation (negative dc link current  $I_{dcI}$ ) in response to the power step change in the Power Dispatcher. Thus it operated as a power slack and ensured that the demands of the Power Dispatcher were satisfied promptly by the local voltage regulator feedback loop. Fig. 3-6(a) shows the fundamental harmonic voltage, and by comparison one sees that the line current in Fig. 3-6(b) is a very good sinusoidal current. Fig. 3-6(c) shows the voltage phase angle,  $\theta_n$ , which controls the power change during the



**Figure 3-6** Transient waveforms in DC Voltage Regulator during power reversal: (a) fundamental harmonic voltage, (b) ac line current, (c) voltage phase angle, (d) dc link current.

transient (there is a slight delay in the voltage phase angle transducer). Fig. 3-6(d) shows the dc link current,  $I_{dc1}$ , immediately at the converter output terminal. The ripples of  $I_{dc1}$  have been filtered by the dc link capacitor so that the output dc current,  $I_{dc2}$ , would not cause communication channel interference. The dc link current is positive during rectification and negative during inversion as is evident in Fig. 3-6(d).

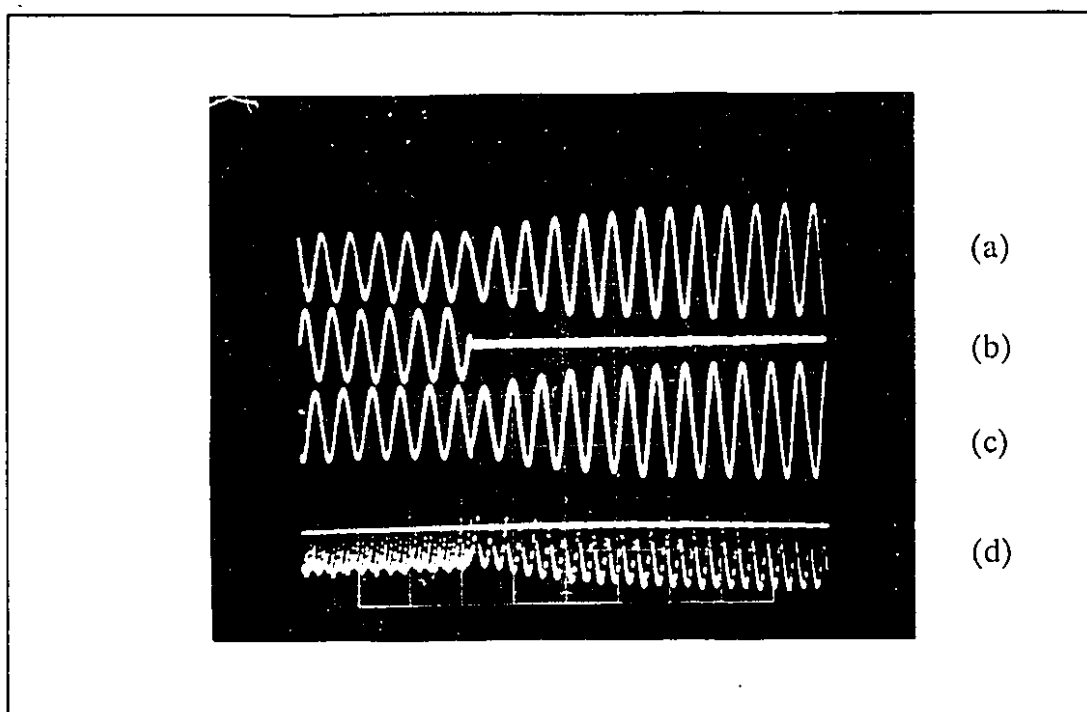
An experiment to simulate multi-terminal (3-station) HVDC operation was performed. Based on the circuit of Fig. 3-1, in the beginning, the Power Dispatcher (DISP) was assigned to deliver a fixed amount of inverter power. The DC Voltage Regulator (VR) automatically assumed the role of a rectifier. Fig. 3-7 shows the oscillogram of (a) the ac current, (b) the dc link current of the DC Voltage Regulator, (c) the ac current and (d) the dc link current of the Power Dispatcher (DISP). As shown in Fig. 3-7, the initial portions of the dc link currents of VR and DISP are respectively positive (rectifier) and negative (inverter). A step power demand of the third station in the dc link was simulated by connecting a resistance across the dc link. From Fig. 3-7(c) and (d) one observes that the Power Dispatcher fulfilled its assigned power in spite of disturbance from the third station. The additional power consumed by the simulated third station was taken up by the DC Voltage Regulator. From Fig. 3-7(a) and (b), it is apparent that the DC Voltage Regulator increased its rectified power so as to accommodate the step power demand of the third station.



**Figure 3-7** Transient waveforms in multi-terminal experiment: (a) ac line current and (b) dc link current in DC Voltage Regulator (VR); (c) ac line current and (d) dc link current in Power Dispatcher (DISP).

The HVDC converter station should be able to survive fault conditions. One kind of fault, the disconnection of one ac phase, has been tested successfully on the DC Voltage Regulator and on the Power Dispatcher. This occurs either through the accidental severance of one line or deliberately by opening the circuit breaker of the line which has a line-to-neutral fault.

Fig. 3-8 shows the line currents in the three ac phases in (a), (b) and (c) and the dc link current in (d) during such a fault which occurred in the *B*-phase of



**Figure 3-8** Transient in disconnection of *B*-phase of DC Voltage Regulator: (a), (b), (c) A, B, C phase line currents; (d) dc link current.

the DC Voltage Regulator. The currents in the remaining phases increased so as to make up for the same power as before the fault. The currents continued to have near sinusoidal waveforms.

### 3.5 Summary

Through the experimental tests under steady-state, transient, and faulted conditions, the significant advantages of voltage-source type PWM converter station in the HVDC applications have been demonstrated in this chapter. The next chapter continues the research on the system parameters and concludes that the voltage-source PWM-HVDC system is not economically unreasonable.

## PARAMETRIC STUDY

### 4.1 Introduction

The realizability of the concepts of **Chapter 2** by the experiments described in **Chapter 3** leads the research to the next stage, which consists of sizing of the valves, the inductors,  $L$ , on the ac side and the capacitor,  $C_{dc}$ , on the dc side of the PWM-HVDC converter station in Fig. 2-1. Since the inductors and the capacitor form an integral part of the converter station, it is critical that they are of reasonable values compared to those presently used in conventional HVDC.

In addition, the parametric studies have been pursued to get an idea as to what carrier frequencies,  $f_r$ , and modulation index,  $M$  [12], of the Sinusoidal Pulse Width Modulation (SPWM) should be used.

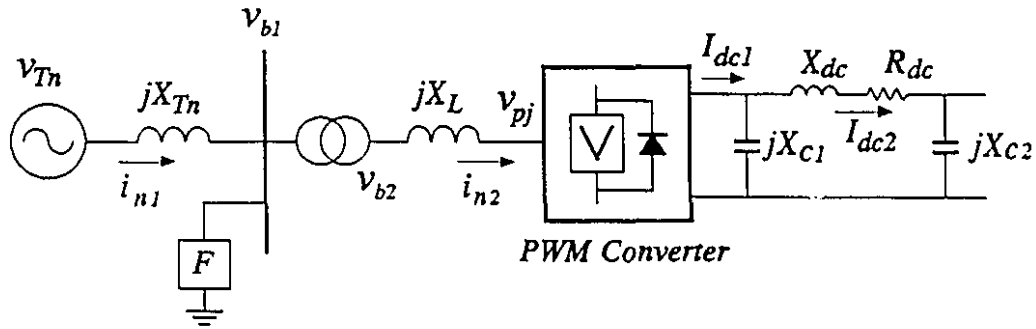
It is assumed in this study that there will be valves capable of switching at 1260 Hz (21 pulse per 60 Hz cycle) with acceptable losses for HVDC applications. It should be stressed that the GTO's used in present high power *Static VAR Compensation* (SVC) application switch only at 120 Hz [4,5]. But given the fact that it takes an average time of 20 years for an innovation to go from the conceptual stage to the market place, it is not unreasonable to proceed with the expectation that when there is application for them, the valve manufacturers will invest in R & D to perfect the GTO's, the MCT's and the SITH's within the 20 year period.

In HVDC transmission systems, the dc voltage ratings are of the order of  $\pm 500$  KV. In the existing converter stations, the 5 KV thyristors are strung in series to build up the voltage withstand [82]. Conceivably, the GTO's and the other gate-turn-off valves will also have to be connected in series to achieve the same high voltage rating. The mastery of the technology of increasing the voltage and the current rating will require extensive research by the manufacturers. In this chapter, the goal is to demonstrate that the "ball-park" figures required of the component sizes are not astronomically large so that the manufacturers will seriously consider the PWM-HVDC system as economically feasible.

## 4.2 System Model for Parametric Study

The voltage-source type PWM-HVDC converter station used for the





**Figure 4-1** Converter station connected to ac utility system and dc system used for feasibility study.

parametric studies is illustrated in Fig. 4-1. In Fig. 4-1, the  $v_{Tn}$  and  $X_{Tn}$  are the Thevenin equivalent voltage and impedance representing the ac utility system. The reactance  $X_L$  includes the leakage reactance of the transformer with additional reactances which may have to be added. On the dc side, the  $X_{c1}$  and  $X_{c2}$  represent the capacitances directly connected across the converter stations. The dc transmission line is represented by the impedance  $R_{dc} + jX_{dc}$ .

The box "F" connected on the bus in Fig. 4-1 represents the ac filter bank which prevents the harmonic currents from being injected into the ac utility network. The ac filter can consist of the shunt  $L$ - $C$  elements which are tuned to the switching harmonics so as to "short-circuit" the harmonic currents. It can be the same type of filter which is used in conventional HVDC [2,62,63] except that the harmonic currents are at a higher frequency so that the requisite  $L$ - $C$  elements are smaller and hence cheaper.

The per unit system is used. The power base is chosen as:

$$\begin{aligned}
 P_{BASE} &= 3 v_{b1BASE} \times i_{n1BASE} \\
 &= 3 v_{b2BASE} \times i_{n2BASE} \\
 &= V_{dcBASE} \times I_{dcBASE}
 \end{aligned} \tag{4.1}$$

The ratings are defined under the condition that the PWM-HVDC station is operating with modulation index  $M=1.0$  and the reactance  $X_L=0.0$ . Thus for the schematic of the converter station connected to the ac utility system as shown in Fig. 4-1:

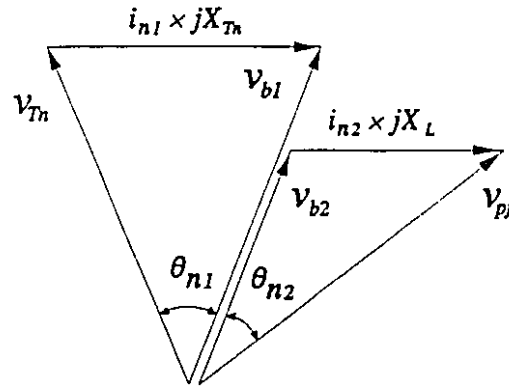
$$\begin{aligned}
 v_{Tn} &= v_{b1} = 1.0 \text{ p.u.} \\
 v_{b2} &= v_{pj} = 1.0 \text{ p.u.} \\
 V_{dc} &= 1.0 \text{ p.u.}
 \end{aligned} \tag{4.2}$$

In Eq. (4.2),  $v_{b1}$  and  $v_{b2}$  are fundamental Fourier Series component of the voltages on the primary and the secondary side of the transformer, and  $v_{pj}$  is fundamental Fourier Series component of converter terminal voltage.

In the study, a weak ac utility system with a *Short Circuit Ratio* [63],  $S.C.R.=3.0$  is assumed. The Thevenin equivalent impedance is then:

$$X_{Tn} = \frac{1}{S.C.R.} = 0.333 \text{ p.u.} \tag{4.3}$$

Fig. 4-2 shows the voltage phasor diagram in the general case when the modulation index  $M$  is not unity. It is assumed that  $1.0 \text{ p.u.}$  power is transmitted to the converter station so that the voltage phase angle subtended by  $v_{Tn}$  and  $v_{b1}$



**Figure 4-2** Phasor diagram of fundamental Fourier Series component of voltages.

will be:

$$\theta_{n1} = \sin^{-1} \left( \frac{X_{Tn}}{v_{Tn} v_{b1}} \right) = 19.74^\circ \quad (4.4)$$

As the  $v_{b1}$  and  $v_{b2}$  are not equal, it is necessary that the turns ratio of the transformer must be chosen such that:

$$n = \frac{v_{b2BASE}}{v_{b1BASE}} \quad (4.5)$$

The transformer secondary voltage,  $v_{b2}$ , and the fundamental Fourier Series voltage on the ac terminal of the converter station,  $\bar{v}_{pj}$ , are related as  $v_{b2} = \bar{v}_{pj} = 1$  p.u. under the condition of the modulation index  $M=1.0$  and  $X_L=0.0$ . When  $M \neq 1.0$ ,  $\bar{v}_{pj}$  can be presented as  $\bar{v}_{pj} = M$  in per unit. Table 4-1 lists the per unit values used in the study.

Table 4-1 System parameters chosen for feasibility study.

Per Unit Values of Fig. 4-1		
$X_{Tn}=0.333 \text{ p.u.}$	$X_{c1}=1.0 \text{ p.u.}$	$X_{c2}=1.0 \text{ p.u.}$
$X_{dc}=1.0 \text{ p.u.}$	$R_{dc}=0.05 \text{ p.u.}$	

### 4.3 Sizing $X_L$ by AC RMS Current

The *rms* (root-mean-square) value of the ac line current is used for rating the bridge valves, the transformers and the reactance  $X_L$ . The ac line current can be obtained by using the superposition principle in which each harmonic component of the current is the line harmonic voltage divided by the line impedance at the harmonic frequency. The *rms* current is generally used for rating since it takes into account of the fundamental component and all the harmonics of the current in the computation of the heating of the component.

For meaningful comparisons, the results from the harmonic calculation will be based on the same power rating condition. As the fundamental Fourier Series component of voltages and currents are the "useful" part of the power-transfer, their steady state values are adjusted to ensure  $1.0 \text{ p.u.}$  power to be transferred to the converter station as the values of  $X_L$  and  $M$  are varied in the parametric study.

On the secondary side of the transformer, the power transmitted across  $X_L$  is:

$$\frac{v_{b2} M \sin(\theta_{n2})}{X_L} = 1.0 \quad (4.6)$$

Referring to the height of the triangle in Fig. 4-2:

$$v_{b2} \cos \frac{\theta_{n1}}{2} = M \cos \left( \theta_{n2} + \frac{\theta_{n1}}{2} \right) \quad (4.7)$$

The two equations (4.6) and (4.7) permit  $v_{b2}$  and  $\theta_{n2}$  to be solved for a specification of  $M$  and  $X_L$ . The magnitude of the fundamental Fourier Series current of the transformer secondary,  $\bar{i}_{n2}$ , is:

$$\bar{i}_{n2} = \frac{v_{pj} \sin \left( \theta_{n2} + \frac{\theta_{n1}}{2} \right) - v_{b2} \sin \frac{\theta_{n1}}{2}}{X_L} \quad (4.8)$$

The converter station is controlled by using the Bi-Logic SPWM scheme. The harmonics of the ac terminal voltages are determined by the choice of the  $M$  and  $f_r$ . Apart from establishing that reasonable inductances and capacitance will enable the voltage-source PWM-HVDC converter station to operate, the study investigates their dependence on the modulation index  $M$  and the carrier frequency  $f_r$ . It is desirable that  $f_r$  is low as it reduces switching losses of the valves. It is also desirable that at the rated ac voltage,  $M$  should be less than 1.0. This allows the voltage amplitude to be raised and lowered for reactive power control. For instance, in choosing  $M=0.8$  for the rated operation, an over-voltage capability up to  $M=1.0$  is permitted.

Having used Eqs. (4.5) to (4.8) to solve for the fundamental Fourier Series component of voltages and currents which will transfer  $1.0 \text{ p.u.}$  power through the converter, it is a straight forward exercise to evaluate the Fourier Series harmonic voltage based on the modulation index  $M$  and the triangular carrier frequency  $f_r$ .

The inductive reactance  $X_L$  is used as a common abscissa in the study. The concern here is that  $X_L$  should not be excessively large. It should be stressed that  $X_L$  includes that transformer leakage reactance which lies in the  $0.15\text{-}0.20 \text{ p.u.}$  range.

In the results presented graphically in Fig. 4-3, the attention is drawn first to the point of intersection of two axes which corresponds to the fundamental

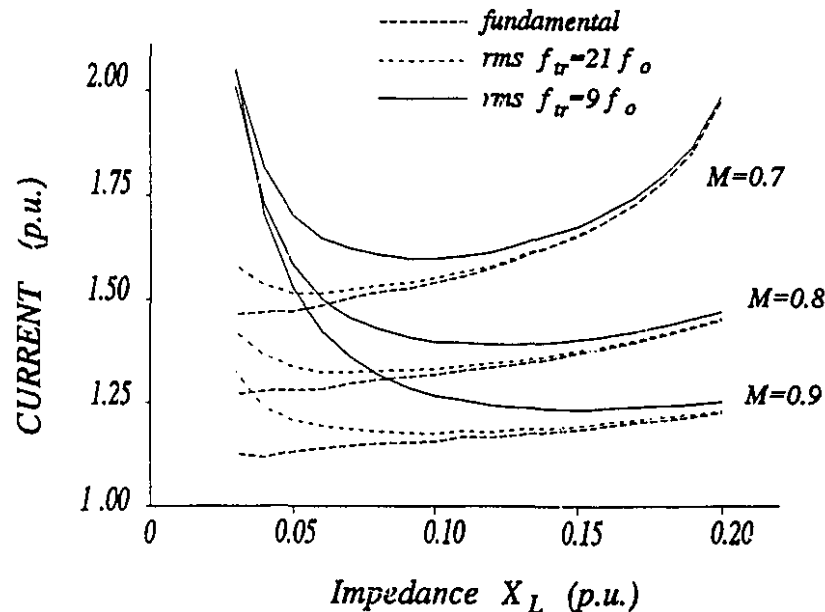


Figure 4-3 Fundamental and rms converter ac current as a function of  $X_L$ .

Fourier Series component of the converter ac phase current which is required to rectify 1.0 p.u. power from the Thevenin equivalent voltage source, for  $M=1.0$ ,  $X_L=0.0$  and  $\bar{i}_{n2}=1.0$  p.u. . In order that the same power is transferred for a lower converter voltage associated with the use of a smaller modulation index  $M$ , a bigger  $\bar{i}_{n2}$  is required. Likewise, for the same  $M$ , a larger current is needed to deliver the same power when  $X_L$  is increased. The large current is required to compensate for the large voltage drop across  $X_L$  so as to be able to deliver the same power.

The *rms* values of the converter ac output current include all the switching harmonic components. As  $X_L$  increases, the filtering effect is apparent and the *rms* values converge towards the fundamental component. Fig. 4-3 also shows the difference between using a carrier of frequencies  $f_r=9\times f_o$  and  $f_r=21\times f_o$ . Here  $f_o$  is the line frequency, 50 or 60 Hz.

As a guide to the cost of  $X_L$ , Fig. 4-4 graphs the VA rating of  $X_L$  based on the formula  $VA=0.5X_L\times i_{n2rms}^2$  and in Fig. 4-5 the cost reference factor based on the formula  $Cost-Reference-Factor=X_L\times i_{n2rms}\times v_{max}$ .

For PWM application, the Cost Reference Factor is likely to be more pertinent because the insulation of the reactance must be capable of withstanding the maximum voltage  $v_{max}$  during PWM switchings.

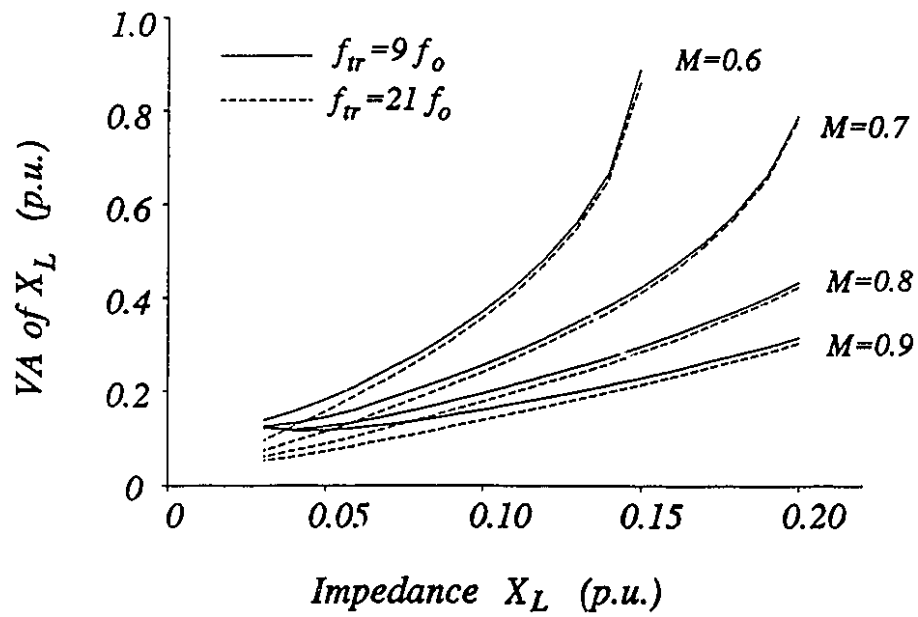


Figure 4-4 VA of  $X_L$  as a function of  $X_L$ .

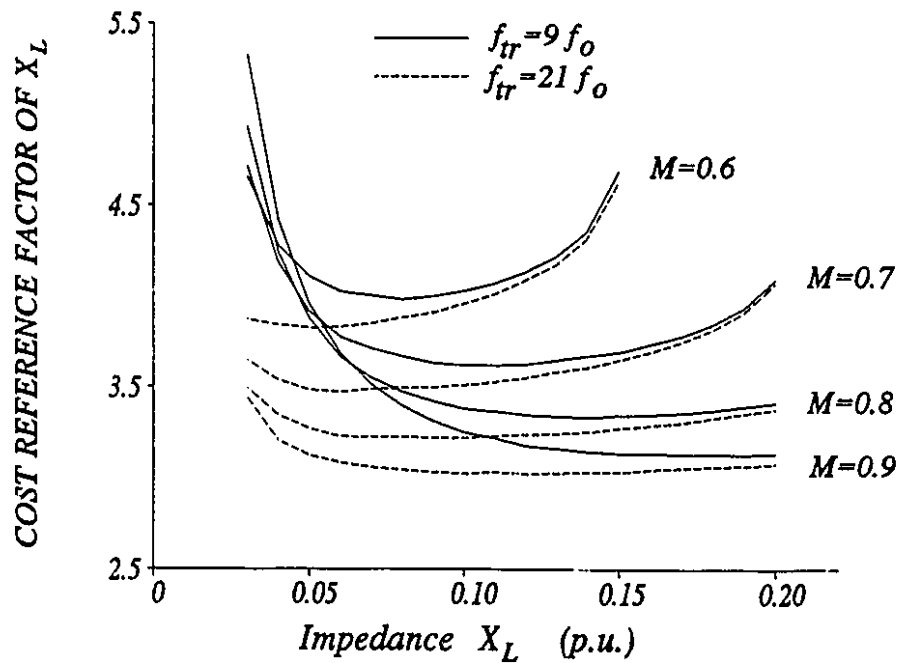


Figure 4-5 Cost Reference Factor ( $X_L \times i_{n2ms} \times v_{max}$ ) vs  $X_L$ .



#### 4.4 Total Harmonic Distortion

Based on the ac line currents,  $i_{n2}$ , and the SPWM switching functions,  $S_j$ , the current injected by the converter into the dc side of Fig. 4-1 can be calculated. A description of one method has appeared in [83,84]. The voltages and currents in the dc side are solved from circuit theory and Fourier Series analysis.

One measure for harmonic appraisal is the *Total Harmonic Distortion* factor. For the converter dc output voltage, the factor  $THD_{vdc}$  is defined as:

$$THD_{vdc} = \left( \sum_{k=1}^{\infty} V_{dck}^2 \right)^{1/2} \times 100\% \quad (4.9)$$

where  $V_{dck}$  is the magnitude (per-unit) of the  $k$ th Fourier Series harmonic voltage across the capacitor  $X_{cl}$ . Also, the Total Harmonic Distortion factor for the converter dc output current,  $THD_{Idc}$ , is defined as:

$$THD_{Idc} = \left( \sum_{k=1}^{\infty} \left( \frac{V_{dck}}{kX_{dc}} \right)^2 \right)^{1/2} \times 100\% \quad (4.10)$$

It is important to keep the factor  $THD_{Idc}$  within certain limit to reduce the harmonic noise interference to the telephone communication system. The typical value is less than or equal to 5% [12,85].

Fig. 4-6 and Fig. 4-7 show the Total Harmonic Distortion factors of the dc voltage and current respectively. In Fig. 4-6, one sees that for  $f_r = 9 \times f_o$ , one just misses complying with the required 5% in the practical range of  $0.15 < X_L$ . At the

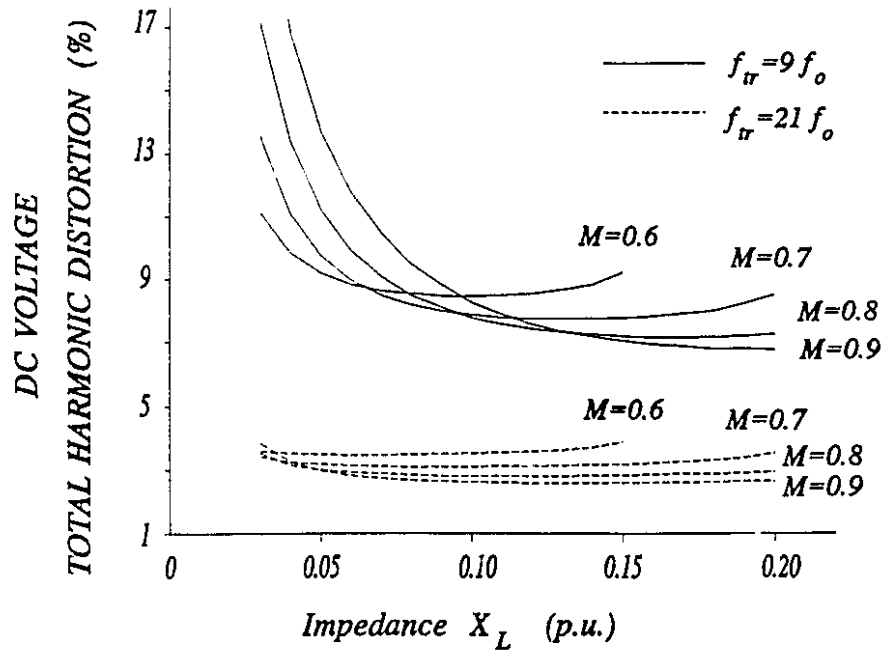


Figure 4-6 Total DC Voltage Harmonic Distortion factor vs  $X_L$ .

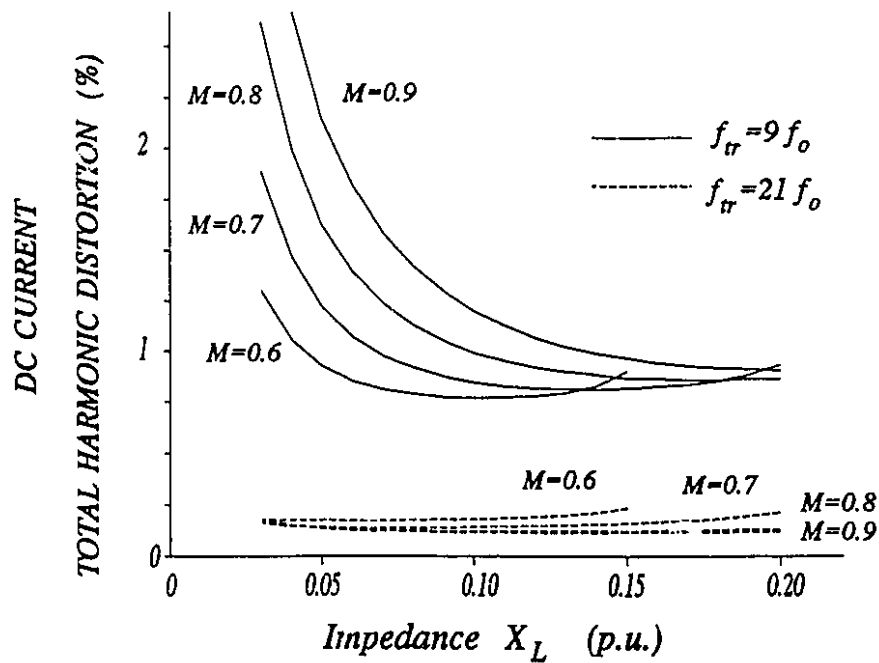


Figure 4-7 Total DC Current Harmonic Distortion factor vs  $X_L$ .

higher carrier frequency of  $f_r = 21 \times f_o$ , the 5% is easily satisfied. The Total Harmonic Distortion factor of the dc current is always below the allowed 5%.

The above studies show conclusively that the fairly large transformer reactance, which is in the  $0.15-0.20$  p.u. range, will contribute towards making the voltage-source PWM-HVDC a practical proposition.

With further refinement in the dc capacitor design, it should be possible to use a carrier frequency which is as low as  $f_r = 9 \times f_o$ . For economic design  $M$  should be as high as possible. If the equipment is overrated to have excess *rms* current carrying capacity,  $M$  can be varied to have a range of voltage magnitude control.

#### 4.5 VA Rating and Switching Losses

Any challenges to the conventional HVDC system must first address the problem of operation under the very high voltage and current ratings of the HVDC environment. Present HVDC systems, which are commonly in the thousands of MVA and hundreds of KV range, operate by connecting thyristors in series. Before PWM techniques can replace the line-commutated HVDC converter station, considerable expense and research will have to be devoted to mastering the technology of series and parallel connections of the force-commutated switching valves. Amongst the problems which have yet to be solved are: (1) reducing the switching losses associated with high frequency operation of

the valves, (2) increasing the voltage limit and the current carrying capacity of the valves or alternatively using series and parallel strings of valves (at reduced ratings) with protection to ensure that they are always stressed equally in steady-state and in transient conditions.

As mentioned in **Chapter 1**, many kinds of high power, force-commutated switching devices have been applied to the industrial power converters. The PWM technique using GTO's has already been operational at the *MVA* levels required in electrical traction, industrial drives, UPS and static VAR compensators, etc. Although there is still a leap from a few megawatts to the hundreds of megawatts range required of HVDC, it is not too early to pursue the conceptual and feasibility studies as have been done in this thesis.

Today, the GTO, the SITH and MCT have characteristics which are suitable for applications requiring high voltage and current ratings. Recently, Japanese researchers [68] have also proposed SITH valves for the PWM type of HVDC converter station which has the single pole capacity of *30 MW (150 kVdc/200 Adc)* using the SITH valves rated at *2500V/800A* with the switching frequency up to *20 kHz*.

In McGill University, preliminary feasibility studies have shown that the *MVA* ratings can be achieved by series and parallel connections of the dc terminals of the voltage-source (boost) type PWM converter modules of Fig. 2-1. It has been shown that the voltage and current stresses in steady-state and in

transients are fairly equitably distributed in the converter modules using acceptable tolerances in components [60]. Using the technique of phase shifting of the triangular carrier in SPWM [61], high quality PWM can be attained by reduced switching rates of the individual valves. This promises reduced switching losses and the ability to use slow switches, i.e., GTO thyristor. The reduction of switching losses through active and passive snubber circuits is again an extensive area for research.

#### **4.6 Summary**

This chapter has addressed the sizing of the ac inductances and the dc capacitor in the voltage-source PWM converter station for HVDC applications, as its proper functioning depends on the presence of fairly large inductances and capacitance. The study has shown that the sizes used in the present HVDC thyristor converter stations are comparable to those required by the voltage-source PWM-HVDC converter stations. Another finding is that fairly low carrier frequency can be used, so that switching losses can be low. These results add to support the practicality of the voltage-source type PWM-HVDC.

Part I of this thesis has been concerned with advancing the application of the Pulse Width Modulation technique to the Voltage-Source type bridge converter. As a research area, the field is well trodden, especially in amplitude and frequency control of Two-Level or Bi-Logic PWM techniques.

The advances made in Chapters 2, 3 and 4 have been in the phase and the

frequency control of the PWM technique. Technically, the implementation is through a Voltage Controlled Oscillator, EPROMs to from a Phase Lock Loop described in **Chapter 2**.

The example of the application found for it in this thesis is in the form of a converter station of HVDC Transmission System. Elsewhere, not included in the thesis, the same concepts have been applied for the control of the Series-Type Static VAR Compensator [86]. The common denominator in all these applications is that the PWM converter interfaces with the power utility system which has its frequency to which the converter must be locked in synchronism through the Phase Lock Loop. Once in synchronism, the phase angle is advanced or retarded so that the converter operates as a rectifier or inverter. In the case of the Static VAR Compensator operation the power input is nulled.

The concepts had first been demonstrated by digital simulations and verified through the experimental tests reported in **Chapter 3**. As the test have shown the excellent characteristics predicted for the PWM-HVDC Transmission System are experimentally realizable, the parametric studies of **Chapter 4** have been conducted to demonstrate that the PWM-HVDC converter station is indeed not unrealistic in terms of cost.

The research on the phase angle and frequency control of PWM has opened up a large field of applications in the electric power utility environment.

Starting from the next chapter, the studies on the Tri-Logic SPWM technique and its applications will be described.

## **DYNAMIC TRI-LOGIC SPWM CONTROL OF 3-PHASE CURRENT-SOURCE CONVERTER**

### **5.1 Introduction**

Although many converters in the past had been labelled as PWM controlled Current-Source bridge converters, they had never lived up to the claims. After the definitive work of Hombu, Ueda and Ueda [40,41], one knows now that because the PWM strategy in use had been the Two-Level or Bi-Logic, the valves could not have switched in the manner as wished by their designers. A re-examination of their experimental results reveals very poor waveforms which have little resemblances to the intended sinusoids. Hombu, Ueda and Ueda [40,41] established that the Three-Level or Tri-Logic PWM should be used and indeed the experimental waveforms show remarkable improvements.

Unfortunately the syntheses of the Tri-Logic PWM signals by Hombu, Ueda and Ueda and other researchers [42-46] had been based on "ad-hoc" engineering design. Typically, the design begins with a decision as to the number of pulses to be used per cycle and choosing a waveform harmonic criterion. Then an optimization exercise follows by which the switching angles are determined for one discretized modulation index level. The information of the switching angles for all the modulation index levels are stored in EPROMs. These "ad-hoc" design methods are static methods because the optimization criterion is based on the steady-state sinusoidal waveform.

The research reported in this chapter is targeted towards a systematic synthesis of a Dynamic Tri-Logic PWM strategy. The term "Dynamic" is used to contrast it with the "Static" methods. The objective is ensure that the "local average" of the output signal is linearly proportional to the input modulating signal at the sampled period. The modulating waveform does not have to be a sine-wave.

It is stated in Part I that the Two-Level or Bi-Logic PWM techniques are in an advanced state of development so that the remaining area of research has been in the phase-angle control. In contrast, the Three-Level or Tri-Logic PWM concepts are at the infancy stage. For this reason, this chapter is devoted to a systematic mapping of its characteristics.

Section 5.2 discusses the peculiarities of the 3-phase current-source bridge



converter and why it is more difficult to operate than the voltage-source topology.

Section 5.3 describes the Dynamic Tri-Logic PWM. The truth table, Table 5-1, is essentially a proof that the proposed Dynamic Tri-Logic PWM will operate the valves of the bridge-converter in the manner prescribed by Hombu, Ueda and Ueda [40,41]. The truth table, Table 5-2 is another proof that the proposed Dynamic Tri-Logic PWM can be synthesized from Two-Level or Bi-Logic PWM by a linear transformation.

The rigorous mathematical foundation, with linear transformation as its corner-stone, ensures that the properties of Bi-Logic PWM carry over to the Tri-Logic PWM. In particular, the Sinusoidal PWM (SPWM) is chosen for the Bi-Logic PWM because it has the "Dynamic" properties sought for. Essentially, the "local average" of the Bi-Logic SPWM output is the linearly amplified signal of the modulation input signal. In fact, the amplification gain is constant and without phase-shift, for a frequency bandwidth of  $1/3$  of the triangle carrier frequency [87]. Since the translation from Bi-Logic to Tri-Logic is also linear, the Tri-Logic PWM outputs are also linear amplified signals of the inputs.

However, there is the problem that the translation formula in Eq. (5.2), "scrambles" the Bi-Logic signals. For this reason, it is necessary to prepare the inputs of the Bi-Logic SPWM signals in anticipation of the "scrambling". The Decoupler Pre-Processors in Section 5.3.5 compensate for the "scrambling" and accomplish the decoupled control of the 3-phase converter output currents by the

input signals.

There is another practical problem of deciding which one of the three legs of the bridge converter should have both the Upper Valve and the Lower Valve simultaneously ON, so as to implement the Zero or Shoot-Through State of the Tri-Logic signal. This problem is discussed in Section 5.3.3 and uses the "single switching action" as the criterion of choosing the Shoot-Through Valves. This is implemented by the PAL (Programmable Array Logic) Gating Circuit described in Appendix B.

## 5.2 Current-Source PWM Converter and Control Difficulties

The top part of Fig. 5-1 shows the 6-valve, 3-phase, current-source PWM converter bridge. It includes the ac line inductances  $L$ , the ac filter capacitors  $C$  and a smoothing inductance  $L_{dc}$  and its resistance  $R_{dc}$  in the dc side.

Comparing with the voltage-source PWM converter topology, Fig. 2-1 in Chapter 2, the current-source PWM converter bridge is a more difficult circuit to master. This is due to the fact that on both the ac and dc sides of the converter, the circuit components are originally all inductive elements. During switchings in the PWM mode of operation, it is not possible to meet the current continuity constraint,  $i(t_-) = i(t_+)$ , in each of the inductive elements,  $L$  and  $L_{dc}$ . Here  $t_-$  and  $t_+$  are respectively the time instants just before and after the switching of a valve. For this reason, in Fig. 5-1 the capacitors,  $C$ , have to be connected across the ac

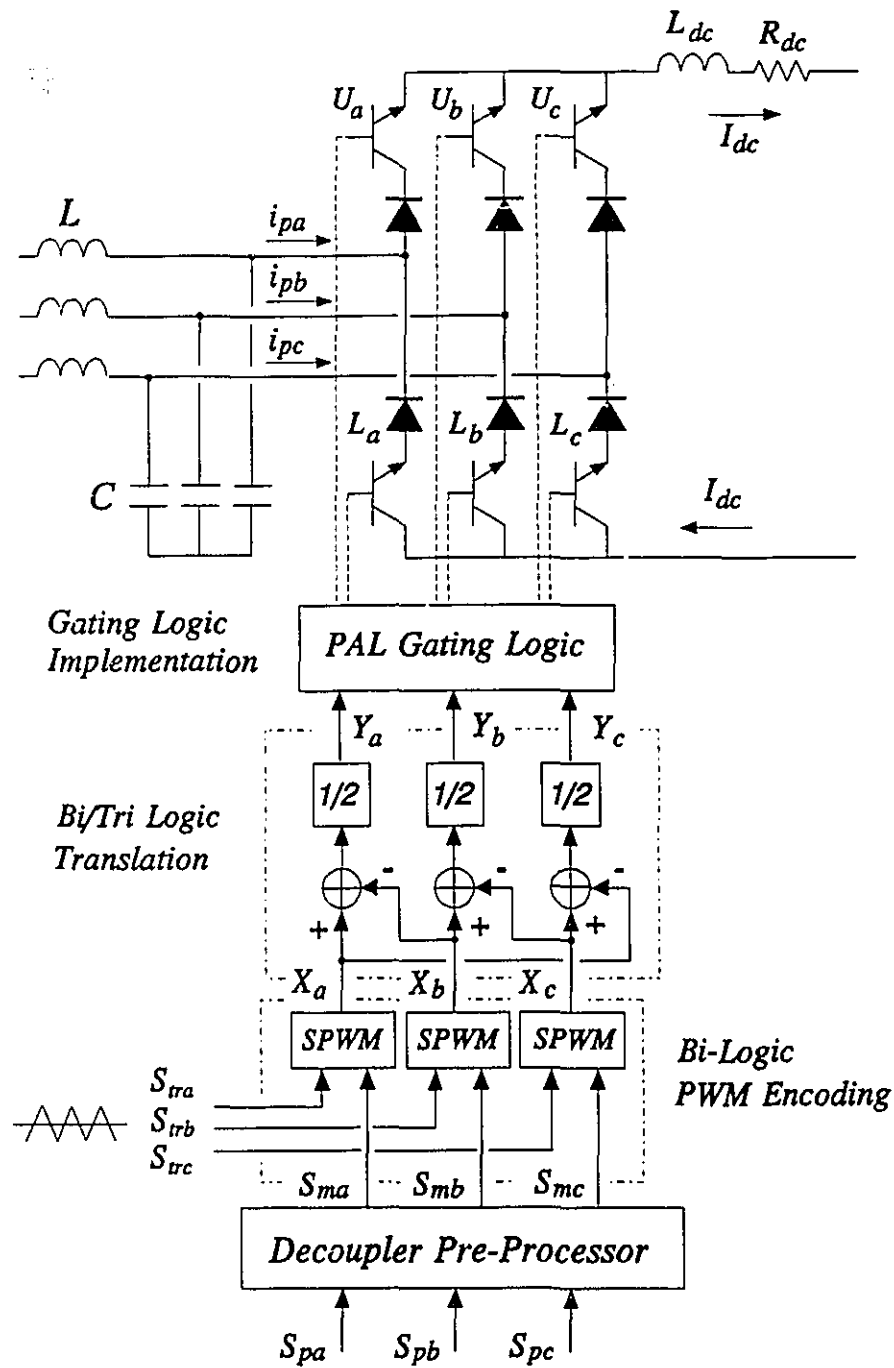


Figure 5-1 Current-source PWM converter with Dynamic Tri-Logic PWM trigger circuit and Decoupler Pre-Processor.

terminals of the converter to act as current buffers and harmonic filters. The presence of the capacitors brings out at least four difficulties which have to be recognized and surmounted.

The first difficulty arises from the capacitor voltages which allow only one of the three upper valves ( $U_a, U_b, U_c$ ) and only one of the three lower valves ( $L_a, L_b, L_c$ ) of the converter bridge to conduct at any time instant. As shown by Japanese researchers, Hombu et al. [40,41], the usual Two-Level or Bi-Logic PWM strategies, which have been developed for the voltage-source converter over the past 20 years, cannot be used. The converter input currents,  $i_{pa}(t)$ ,  $i_{pb}(t)$  and  $i_{pc}(t)$ , must be the three level ( $+I_{dc}, 0, -I_{dc}$ ) type of waveforms. It is necessary to perfect a new Three-Level or Tri-Logic PWM logic.

The second difficulty is again due to the capacitor voltage which can apply a reversed anode-to-cathode voltage across on the valve which is receiving a Turn-ON gating signal. As this valve cannot conduct until the reversed voltage is removed by the proper Turning-OFF of the valve which has been ON, there is a brief non-conduction period. The resultant destructive  $L_{dc} di_{dc}(t)/dt$  voltage can be avoided only by the provision of a current snubber circuit. The current snubber circuit is not shown in Fig. 5-1 to reduce the complication in the presentation.

The third difficulty comes from the resonance between capacitor  $C$  and the inductance  $L$  in the ac lines. The resonance frequency must be chosen to avoid

forced-resonance from two sources: (i) the 5<sup>th</sup>, 7<sup>th</sup> and higher odd harmonics from the ferromagnetic nonlinearity of the ac source, (ii) the switching harmonics of the PWM converter. For high power applications, the switching rates of the valves have to be lowered so as to reduce switching losses. Thus the choice of the  $L$ - $C$  resonance frequency is pushed towards the low frequency end.

The **fourth** difficulty arises from the fact that the additional energy storage elements in the form of the capacitor  $C$  increase the system equation dimensionality by one. By comparison with the voltage-source topology, the current-source topology is potentially more unstable. This is because in our design, which is based on using indirect ac current control, the unity power factor condition is obtained by a "*feed-forward*" loop which calculates the compensation required for the voltage drops across the inductive reactance,  $\omega L$ , and the charging current through the capacitive reactance,  $1/\omega C$ , so that the converter injects the right amount of ac currents for unity power factor operation. However, this compensation is for the 60 Hz steady-state operating condition only and results in poor stability [58,69-72]. For full compensation, it is necessary to implement the  $Ld/dt$  and  $Cd/dt$  operators in the "*feed-forward*" loop. In the indirect current control of the unity power factor voltage-source PWM converter [58], the  $Ld/dt$  operator can be implemented using analog components together with a filter which eliminates the high frequency noise introduced by the differentiator, to secure the same stable operating region as hysteresis control of the voltage-source PWM converter [59]. The addition of the capacitors in the

current-source PWM converter poses an impossible task because it requires a  $d^2/dt^2$  operation to fulfil the  $Cd/dt$  operator to compute the current for charging the capacitor.

### 5.3 Dynamic Tri-Logic PWM

To overcome the first difficulty, this section develops the principles of the Dynamic Tri-Logic PWM strategy [78]. Since the capacitor voltages prevent more than one valve in the Upper and Lower valves of the converter to conduct at any one time instant, the current-source PWM converter has to operate with the currents based on the seven combinations of the Tri-Logic variables as shown in Table 5-1 in Section 5.3.1. Many "Static" Tri-Logic PWM methods [42-46] have been proposed for triggering the current-source PWM converter. But they cannot be used for dynamic control since they have been conceived exclusively for obtaining a good sinusoidal waveform in steady-state operation only.

A Dynamic Tri-Logic PWM strategy, whose converter output signal (after filtering) is the linearly amplified form of the modulating signal, is required for the proper operation of the current-source PWM converter if feedback signals are channelled through the converter for stabilization and active filtering. As the current-source PWM converter must be able to fulfil the multiple functions of unity power factor operation with near sinusoidal waveforms while maintaining close dc current regulation with stable and fast response, by necessity the PWM

strategy must be a dynamic one so that the power of linear system theory can be applied in the design of this fairly complex system. The Two-Level or Bi-Logic Sinusoidal PWM strategy, which has been used in the voltage-source PWM HVDC converter station of Chapters 2, 3 and 4, has the dynamic attributes. As will be shown, their qualities are passed onto the Tri-Logic PWM.

The implementation of the Dynamic Tri-Logic PWM strategy is shown in the functional blocks in Fig. 5-1. The stages of signal processing are added in order to make the local average values of the converter terminal currents,  $i_{pa}(t)$ ,  $i_{pb}(t)$  and  $i_{pc}(t)$ , to be the linearly amplified forms of the control input signals,  $S_{pa}(t)$ ,  $S_{pb}(t)$  and  $S_{pc}(t)$ .

In Fig. 5-1, the *Decoupler Pre-Processor* stage prepares the input modulating signals in anticipation that 3-phase ac circuit is one of two possibilities: (i) *wye* connection, (ii) *delta* connection (which will be shown later in Figs. 5-6 and 5-7 respectively). The aim is to ensure that each of three input modulating signals controls the ac current in the phase assigned to it.

The output signals of the Decoupler Pre-Processor,  $S_{ma}(t)$ ,  $S_{mb}(t)$  and  $S_{mc}(t)$ , are then encoded into Bi-Logic PWM signals,  $X_a(t)$ ,  $X_b(t)$  and  $X_c(t)$  by the SPWM strategy, using triangular carrier signals,  $S_{ra}$ ,  $S_{rb}$  and  $S_{rc}$ .

The Bi-Logic PWM signals,  $X_a(t)$ ,  $X_b(t)$  and  $X_c(t)$ , are next translated into Tri-Logic PWM signals,  $Y_a(t)$ ,  $Y_b(t)$  and  $Y_c(t)$ , which will be used finally to switch

the valves through the *PAL Gating Logic* circuit.

The details in each signal processing stages will be described in following sub-sections.

### 5.3.1 Tri-Logic PWM States, $Y_k(t)$

The Tri-Logic variable,  $Y_k(t)$  (subscript  $k=a, b, c$  for each of the 3 phases), is defined to have three possible values:  $+1, 0, -1$ . Thus the  $k$ th phase output current of the converter,  $i_{pk}(t)$ , is:

$$i_{pk}(t) = Y_k(t) I_{dc}(t) , \quad (k = a, b, c) \quad (5.1)$$

where  $I_{dc}(t)$  is the dc line current.

Table 5-1 lists all the possible Tri-Logic states of the 6-valve, 3-phase, current-source PWM converter and their realizations by the conduction states of the Upper valves,  $U_k$ , and the Lower valves,  $L_k$ .  $U_k=1$  and  $L_k=1$  denote that  $U_k$  and  $L_k$  are switched ON.  $U_k=0$  and  $L_k=0$  denote the OFF states. In the state designations #1, #2, ..., #6,  $I_{dc}(t)$  flows through one of the three ac terminal lines and returns through another. In the state #0 (which has three possible states: #D, #E and #F), all the three ac terminal lines do not carry any current. No current is admitted from the dc side to the ac side. The dc link current,  $I_{dc}(t)$ , flows through a "shoot-through" path constructed by the conduction of the Upper and the Lower valves of the same leg of one of the three phases.



Table 5-1 Current-Source PWM Converter States

State Designation	Tri-Logic			Upper Valve			Lower Valve		
	$Y_a$	$Y_b$	$Y_c$	$U_a$	$U_b$	$U_c$	$L_a$	$L_b$	$L_c$
#1	0	+1	-1	0	1	0	0	0	1
#2	+1	-1	0	1	0	0	0	1	0
#3	+1	0	-1	1	0	0	0	0	1
#4	-1	0	+1	0	0	1	1	0	0
#5	-1	+1	0	0	1	0	1	0	0
#6	0	-1	+1	0	0	1	0	1	0
#0, #D	0	0	0	1	0	0	1	0	0
#0, #E	0	0	0	0	1	0	0	1	0
#0, #F	0	0	0	0	0	1	0	0	1

### 5.3.2 Bi/Tri-Logic PWM Translation

As shown in Fig. 5-1, the Tri-Logic variables  $Y_k(t)$  are obtained from the Bi-Logic variables,  $X_j(t)$  ( $j=a, b, c$  for each of three phases). Each Bi-Logic variable has two possible values:  $X_j(t)=+1$  or  $X_j(t)=-1$ , which are generated from the Sinusoidal Pulse-Width-Modulation (SPWM) function blocks which accept as their inputs, the modulating signals,  $S_{mj}(t)$ , and the triangular carrier signals,  $S_{cj}$ .

The Bi-Logic PWM variables,  $X_j(t)$ , are translated into the Tri-Logic PWM

variables,  $Y_k(t)$ , through the block of *Bi/Tri-Logic Translation* which is based on the linear mapping:

$$\begin{bmatrix} Y_a(t) \\ Y_b(t) \\ Y_c(t) \end{bmatrix} = \frac{1}{2} \begin{bmatrix} 1 & -1 & 0 \\ 0 & 1 & -1 \\ -1 & 0 & 1 \end{bmatrix} \begin{bmatrix} X_a(t) \\ X_b(t) \\ X_c(t) \end{bmatrix} \quad (5.2)$$

$$\text{or} \quad \underline{Y}_{abc} = \frac{1}{2} [C] \underline{X}_{abc} \quad (5.3)$$

Table 5-2 lists all the  $2^3=8$  combinations of the three Bi-Logic PWM variables,  $X_j$  ( $j=a, b, c$ ), and their corresponding Tri-Logic PWM variables,  $Y_k$  ( $k=a, b, c$ ), based on Eq. (5.2). The important fact emerging from Table 5-2 is

**Table 5-2** Truth Table of Bi/Tri-Logic Translation

State Designation	Bi-Logic			Tri-Logic		
	$X_a$	$X_b$	$X_c$	$Y_a$	$Y_b$	$Y_c$
#0, #D, #E, #F	+1	+1	+1	0	0	0
#1	+1	+1	-1	0	+1	-1
#2	+1	-1	+1	+1	-1	0
#3	+1	-1	-1	+1	0	-1
#4	-1	+1	+1	-1	0	+1
#5	-1	+1	-1	-1	+1	0
#6	-1	-1	+1	0	-1	+1
#0, #E, #D, #F	-1	-1	-1	0	0	0

that the Tri-Logic PWM variables form the complete list in Table 5-1. When the valve switchings are based on Table 5-1, they fulfil the constraints of the current-source PWM converter operation, which is that only one Upper and only one Lower Valve can conduct simultaneously. Thus the translation based on Eq. (5.2) allows the current-source PWM converter to be driven by Bi-Logic PWM signals.

For the past two decades, there have been intensive research on Bi-Logic PWM. The translation algorithm of Eq. (5.2) allows this knowledge from Bi-Logic PWM research to be applied to Tri-Logic PWM.

Fig. 5-2 illustrates how the three Tri-Logic signals,  $Y_k(t)$ , are generated from the modulating signals,  $S_{mj}(t)$  ( $j=a, b, c$ ). In this example, the modulating signals are balanced 3-phase sinusoidal waveforms. Fig. 5-2(a) shows how the Bi-Logic PWM encoding is done by the SPWM strategy. The same triangular carrier is used for all the three phases to produce the Bi-Logic variables shown in Fig. 5-2(b), (c) and (d). The three sequences of Tri-Logic signals  $Y_a(t)=[X_a(t)-X_b(t)]/2$ ,  $Y_b(t)=[X_b(t)-X_c(t)]/2$ , and  $Y_c(t)=[X_c(t)-X_a(t)]/2$  are shown in Fig. 5-2(e), (f) and (g) respectively.

In the complete cycle of the modulating signal, the procession of the Tri-Logic states in the time dimension consists of six sub-periods. The sequence of the Tri-Logic states in Fig. 5-2(e), (f) and (g) is described by the six lines of Table 5-3 as a sequence of the state designation numbers from Table 5-1. Each of the sub-periods is identified by the number of the first state of the six lines.

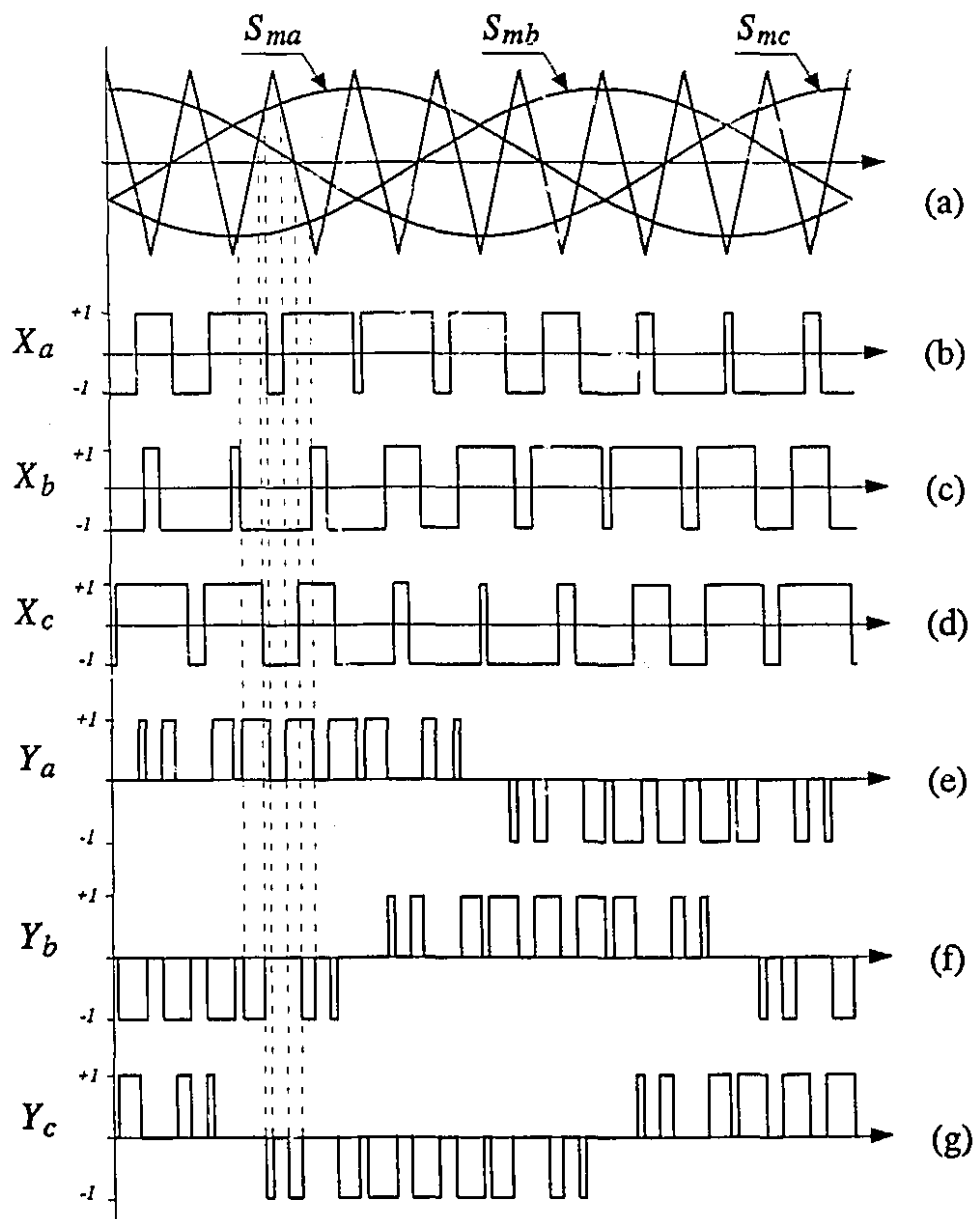


Figure 5-2 Generation of Tri-Logic PWM. (a) SPWM technique; (b),(c),(d) Bi-Logic PWM signals; (e),(f),(g) Tri-Logic PWM signals.

Table 5-3 Sequence of Tri-Logic States

Sub-Period Identification	Contiguity Interpretation (#0)	Sequence in Sub-Period
No.2	#E	- 2 - 0 - 2 - 6 - 0 - 6 - 2 - 0 - 2 -
No.3	#D	- 3 - 0 - 3 - 2 - 0 - 2 - 3 - 0 - 3 -
No.1	#F	- 1 - 0 - 1 - 3 - 0 - 3 - 1 - 0 - 1 -
No.5	#E	- 5 - 0 - 5 - 1 - 0 - 1 - 5 - 0 - 5 -
No.4	#D	- 4 - 0 - 4 - 5 - 0 - 5 - 4 - 0 - 4 -
No.6	#F	- 6 - 0 - 6 - 4 - 0 - 4 - 6 - 0 - 6 -

### 5.3.3 Single Switching Tri-Logic State Transition

It is apparent that the transition from one Tri-Logic state to the next Tri-Logic state must be executed by one "*single switching action*" which consists of turning OFF of one of the two valves which have been ON and turning ON of a new valve to form the next state.

Two Tri-Logic states are called "*contiguous*" when the transition from one state to the other can be effected by a *single switching action*. For example, the Tri-Logic state (+1, -1, 0) or #2 as shown in Fig. 5-3 has four contiguous states. Two of them consist of keeping switch  $L_b$  unchanged and making the changes in the Upper valves as in the cases of #6 and #E. The other two, consist of keeping

$U_a$  fixed as for #3 and #D.

By examining the contiguity of all the states in Table 5-1, it is found that they form a network as shown in Fig. 5-4.

Each sub-period, in Table 5-3, consists of oscillating transitions involving three Tri-Logic states, one of which is #0 or (0, 0, 0). The choice of which of the three *shoot-through* states (#D, #E, #F), is determined by the contiguity requirement embodied in Fig. 5-4.

Fig. 5-3 also shows the Tri-Logic states which come into play in the first

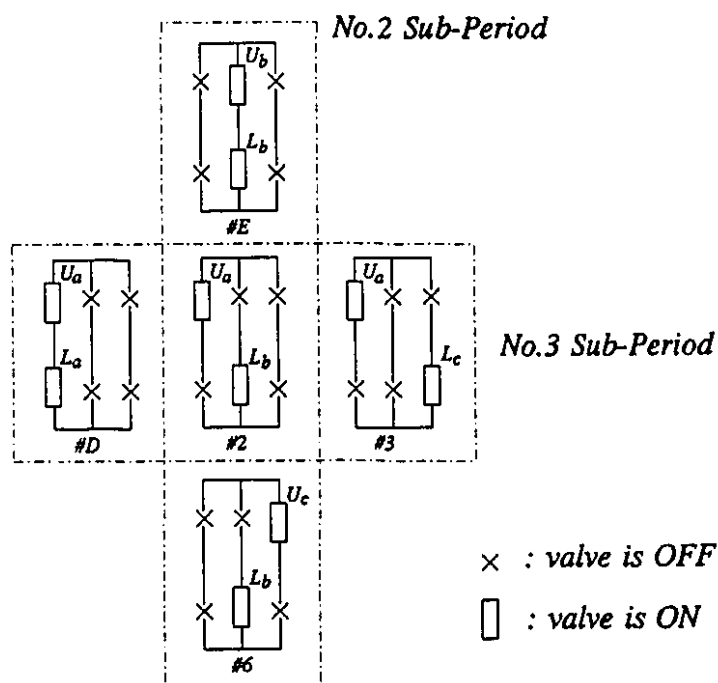
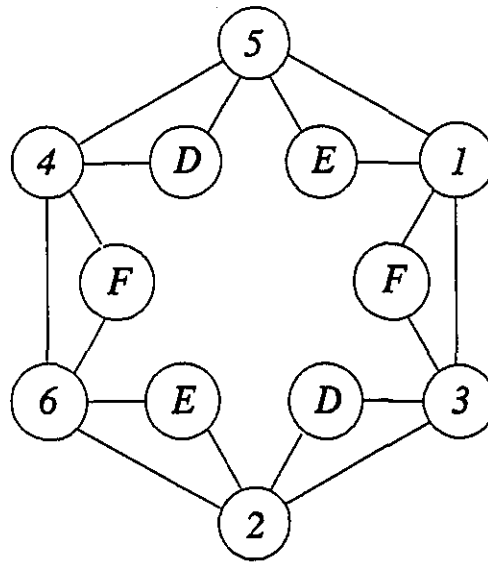


Figure 5-3 Switching state #2 and four contiguous states in 6-valve current-source PWM converter bridge.



**Figure 5-4** Contiguous state of 6-valve current-source converter.

and second lines of Table 5-3 which have been labelled as *No.2* and *No.3* sub-periods. The *#E shoot-through* state is used in connection with the *No.2* sub-period in the interpretation of the *#0* or  $(0, 0, 0)$  state. This interpretation allows  $L_a$  and  $L_c$  to be in the OFF states and  $L_b$  to be in the ON state all through this sub-period when the signals  $Y_k(t)$  call for the stage transitions  $-2-0-2-6-0-6-\dots$ . Only the Upper valves are switched. In the *No.3* sub-period, the states oscillate around *#2*, *#3* and *#0* (which is interpreted as *#D*). As Fig. 5-3 shows, this is efficiently handled by making  $U_a$  ON,  $U_b$  and  $U_c$  OFF throughout this sub-period.

The transition between sub-periods occurs when the state passes from the last member of one line to the first member of the next line in Table 5-3. From the network of contiguous states of Fig. 5-4, it is seen that the line-to-line

transitions in Table 5-3: #2 to #3, #3 to #1, #1 to #5 ... are all contiguous transitions.

The block of *PAL Gating Logic* circuit in Fig. 5-1, receiving the procession of the Tri-Logic PWM signals, issue the switching instructions to the six valves of converter bridge. Its design has to take into account of the features embodied in Table 5-3 and Fig. 5-4. Essentially, it must be able resolve the ambiguity of the #0 state, that is whether #D, #E or #F should be used. It must recognize the arrival of Sub-Period Identification state of Table 5-3 and use the Contiguity Interpretation of the #0 state to implement the *shoot-through* gating signals. The details of the design for the *PAL Gating Logic* circuit will be described in Appendix B.

### 5.3.4 Linear Signal Amplification

Using the Bi/Tri Logic Transformation described above, the 6-valve, 3-phase, current-source PWM converter bridge can be made to function as three sampled linear signal amplifiers for the modulating signals  $S_{mj}(t)$  ( $j=a, b, c$ ). The property of the linear amplifier is derived from the stage of encoding the modulating signals to Bi-Logic PWM and from the linear mapping in the translation to Tri-Logic PWM.

In the Bi-Logic SPWM strategy, each triangular carrier signal,  $S_{trj}$ , samples the value of the modulating signal  $S_{mj}(t)$  at the sampling period of the carrier



signal and embeds the information as the widths of the  $+1$  and  $-1$  pulses of  $X_j(t)$ . In practice, the modulating signal is usually a sinusoidal waveform but in actual fact it can be any arbitrary waveform provided that its frequency bandwidth is below  $1/3$  the carrier frequency [61,87]. In fact, the SPWM output signal  $X_j(t)$  can be shown to be [81]:

$$X_j(t) = \frac{I}{P_{Str}} S_{mj}(t) + N_j(t) \quad (j=a,b,c) \quad (5.4)$$

where  $P_{Str}$  is the peak value of the triangular carrier  $S_{mj}$ , and  $N_j(t)$  consists of the switching harmonics of the carrier and the sidebands. It is assumed that the carrier frequency of  $S_{mj}$  is sufficiently high so that the frequency spectrum of  $N_j(t)$  is in the high frequency end of the spectrum so that it can be filtered by the inductances and the capacitances of the converter. Thus  $N_j(t)$  in Eq. (5.4) can be omitted. Thus the  $\bar{X}_j(t)$ , defined as the local average values of the Bi-Logic SPWM signals  $X_j(t)$ , is:

$$\bar{X}_j(t) = \frac{I}{P_{Str}} S_{mj}(t) \quad (j=a,b,c) \quad (5.5)$$

Substituting Eq. (5.5) into Eq. (5.2) and thereafter Eq. (5.2) into Eq. (5.1), the local average values of the ac terminal input currents of converter,  $\bar{i}_{pk}(t)$ , will be:

$$\bar{i}_{Pabc} = A [ C ] S_{Mabc} \quad (5.6)$$

where  $A = \frac{I_{dc}(t)}{2 P_{Str}}$ ,

$$\bar{i}_{Pabc} = [ \bar{i}_{pa}(t), \bar{i}_{pb}(t), \bar{i}_{pc}(t) ]^T,$$

$$\underline{S}_{Mabc} = [ S_{ma}(t), S_{mb}(t), S_{mc}(t) ]^T .$$

In the control design, the term  $A$  can be made to be constant through an auxiliary feedback loop, which makes the  $P_{str}$  proportional to the  $I_{dc}(t)$ . This is to keep the gain of the Tri-Logic PWM converter function constant regardless of the variation of dc link current  $I_{dc}(t)$ . Thus the currents  $\bar{i}_{pk}(t)$  ( $k=a, b, c$ ) are the linearly amplified (constant gain without phase shift) outputs of the modulating signals,  $S_{mj}(t)$ .

The top parts of Figs. 5-6 and 5-7, in Section 5.3.5, show the equivalent circuits of the current-source PWM converter based on Eq. (5.6). From the  $[C]$  matrix in Eq. (5.2) the ideal current sources,  $A \times S_{ma}(t)$ ,  $A \times S_{mb}(t)$  and  $A \times S_{mc}(t)$ , are connected in *delta*.

#### 5.3.4.1 Frequency Spectrum

Since Eq. (5.2) is a linear mapping, the spectrum of Tri-Logic PWM signal is a linear combination of the spectra from the Bi-Logic PWM signals. For example, the spectrum of the Tri-Logic PWM signal  $Y_a(t)$  is based on applying Eq. (5.2) to the spectrum (complex numbers) of the signals  $X_a(t)$  and  $X_b(t)$ . Fig. 5-5 (a) and (b) show respectively the spectrum (magnitudes) of the Bi-Logic PWM and Tri-Logic PWM for the case: SPWM modulating index  $M=0.8$ , triangular carrier frequency  $=21 \times 60 = 1260$  Hz. In Fig. 5-5(b), all the harmonics at integral multiples ( $n=1,3,\dots$ ) of the carrier frequency (1260 Hz) are eliminated. One set

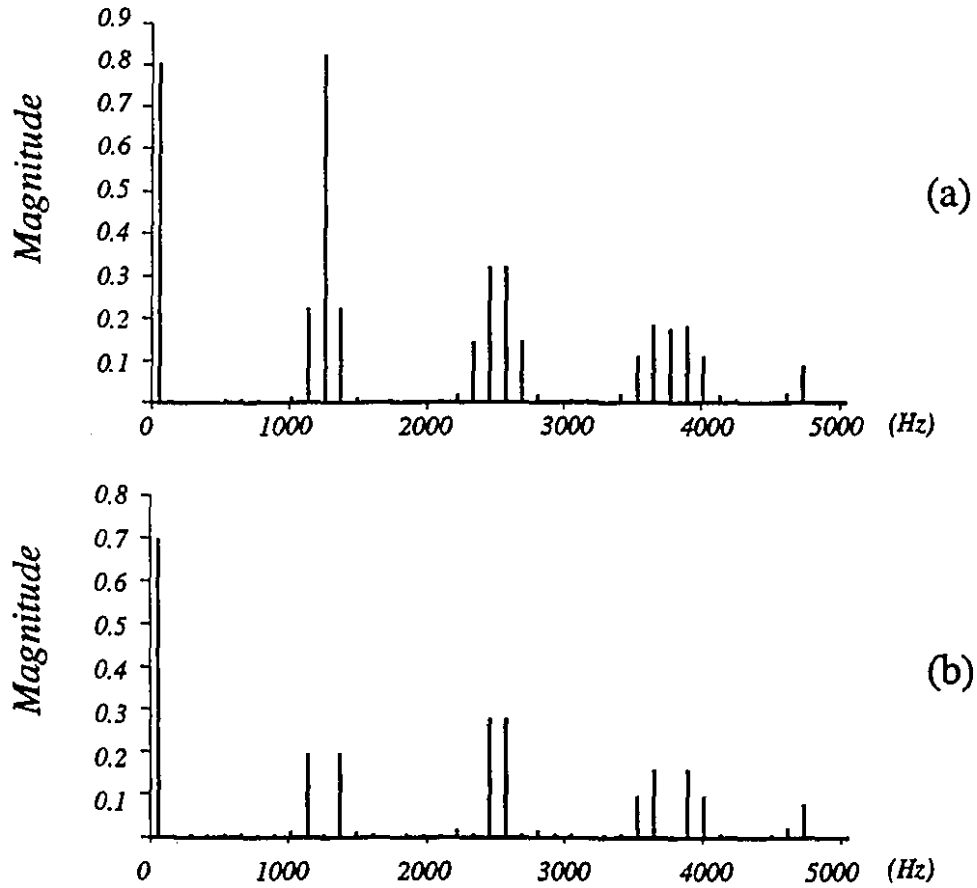


Figure 5-5 (a) Spectrum of Bi-Logic PWM signals  $X_j$ ,  
(b) Spectrum of Tri-Logic PWM signals  $Y_k$ .

of the sideband harmonics ( $2 \times 1260 \pm 2 \times 60$  Hz) is also eliminated.

### 5.3.5 Decoupler Pre-Processing

Because of the form of the  $[C]$  matrix in Eq. (5.2) the ideal current-source amplifiers,  $A \times S_{ma}(t)$ ,  $A \times S_{mb}(t)$  and  $A \times S_{mc}(t)$  are connected in *delta* as shown in

Figs. 5-6 and 5-7. Thus there is need for a *Decoupler Pre-Processor* block located as shown in Fig. 5-1, so that the input control signals,  $S_{pa}(t)$ ,  $S_{pb}(t)$  and  $S_{pc}(t)$ , can control the local average values of the converter ac terminal currents  $\bar{i}_{pa}(t)$ ,  $\bar{i}_{pb}(t)$ , and  $\bar{i}_{pc}(t)$  directly.

It is proposed that the Decoupler Pre-Processor consists of a transformation by a  $3 \times 3$  constant matrix  $[D]$  which relates the input control signals  $\underline{S_{Pabc}} = [S_{pa}(t), S_{pb}(t), S_{pc}(t)]^T$  to the modulating signals  $\underline{S_{Mabc}}$  by the equation:

$$\underline{S_{Mabc}} = [D] \underline{S_{Pabc}} \quad (5.7)$$

Substituting Eq. (5.7) into Eq. (5.6):

$$\bar{\underline{i_{Pabc}}} = A [C] [D] \underline{S_{Pabc}} \quad (5.8)$$

The desirable result is:

$$\bar{\underline{i_{Pabc}}} = A \underline{S_{Pabc}} \quad (5.9)$$

Thus, it is required that  $[D] = [C]^{-1}$ .

The determinant of matrix  $[C]$  in Eq. (5.3) is zero, meaning that the rank of the  $3 \times 3$  matrix  $[C]$  is less than 3 and there is no inverse. The result of Eq. (5-9) can be achieved if the rank is increased. This is done by first defining:

$$[D] = \frac{1}{3} [C]^T \quad (5.10)$$

Substituting Eq (5.10) into Eq. (5.8), one has:

$$\bar{i}_{pabc} = A \underline{S}_{pabc} - \underline{S}_o \quad (5.11)$$

where  $\underline{S}_o = [S_o(i), S_o(t), S_o(t)]^T$  and  $S_o(t) = (S_{pa}(t) + S_{pb}(t) + S_{pc}(t))/3$ .

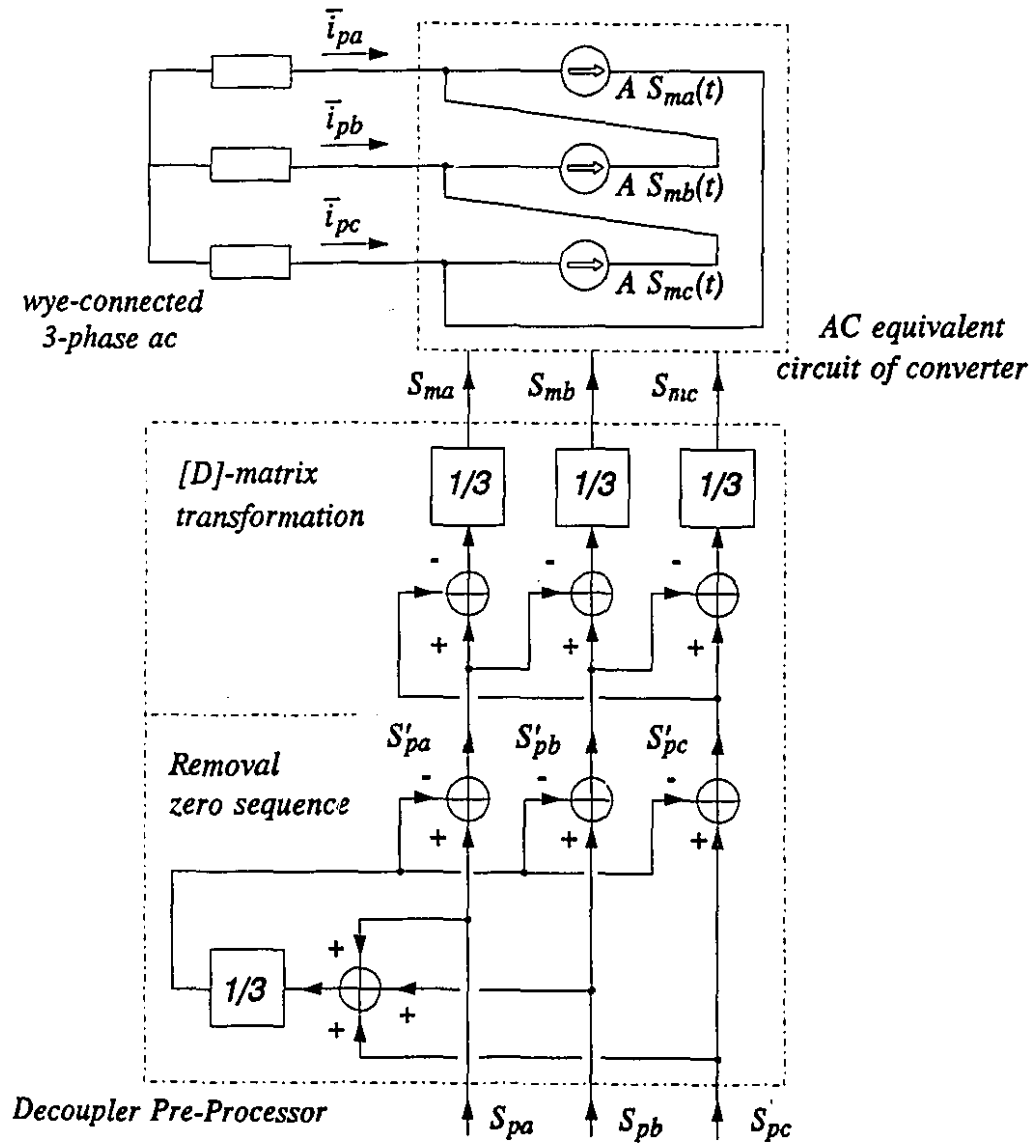


Figure 5-6 Decoupler Pre-Processor for wye-connected 3-phase ac.

### 5.3.5.1 WYE-Connected 3-Phase AC

The result of Eq. (5.9) is possible when  $\underline{S}_o = \underline{0}$  in Eq. (5.11). In power engineering, this constraint is equivalent to requiring that the zero sequence does not exist.

Fig. 5-6 is the schematic of the Decoupler Pre-processor for the converter which has an isolated neutral, wye-connected 3-phase ac line circuits. The input control signals,  $S_{pa}(t)$ ,  $S_{pb}(t)$ ,  $S_{pc}(t)$ , pass through a first stage which removes the zero sequence component. The intermediate signals, bearing a prime, satisfy  $S_o(t) = (S'_{pa}(t) + S'_{pb}(t) + S'_{pc}(t))/3 = 0$ . The next stage consists of realizing Eq. (5.7) where the matrix  $[D]$  is given by Eq. (5.10). Thus each of three phase currents,  $\bar{i}_{pk}(t)$ , is completely controlled by the control input signals,  $S_{pj}(t)$ , independently.

Since there cannot be a zero sequence current flowing in this isolated neutral, wye-connected circuit, setting  $S_o(t) = 0$  does not introduce any error.

### 5.3.5.2 DELTA-Connected 3-Phase AC

When the 3-phase ac sources and the  $L$ - $C$  circuits are *delta*-connected, as shown in Fig. 5-7, the ac terminal currents,  $\bar{i}_{pk}(t)$ , are related to the three ac phase currents,  $i_u(t)$ ,  $i_v(t)$ ,  $i_w(t)$ , by the equation:

$$\bar{i}_{Pabc} = [C] \underline{i}_{uvw} \quad (5.12)$$

where  $\underline{i}_{uvw} = [i_u(t), i_v(t), i_w(t)]^T$ .

By subtracting Eq. (5.6) from Eq. (5.12), the result is:

$$[C] (\underline{i}_{uvw} - A \underline{S}_{Mabc}) = 0 \quad (5.13)$$

As the  $3 \times 3$  matrix  $[C]$  in Eq. (5.13) has a zero determinant, it is necessary that:

$$i_u(t) + i_v(t) + i_w(t) = 0 \quad (5.14)$$

$$S_{ma}(t) + S_{mb}(t) + S_{mc}(t) = 0 \quad (5.15)$$

before  $i_u(t)$ ,  $i_v(t)$ ,  $i_w(t)$  can be controlled directly in the decoupled way.

As shown in Fig. 5-7, the Decoupler Pre-Processor removes the zero sequence components from the input signals  $S_{pj}(t)$  so that Eq. (5.15) can be

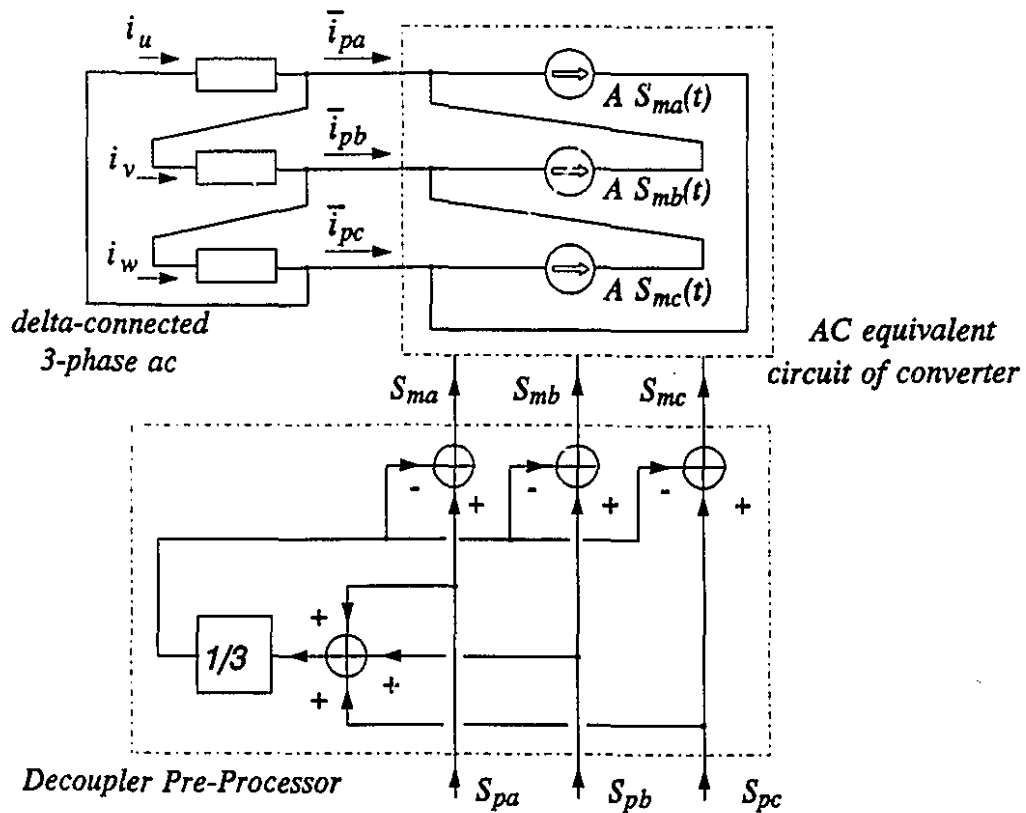


Figure 5-7 Decoupler Pre-Processor for *delta*-connected 3-phase ac.

satisfied. However, if there exists a zero sequence current,  $i_o(t)$ , which circulates around the *delta* loop of the 3-phase ac circuits, it cannot be controlled.

The extent of decoupled control attainable is:

$$\underline{i}_{uvw} = A \underline{S}_{Pabc} + \underline{i}_o \quad (5.16)$$

where  $\underline{i}_o = [i_o(t), i_o(t), i_o(t)]^T$

## 5.4 Summary

This chapter has presented the Dynamic Tri-Logic PWM strategy which is translated from any 3-phase Bi-Logic SPWM signals. The Tri-Logic PWM fits the operational requirements of the 6-valve, 3-phase, current-source PWM converter. In the implementation of the switchings of the valves as controlled by the Dynamic Tri-Logic PWM, the state transition involving a single switching operation only is permitted. The Dynamic Tri-Logic PWM provides the converter with the characteristics of linear amplifiers, with the frequency bandwidth restricted by the frequency of the carrier frequency. The decoupled control over each of the three phases of the current-source PWM converter has been achieved by applying the Pre-Processing Stage to the inputs.

The next chapter will describe a design of the digital control for the current-source PWM converter using the proposed Dynamic Tri-Logic PWM strategy. The digital controller is based on multi-DSP in parallel for the computation of Pole-Placement algorithms.



## MULTI-DSP REAL-TIME CONTROL

### 6.1 Introduction

The previous chapter has identified four difficulties inherent in the 6-valve, 3-phase, current-source PWM converter. In order to overcome the main difficulties the converter has to operate under Tri-Logic PWM strategy. The Dynamic Tri-Logic SPWM strategy and the Decoupler Pre-Processor have been presented in **Chapter 5**.

The present chapter develops and describes a new digital control scheme based on the Pole Placement method to solve the remaining control difficulties caused by the ac capacitors. These are: (1) the stable operating region which is too limited, (2) the  $L$ - $C$  resonance from the ac capacitors. The current-source converter is provided with a current snubber circuit as protection against

$L_{dc}dI_{dc}/dt$  voltage.

In applying the Pole-Placement method, the following innovative approaches have been followed:

- (1) The mathematical equations are formulated in such a way that each of the three ac phases is treated independently and separately. This formulation is possible because the Decoupler Pre-Processor enables PWM converter to operate as three independent linear amplifiers.
- (2) The entire control task has been implemented digitally. So far, the success of digital controls has been limited to relatively slow processes, such as in robotics and in chemical engineering. The challenge here is to realize a completely digital controller for the PWM converters and to find out what are the key parameters for the successful implementation. A very important conclusion from the research is that the frequency bandwidth needed for the pole-placement feedback is very intolerant of computational delays. To hasten the computation, the pole-placement algorithms were executed by two Texas Instrument TMS320C25 Digital Signal Processors in parallel with a clock frequency of 40 MHz.

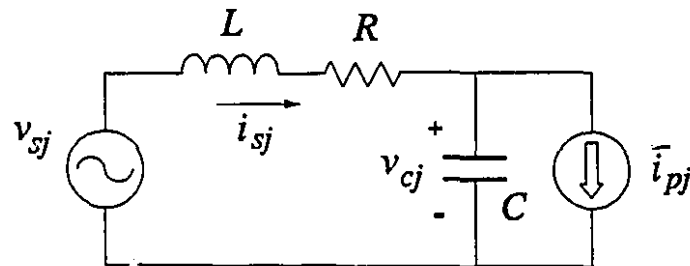
In proving the concepts of Chapter 5 and the control methods of this chapter, a 1-KVA size, 6-valve (Bipolar Transistor), 3-phase, Current-Source PWM Converter was constructed. The digital controller used, was a multi-DSP controller which had been designed and constructed in our laboratory.

The following functions were specified for the Current-Source PWM converter:

- (1) operate as a stand-alone Rectifier,
- (2) DC-side: Close regulation of dc link current. Fast response to dc link current reference setting.
- (3) AC-side: Near sinusoidal current at unity power factor. Active filtering capability.

## 6.2 Mathematical Model

As Eq. (5.9) can be achieved by using the Dynamic Tri-Logic SPWM scheme with the Decoupler Pre-Processor stage, the ac side of the current-source PWM converter of Fig. 5-1 in previous chapter can be simply modelled as three separate, decoupled linear amplifiers of the control input signals,  $S_{pj}(t)$  ( $j=a, b, c$ ). Any one of the three phases of the converter can be separately represented by the



**Figure 6-1** Single phase equivalent ac circuit of the current-source PWM converter. ( $j=a, b, c$ )

single phase equivalent circuit shown by Fig. 6-1.

In Fig. 6-1,  $v_{sj}(t)$ ,  $j=a, b, c$  for each of the three phases, is the phase-neutral ac voltage source. Each phase of the PWM converter is modelled as the equivalent current source with the value of  $\bar{i}_{pj}(t)$ . The switching harmonics in the converter terminal current, will be neglected. By judicious design they are filtered out sufficiently by the inductances and the capacitances of the converter.

Each ac phase circuit can be simply controlled by the equivalent linear amplifier,  $\bar{i}_{pj}(t) = A \times S_{pj}(t)$ , using a linear combination of the current and the voltage feedback signals of that phase. This approach has the distinct advantage in reducing the order of the system equations and in shortening the computational delays. Compared with other methods [47,48] which require the *Park's* power invariant transformation [88] from the *a-b-c* frame to the *d-q* frame, to be followed by an inverse transformation back to the *a-b-c* frame again, the computation burden is less. Furthermore the *d-q* frame equations are not decoupled.

In the circuit of Fig. 6-1, by choosing the ac line current,  $i_{sj}(t)$ , and the capacitor voltage,  $v_{cj}(t)$ , as the system state variables, the state-space description of the circuit is:

$$\begin{bmatrix} \frac{d}{dt} i_{sj}(t) \\ \frac{d}{dt} v_{cj}(t) \end{bmatrix} = \begin{bmatrix} -\frac{R}{L} & -\frac{1}{L} \\ \frac{1}{C} & 0 \end{bmatrix} \begin{bmatrix} i_{sj}(t) \\ v_{cj}(t) \end{bmatrix} + \begin{bmatrix} 0 \\ -\frac{1}{C} \end{bmatrix} \bar{i}_{pj}(t) + \begin{bmatrix} \frac{v_{sj}(t)}{L} \\ 0 \end{bmatrix} \quad (6.1)$$

The output is:

$$i_{sj}(t) = \begin{bmatrix} 1 & 0 \end{bmatrix} \begin{bmatrix} i_{sj}(t) \\ v_{cj}(t) \end{bmatrix} \quad (j = a, b, c)$$

Removing the input term  $v_{sj}(t)$  by subtracting the steady-state operating values from Eq. (6.1), the small perturbation variable model is:

$$\begin{bmatrix} \frac{d}{dt} \Delta i_{sj}(t) \\ \frac{d}{dt} \Delta v_{cj}(t) \end{bmatrix} = \begin{bmatrix} -\frac{R}{L} & -\frac{1}{L} \\ \frac{1}{C} & 0 \end{bmatrix} \begin{bmatrix} \Delta i_{sj}(t) \\ \Delta v_{cj}(t) \end{bmatrix} + \begin{bmatrix} 0 \\ -\frac{1}{C} \end{bmatrix} \Delta \bar{i}_{pj}(t) \quad (6.2)$$

$$\Delta i_{sj}(t) = \begin{bmatrix} 1 & 0 \end{bmatrix} \begin{bmatrix} \Delta i_{sj}(t) \\ \Delta v_{cj}(t) \end{bmatrix} \quad (j = a, b, c)$$

or

$$\frac{d}{dt} \Delta \underline{x}_j(t) = [A] \Delta \underline{x}_j(t) + [B] \Delta u_j(t)$$

$$\Delta y_j(t) = [C] \Delta \underline{x}_j(t)$$

$$(j = a, b, c)$$

where, the small perturbation variables are defined as:

$$\Delta i_{sj}(t) = i_{sj}(t) - i_{sjo}(t)$$

$$\Delta v_{cj}(t) = v_{cj}(t) - v_{cjo}(t) \quad , \quad (j = a, b, c) \quad (6.3)$$

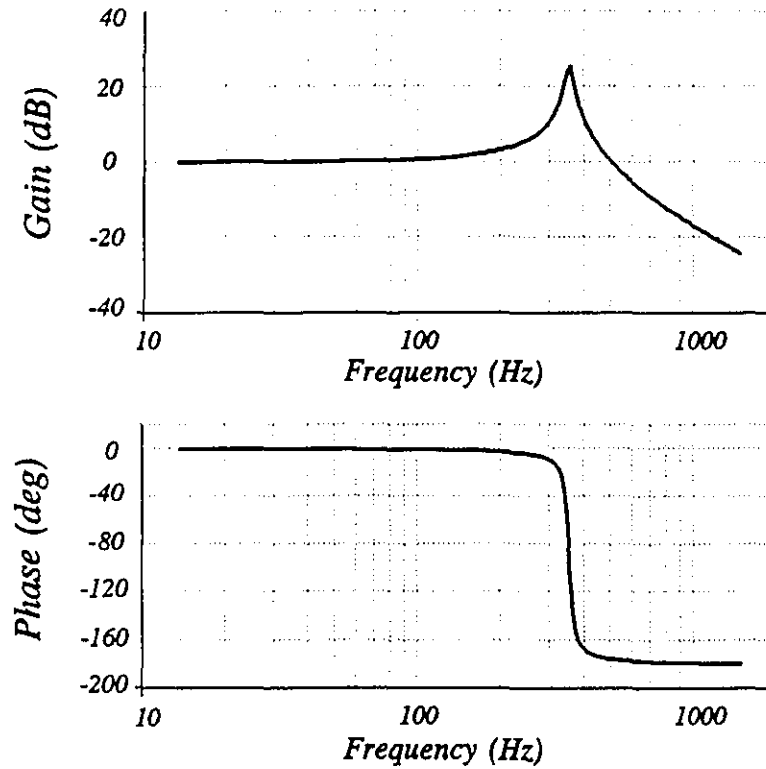
$$\Delta \bar{i}_{pj}(t) = \bar{i}_{pj}(t) - \bar{i}_{pjo}(t)$$

and,  $i_{sjo}(t)$ ,  $v_{cjo}(t)$  and  $\bar{i}_{pjo}(t)$  are the steady-state operating values of the ac line current, the capacitor voltage and the equivalent current source respectively.

### 6.3 Control Difficulties

From Eq. (6.2), one sees that the first row element in the vector  $[B]$  is zero so that the ac line currents,  $\Delta i_{sj}(t)$ , cannot be directly controlled by the input variables  $\Delta \bar{i}_{pj}(t)$ . The adjustment of the ac line current is delayed by one order compared with the control performance in the voltage-source topology [89]. Physically, this is a consequence of the capacitor  $C$  connected directly across the ac terminals of the converter. For adjusting the ac line current, the converter needs to inject the right amount of charging current to the ac capacitor so as to make the capacitor voltage correctly compensate for the voltage drops across the  $R$  and  $L$  of the line. During the transient period, in order to compensate for the  $L di_{sj}(t)/dt$  voltage drop across the line inductance, the converter current  $\bar{i}_{pj}(t)$  has to include the capacitor charging current component which must contain the second derivative  $C d^2 i_{sj}(t)/dt^2$ . However, this task is difficult to implement as the  $d^2/dt^2$  operator introduces noise and cannot be used in the control circuit.

Another control difficulty is shown by Fig. 6-2 which plots the open-loop frequency response of  $\Delta y(s)/\Delta u(s)$  from Eq. (6.2) for the converter parameters listed in Table 6-1 of Section 6.6. Since in high power applications the switching rates of the valves have to be lowered so as to reduce switching losses, the choice of  $L$ - $C$  resonance frequency is pushed into the low frequency end. In the design example, there is a resonance peak close to 5th harmonic frequency in Fig. 6-2. Because of the 5th, 7th and other odd harmonics from the ferromagnetic



**Figure 6-2** Open-loop frequency response of the system showing  $L$ - $C$  resonance.

nonlinearity of the ac voltage source and the switching harmonics from the converter, the resonance will cause serious low order harmonic distortions on the ac line currents under steady-state operation condition.

During transients, the oscillations of the  $L$ - $C$  resonance will persist unless there is adequate damping. From Eq. (6.2) the system poles are calculated as:

$$P_{1,2} = -\frac{R}{2L} \pm j \frac{\sqrt{4LC - R^2C^2}}{2LC} \quad (6.4)$$

It can be seen that on the  $S$ -plane, the resonance performance corresponds to one

pair of the low damping poles being located near the imaginary axis. The damping factor  $\xi = R\sqrt{C}/2\sqrt{L}$  is low, as the ratio of  $R/L$  is small in most rectifier systems.

## 6.4 Control Strategy

To solve the above control difficulties, the *Pole Placement* control strategy from the modern control theory [90] is proposed to improve the dynamic performance characteristics of the circuit. By calculating the controllability of Eq. (6.2), it is known that the system of Eq. (6.2) is completely controllable for all possible steady-state operating points. Thus the low damping poles of the system can be moved to any desired locations by means of state feedback control. As defined by Eq. (6.3), the state vector  $\Delta \underline{x}_i(t)$  in Eq. (6.2) is the "error" between the ac line current and the ac capacitor voltage and their desired steady-state waveforms. By using the state-feedback technique, the  $\Delta \underline{x}_i(t)$  can be made converge to the origin at a faster rate determined by the Placement of the Poles. When the error  $\Delta \underline{x}_i(t) = \underline{0}$ , the ac line currents and the capacitor voltages are tracking their desired waveform templates. In maintaining  $\Delta \underline{x}_i(t) = \underline{0}$ , the harmonic distortions which arise from the interactions with the  $L$ - $C$  resonance frequency are suppressed, and the converter operates virtually as an *Active Filter*.

Considering the requirement of the complex calculations in realizing the Pole Placement control strategy, the decision is made to build a system controller



based on multi-DSPs (*Digital Signal Processors*) and parallel processing techniques in real-time.

### 6.4.1 Discretization of System Model

In implementing the digital control design, the continuous time system model of Eq. (6.2) needs to be transformed into the discrete-time system formulation.

Considering the *Zero-Order-Hold Sampling* [91,92] of Eq. (6.2) with the sampling period  $\Delta T$ , for the sampling instants  $t_k = k\Delta T$  ( $k=1, 2, 3\cdots$  denote the sampling sequence), the state at the next sampling time  $t_{k+1}$  is given by [91,92]:

$$\begin{aligned}\Delta \underline{X}_j(t_{k+1}) &= [G] \Delta \underline{X}_j(t_k) + [H] \Delta U_j(t_k) \\ \Delta Y_j(t_k) &= [C] \Delta \underline{X}_j(t_k)\end{aligned}\tag{6.5}$$

where  $\Delta \underline{X}_j(t_k) = [\Delta i_{sj}(t_k), \Delta v_{cj}(t_k), \Delta \bar{i}_{pj}(t_{k-1})]^T$ ,  $\Delta U_j(t_k) = \Delta \bar{i}_{pj}(t_k)$ , ( $j=a, b, c$ ),

$$G = \begin{bmatrix} e^{[A]\Delta T} & H_1 \\ 0 & 0 \end{bmatrix}_{3 \times 3}, \quad H = \begin{bmatrix} H_2 \\ I \end{bmatrix}_{3 \times 1}, \quad C = [1 \ 0 \ 0]_{1 \times 3}$$

It is assumed that there is a delay between the sampling instants ( $t_k$ ) of the feedback signal and the time needed to compute the control signal. This assumption is embedded in:

$$H_1 = e^{[A](l-m)\Delta T} \int_0^{m\Delta T} e^{[A]s} ds [B] \tag{6.5-a}$$

$$H_2 = \int_0^{(1-m)\Delta T} e^{[A]s} ds [B] \quad (6.5-b)$$

where  $m\Delta T$ , ( $0 \leq m \leq 1$ ), represents the computational delay. Because of this delay the discretized system model is increased by one order. This is necessary in the control design when the computational delay has a serious effect on the frequency bandwidth of the control system.

#### 6.4.2 Pole Placement Feedback Control

Fig. 6-3 shows the block diagram of the detailed closed-loop control as implemented for phase-*a*. The inner state feedback loop, which is enclosed by the dotted line box of "*feedback*", is used to stabilize the ac *L-C* resonance circuit and to improve its transient response. It ensures that the measured values of the ac line current and the capacitor voltage will track their waveform templates provided by the dotted line box of "*feed-forward*".

At the  $k$ th sampling instant ( $t=t_k$ ), the ac line current,  $i_{sa}(t_k)$ , and the capacitor voltage,  $v_{ca}(t_k)$ , are measured, and the state variables  $\Delta \underline{X}_a(t_k)$  are calculated, using Eq. (6.3). The control input variable  $S_{pa}(t_k)$  consists of two components:

$$S_{pa}(t_k) = \bar{i}_{pao}(t_k) + \Delta \tilde{U}_a(t_k) \quad (6.6)$$

$\bar{i}_{pao}(t_k)$  is computed from the feed-forward loop in order to meet the unity power factor requirement of the line current  $i_{sa}(t)$ . The control will be described

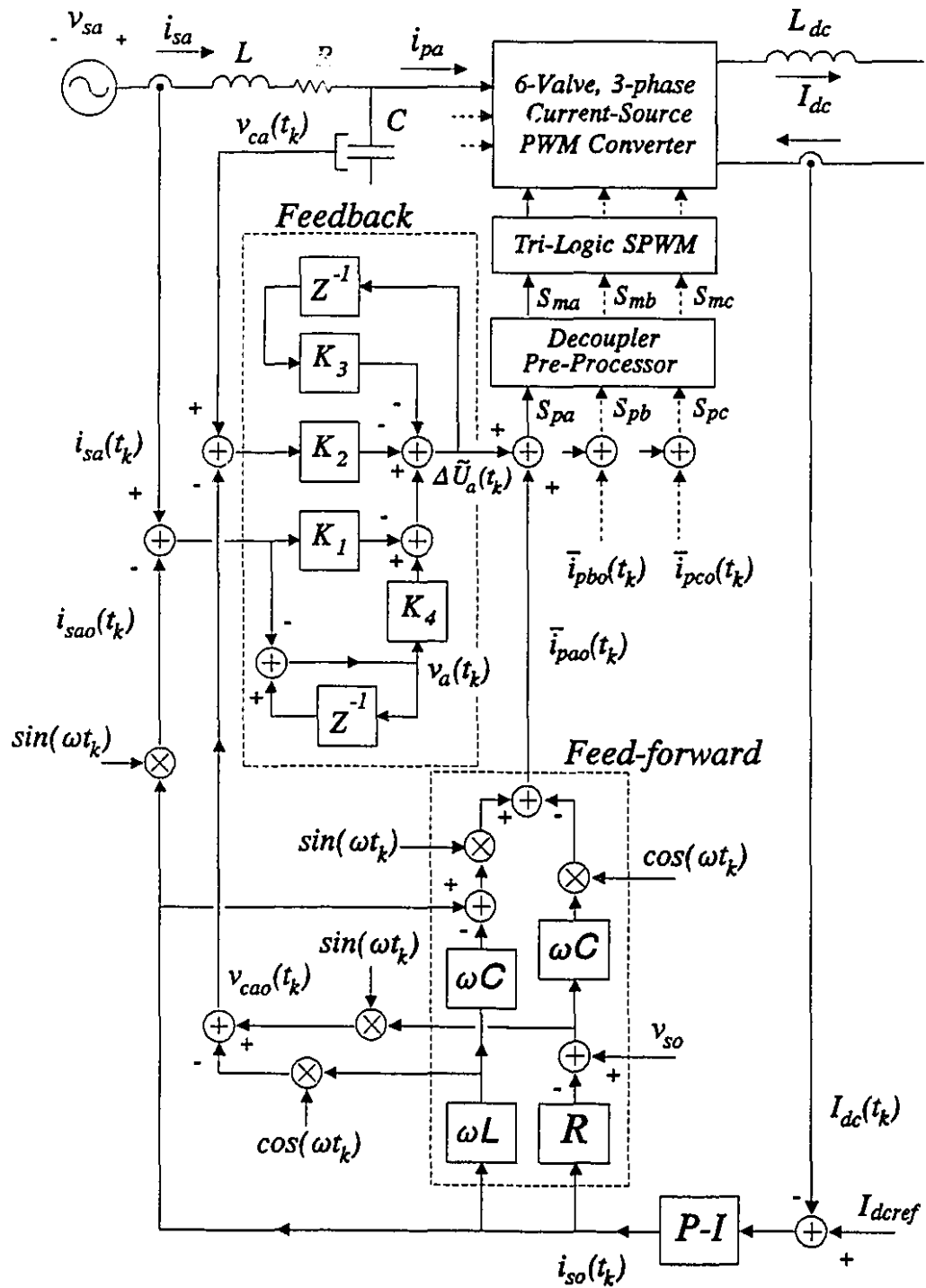


Figure 6-3 Pole Placement control scheme.

in the next section, Section 6.4.3.

$\Delta \tilde{U}_a(t_k)$  represents the state feedback control based on the Pole Placement control law:

$$\Delta \tilde{U}_a(t_k) = -[K_1, K_2, K_3] \Delta \underline{X}_a(t_k) + K_4 v_a(t_k) \quad (6.7)$$

where, the  $K_1$ ,  $K_2$  and  $K_3$  are the gains of the state feedback loop which are designed to move the poles of the system of Eq. (6.5) to the desired positions. It can be proved that Eq. (6.5) is keeping the complete controllable characteristic after it has been discretized from Eq. (6.2) with the sampling period  $\Delta T = 397 \mu s$ , which will be used later in the experiments described in Section 6.6, so that one can apply a pole placement technique. The additional term:

$$v_a(t_k) = v_a(t_{k-1}) - \Delta i_{sa}(t_k) \quad (6.8)$$

is an integral tracking control loop with the gain  $K_4$ , which is chosen to minimize the error between the ac line current,  $i_{sa}(t)$ , and its waveform template,  $i_{sao}(t)$ . This control is necessary when the system model parameters are not accurately known.

In the control implementation, the gain in the equivalent linear amplifier  $\bar{i}_{pa}(t) = A \times S_{pa}(t)$ , described in Section 5.3.4, is chosen as  $A=1$ , so that the feedback control signal  $\Delta \tilde{U}_a(t_k) \equiv \Delta U_a(t_k)$ . Denoting  $t_k$  by  $k$  and  $[K_1 \ K_2 \ K_3]$  by  $K_{1-3}$ , and substituting Eqs. (6.8) and (6.5) into Eq. (6.7),  $\Delta U_a(k+1)$  ( or  $\Delta U_a(t_{k+1})$  ) can be solved as:

$$\begin{aligned}
 \Delta U_a(k+1) &= K_4 [v_a(k) - [C] ([G] \Delta \underline{X}_a(k) + [H] \Delta U_a(k))] \\
 &\quad - K_{I-3} ([G] \Delta \underline{X}_a(k) + [H] \Delta U_a(k)) \\
 &= \Delta U_a(k) + K_{I-3} \Delta \underline{X}_a(k) \\
 &\quad - (K_4 [C] + K_{I-3}) ([G] \Delta \underline{X}_a(k) + [H] \Delta U_a(k))
 \end{aligned} \tag{6.9}$$

Together with Eq. (6.5), the closed-loop system equations for each of the three phases are:

$$\begin{aligned}
 \begin{bmatrix} \Delta \underline{X}_j(k+1) \\ \Delta U_j(k+1) \end{bmatrix} &= \begin{bmatrix} G & H \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \Delta \underline{X}_j(k) \\ \Delta U_j(k) \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} W_j \\
 j &= a, b, c
 \end{aligned} \tag{6.10}$$

where, the state feedback input  $W_j$  is:

$$\begin{aligned}
 W_j &= -K_s \begin{bmatrix} \Delta \underline{X}_j(k) \\ \Delta U_j(k) \end{bmatrix} = [S_1 \ S_2] \begin{bmatrix} \Delta \underline{X}_j(k) \\ \Delta U_j(k) \end{bmatrix} \\
 j &= a, b, c
 \end{aligned} \tag{6.11}$$

and  $S_1 = K_{I-3} ([I] - [G]) - K_4 [C] [G]$

$$S_2 = I - K_{I-3} [H] - K_4 [C] [H]$$

It can be shown that if Eq. (6.5) is completely controllable, Eq. (6.10) is also completely controllable. The gain vector  $K_s = -[S_1 \ S_2]$  can be solved by applying Ackermann's formula [91,92]:

$$K_s = [0 \ 0 \ 0 \ 1] [C_t]^{-1} P([\bar{G}]) \tag{6.12}$$

where,

$$[\bar{G}] = \begin{bmatrix} G & H \\ 0 & 0 \end{bmatrix}$$

is the system matrix of Eq. (6.10), and  $P(\bullet)$  is closed-loop system characteristic polynomial with desired pole locations, and  $[C_t]$  is the controllability matrix of Eq. (6.10). Thus the state feedback gains  $K_4$  and  $K_{1-3}$  can be found from Eq. (6.11):

$$K_s = [K_{1-3} \ K_4] \begin{bmatrix} [G] - [I] & [H] \\ [C][G] & [C][H] \end{bmatrix} - [0 \ 0 \ 0 \ 1] \quad (6.13)$$

Therefore,

$$[K_1 \ K_2 \ K_3 \ K_4] = (K_s + [0 \ 0 \ 0 \ 1]) \begin{bmatrix} [G] - [I] & [H] \\ [C][G] & [C][H] \end{bmatrix}^{-1} \quad (6.14)$$

As the system model is completely controllable, in theory it is possible to assign the desired closed-loop system poles to any position on the Z-plane. The "deadbeat" control scheme [91,92], which is accomplished by placing all the poles at the zero of the Z-plane, is the desired way to achieve fast transient response. However, in practice this may not be realizable because of the "saturation" limits on the magnitudes of the control inputs. In particular in the SPWM function of Fig. 5-1 in previous chapter, the modulating signals,  $S_{ma}(t)$ ,  $S_{mb}(t)$  and  $S_{mc}(t)$ , must be less than the peak value of the triangular carrier signal  $S_r(t)$ . From the laboratory experience, the assignment of the poles too close to the zero of the Z-plane has, in fact, led to instability.

Since the damping factors of poles of Eq. (6.5) are mainly determined by

the time constant  $L/R$ , in the control design, the desired closed-loop system poles have been chosen by substituting as large as possible the value of the resistance  $R$  into Eq. (6.5), and using corresponding eigenvalues as the ideal closed-loop system pole positions.

### 6.4.3 Unity Power Factor Feed-Forward Control

To achieve unity power factor control, the steady-state converter terminal current,  $\bar{i}_{pao}(t_k)$ , has been determined from the steady-state solutions of Eq. (6.1) when the ac source voltage  $v_{so}$  and the system parameters  $L$  and  $C$  are known. This is done in the dotted line box labelled "feed-forward" in Fig. 6-3.

Assuming the  $a$ -phase ac supply voltage is:

$$v_{sa}(t) = v_{so} \sin(\omega t - \theta_a) \quad (6.15)$$

for unity power factor operation the desired ac line current waveform template is:

$$i_{sao}(t_k) = i_{so}(t_k) \sin(\omega t_k - \theta_a) \quad (6.16)$$

where,  $\theta_a$  is a phase angle and  $v_{so}$  is the peak value of ac voltage source. The quantity,  $i_{so}(t_k)$ , is the instantaneous peak value of the ac 3-phase line current templates. Substituting Eqs. (6.15) and (6.16) into Eq. (6.1), for constant value of  $i_{so}(t_k)$ , the steady-state solution of the capacitor voltage template,  $v_{cao}(t_k)$ , is given by:

$$\begin{aligned} v_{cao}(t_k) = & (v_{so} - R i_{so}(t_k)) \sin(\omega t_k - \theta_a) \\ & - \omega L i_{so}(t_k) \cos(\omega t_k - \theta_a) \end{aligned} \quad (6.17)$$

Therefore, the steady-state converter terminal current,  $\bar{i}_{pao}(t_k)$ , can be obtained through the equation:

$$\begin{aligned}\bar{i}_{pao}(t_k) &= i_{sao}(t_k) - C \frac{d}{dt} v_{cao}(t_k) \\ &= (1 - \omega^2 LC) i_{so}(t_k) \sin(\omega t_k - \theta_a) \\ &\quad - \omega C (v_{so} - R i_{so}(t_k)) \cos(\omega t_k - \theta_a)\end{aligned}\tag{6.18}$$

As shown in Fig. 6-3, the current amplitude  $i_{so}(t_k)$  comes from the current regulation  $P$ - $I$  (Proportional and Integral) control block in the outer feedback control loop. The function of the outer dc current regulation loop is to null the error between the dc link current  $I_{dc}(t)$  and its reference setting  $I_{dcref}$ . When this error appears, it is used to adjust the magnitude of the line current command  $i_{so}(t_k)$ . Through Eq. (6.18),  $i_{so}(t_k)$  adjusts  $\bar{i}_{pao}(t_k)$  in magnitude and in phase angle so as to make the converter increase or decrease the transmitted power while preserving unity power factor operation.

In the "feed-forward" control loop of Fig. 6-3, the in-phase and the in-quadrature references,  $\sin(\omega t_k)$  and  $\cos(\omega t_k)$ , are from the sinusoidal waveform generators which are synchronized with the ac voltage sources.

Only the  $a$ -phase control implementation is shown. The  $b$  and  $c$ -phases are identical except that their in-phase and the in-quadrature references are shifted by  $-120^\circ$  and  $-240^\circ$  respectively.



#### 6.4.4 Frequency Bandwidth

The above Pole Placement control design is realizable because the Dynamic Tri-Logic PWM scheme and the Decoupler Pre-Processor, introduced in pervious chapter, enable each modulating signal to control its ac phase as a linear amplifier. However, the frequency bandwidth of this equivalent linear amplifier needs to be considered to ensure that the feedback can be implemented successfully.

From the theory of Sinusoidal PWM, it is known that for the modulating index  $M \leq 1$ , the frequency bandwidth of linear amplification in the SPWM strategy is up to  $1/3$  of the triangular carrier frequency [61,87]. Therefore, for active filtering of the low order harmonics in the ac circuits (up to the 7<sup>th</sup> harmonic in our design), the lowest triangular carrier frequency used to encode the bi-logic PWM signals in Fig. 5-1 of Chapter 5 should satisfy with the formula  $f_r \geq (3 \times 7)f_o$  Hz ( $f_o$  is the line frequency).

In the adopted control design philosophy, the circuit  $L$ - $C$  resonance frequency is chosen to be low enough with respect to the PWM triangular carrier frequency so that it falls within the frequency bandwidth of the equivalent linear amplifier. Although the  $L$ - $C$  resonance frequency interacts with the low order harmonic sources, the state-feedback control loops can react fast enough so as to ensure  $\Delta \underline{X}_j(t) = \underline{0}$ . As such the  $L$ - $C$  resonance is suppressed.

Another factor affecting the frequency bandwidth of the feedback control loop is related to the choice of the sampling frequency and the computational delays,  $m\Delta t$  of Eqs. (6.5-a) and (6.5-b) [91,92] in the digital controller. In the digital control, the SPWM strategy is implemented by the "four timer" [93] method in which the control sampling instants are taken at each of the extremum points on the SPWM triangular carrier waveform. Thus the sampling frequency is fixed at twice the triangular carrier frequency. In high power applications where the switching losses of the valves can be considerable, it is necessary to maintain high efficiency by reducing the switching frequency. In such situations, one suffers a loss of control frequency bandwidth. For this reason it is critical that there should not be any further encroachment on the frequency bandwidth because of the computational delays. For example, from the experiments it was found that using the sampling time period as the delay (this corresponds to  $m=1$  in Eqs. (6.5-a) and (6.5-b)) had led to system instability. Therefore, the control command was executed as soon as the numerical computations were completed. The computational delay was:  $m=0.2$  in Eqs. (6.5-a) and (6.5-b). The following methods have been used to minimize the computational delays:

- (1) The control feedback algorithm is chosen to minimize the computational time. By using the system model in the  $a-b-c$  frame, one avoids the calculations of the transformations from the  $a-b-c$  frame to the  $d-q$  frame and the inverse transformations back to the  $a-b-c$  frame. Because of the wye connection on ac side of converter, the feedback controls on only two

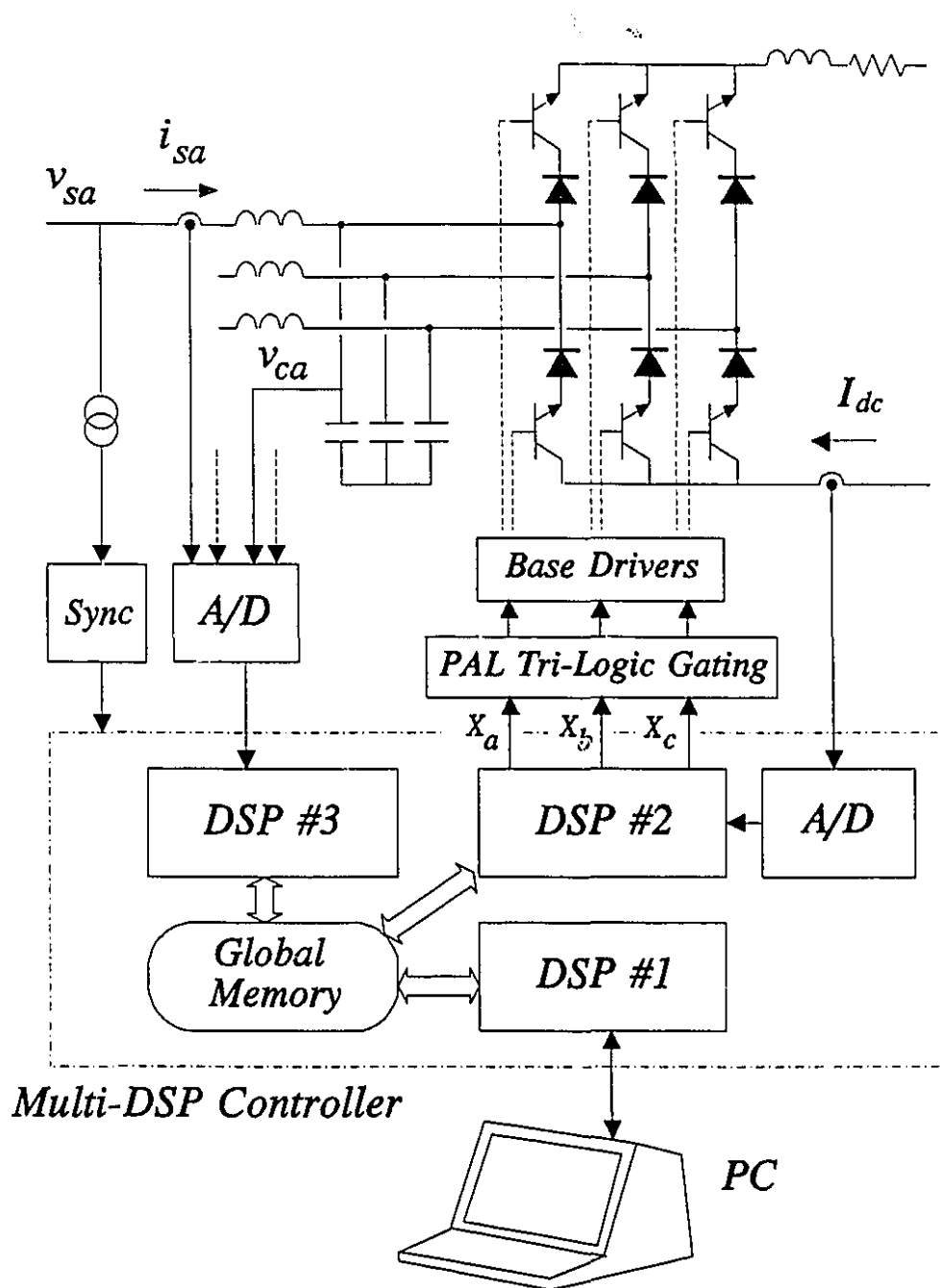
of the ac phases are calculated.

- (2) The digital controller is implemented by using fast, parallel Digital Signal Processors. (see Section 6.5)
- (3) Programmable Array Logic (PAL) is used to implement the Tri-Logic Gating. (see Appendix B).

## 6.5 Multi-DSP Control

High performance, fast Digital Signal Processors (DSPs) and parallel processing techniques provide the system controller with very powerful computational capabilities. In meeting the requirement to reduce computational delays so as to obtain a broad frequency bandwidth in the digital feedback control loop, a real-time multi-DSP controller is employed to implement the control schematic of Fig. 6-3. Fig. 6-4 shows the hardware design of the multi-DSP controller.

The *Multi-DSP Controller* of Fig. 6-4 has been designed and implemented in the Power Electronics Laboratory of McGill University, and has been used as a digital controller for PWM converters for a variety of applications [94-96]. As shown in Fig. 6-4, the Multi-DSP Controller consists of three high-speed DSPs (*Texas Instrument TMS320C25s*) operating independently in parallel. Each of DSPs has its own local program and data memories, and operates at 40 MHz clock frequency. The operations of the three DSPs are synchronized by using the



**Figure 6-4** Hardware configuration of current-source PWM converter with multi-DSP controller.

interrupt signals and a hardware synchronization circuit (which is not shown in Fig. 6-4). During real-time operation, the parameters for the calculations and data are exchanged between the DSPs through a 3-port global memory.

The outputs of the Multi-DSP Controller have to be converted into base drive signals to activate the valves of the converter which operate under the Tri-Logic SPWM strategy described in Chapter 5. This is accomplished by the *PAL* (Programmable Array Logic) *Tri-Logic Gating* hardware circuit which is connected between the current-source PWM converter and the Multi-DSP Controller. It transforms the Bi-Logic SPWM signals,  $X_a(t)$ ,  $X_b(t)$  and  $X_c(t)$ , which are generated from the Multi-DSP Controller, into the Tri-Logic PWM signals based on Eq. (5.2). It has also the duty to store temporarily in the memory the Tri-Logic state sequence and then from its historical context to choose the *shoot-through* state (#D, #E or #F of Table 5-3) automatically. This depends on the programmed logic, which has been designed to fulfil the requirement of state contiguity embodied in Fig. 5-4 of Section 5.3.3. Its output trigger signals are sent to the converter valves through the *Base Drivers* circuit. The design details of the *PAL Tri-Logic Gating* circuit are described in **Appendix B**.

To access the feedback state signals of the new Pole Placement control strategy of Fig. 6-3, two current transducers and two voltage transducers measure the instantaneous ac line currents and capacitor voltages of two of wye connected ac phases. There is an additional current transducer to measure the dc current

for the outer current regulator loop.

The "Sync" block in Fig. 6-4 is a zero-crossing detection circuit for measuring the ac source voltage phase angle. Using it as a phase reference, a software implemented *Phase Lock Loop* (PLL) produces the in-phase and the in-quadrature sinusoidal reference waveforms,  $\sin(\omega t_k)$  and  $\cos(\omega t_k)$ , in the "feed-forward" control block of Fig. 6-3. The sinusoidal reference waveforms are synchronized with the ac voltage source.

A *Personal Computer* (PC) is connected to the Multi-DSP Controller through a serial communication channel, by which the control program codes can be down-loaded to each of the DSPs and the control parameters can be modified and displayed during the real-time control.

In order to shorten the computational delay time  $m\Delta T$  in Eq. (6.5), all the computation tasks to implement the feedback control shown in Fig. 6-3 have been evenly shared between DSP #2 and DSP #3, and executed in parallel. The DSP #1 has been mainly used to exchange the control parameters and the converter status signals with the PC during operation.

The control program of each DSP is divided into several computational stages in the duration of a sampling period. When all three DSP have completed the calculation of one stage, they exchange intermediate results through the global memory, and then continue the calculations of the next stage. The three DSPs

operate synchronously under the controls of the synchronization circuit which ensure that the stage-by-stage parallel calculations are kept in step.

The control programs have been written in the assembler language. 16-bit fixed-point arithmetic operations have been used. The details on the sharing of the control tasks and the programs by each DSP are described in **Appendix C**.

## 6.6 Experimental Results

A 1-kVA size laboratory model of the bipolar transistor current-source PWM converter bridge using the multi-DSP controller, as shown in Fig. 6-4, has been constructed. Tests have been conducted for the verifications of the proposed Dynamic Tri-Logic PWM trigger method, the Decoupler Pre-Processor and the Pole Placement control schemes under the rectifier mode of operation.

The parameters of the current-source PWM rectifier used in the experiments are shown in Table 6-1. On the dc side, a resistance load is

**Table 6-1** Current-Source PWM Converter Parameters.

Converter Bridge Parameters		
$v_s = 70 \text{ V}_{rms}$	$\omega L = 2.5 \text{ ohm}$	$L_{dc} = 200 \text{ mH}$
$C = 30 \text{ } \mu\text{F}$	$R = 0.8 \text{ ohm}$	$R_{dc} = 0.5 \text{ ohm}$

connected. On the ac side, the circuit  $L$ - $C$  resonance frequency is chosen to be 357 Hz which is close to the 5th harmonic.

In the experiment, the software of the "four timer" method [93] is used to implement the Bi-Logic SPWM function of Fig. 5-1. The number of carrier triangular is set as 21 per modulating signal period. In the multi-DSP controller, the sampling frequency is chosen to be twice of the triangular carrier frequency,  $60 \times 21 \times 2 = 2520$  Hz (sampling period  $\Delta T = 397 \mu\text{s}$ ). In each sampling period, the control programs of the three DSPs are executed in parallel through seven

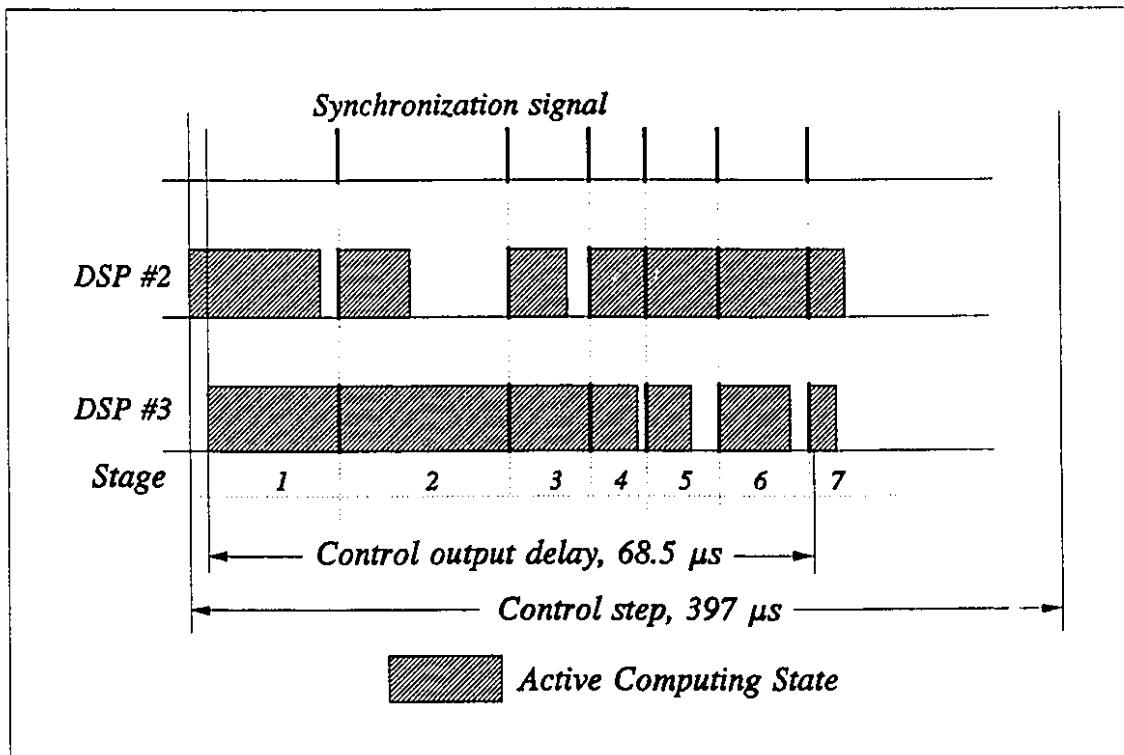


Figure 6-5 Active parallel computing times of the DSPs in each sampling period. (See Table 6-2 for details.)



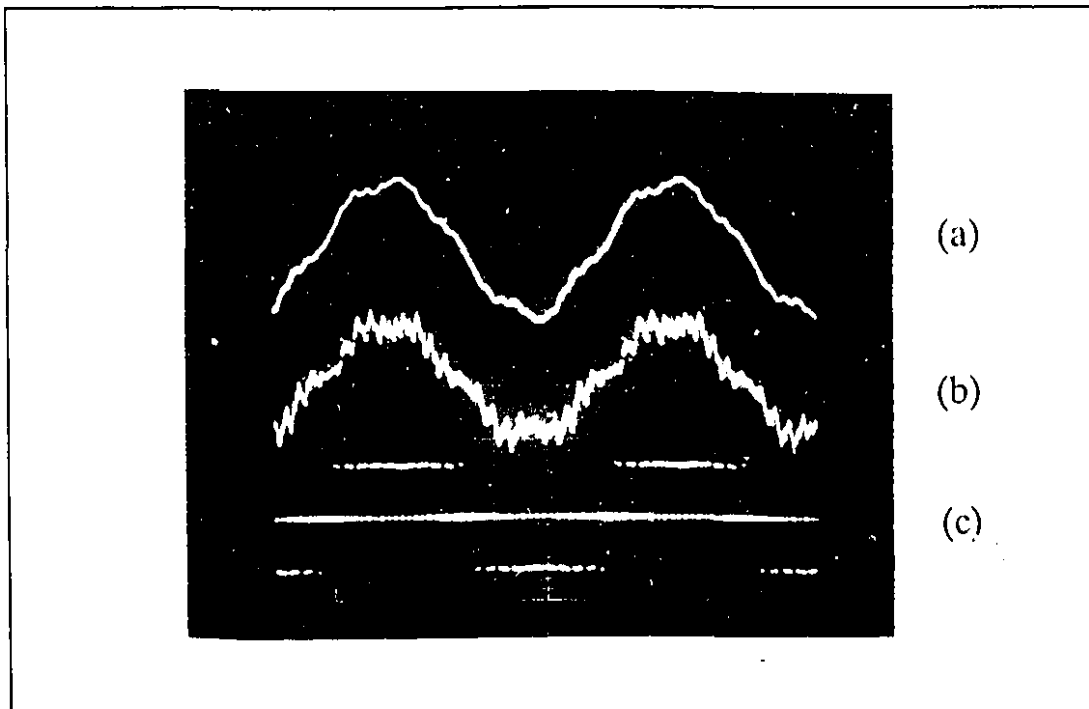
Table 6-2 Length of active computing time for the DSPs.

<i>Stages</i>	<i>1</i>	<i>2</i>	<i>3</i>	<i>4</i>	<i>5</i>	<i>6</i>	<i>7</i>
<i>DSP #2</i>	10.3 $\mu s$	7.0 $\mu s$	5.0 $\mu s$	6.6 $\mu s$	8.1 $\mu s$	10.0 $\mu s$	4.0 $\mu s$
<i>DSP #3</i>	14.6 $\mu s$	19.2 $\mu s$	9.0 $\mu s$	4.4 $\mu s$	3.5 $\mu s$	6.5 $\mu s$	3.0 $\mu s$

calculation stages. The active computing times executed in experiments are shown in Fig. 6-5 and Table 6-2. The first row of pulse waveform in Fig. 6-5 is the synchronization signal which controls the beginning of each parallel calculation stages. It is seen that the control computational delay time  $m\Delta T \leq 0.2 \times \Delta T$  is achieved.

### 6.6.1 Active Filtering Test

Fig.6-6 shows the steady-state operating waveforms of: (a) the ac line current, (b) the capacitor voltage and (c) the terminal PWM pulse current in the current-source PWM converter without the Pole Placement state feedback control. This corresponds to the case of the control variable  $\Delta \tilde{U}_a(t_k) = 0$  in Eq. (6.6). Typically the ac voltage source in the Power Electronics laboratory of McGill University contains the 3<sup>rd</sup> and the 5<sup>th</sup> harmonic. They cause the severe 5<sup>th</sup> harmonic distortions in the ac line current and the capacitor voltage waveforms



**Figure 6-6** Waveforms without Pole Placement state feedback control:  
 (a) ac line current,  $5 A_{rms}$ ; (b) capacitor voltage,  $67 V_{rms}$ ; (c)  
 converter terminal pulse current,  $i_{pj}(t)$ .  
 ( dc line current  $I_{dc}=10 A$ , and load  $R_{dc}+R_{load}=9 ohm$  )

because in this study the  $L$ - $C$  resonance frequency has been chosen to be close to the 5th harmonic.

For comparison, Fig. 6-7 shows the same waveforms of the current-source PWM converter with the Pole Placement state feedback control under the same test condition. The state feedback gains shown in "feedback" block of Fig. 6-3, have been chosen as  $K_1=-0.8289$ ,  $K_2=0.0459$ ,  $K_3=0.3876$  and  $K_4=0.0$ . These gains

assign the desired closed-loop system pole positions to be the same as the eigenvalues of Eq. (6.5) for a time constant of  $\tau = 0.332 \text{ ms}$  (which corresponds to a equivalent system in which the line resistance has been increased to  $R = 20 \text{ ohm}$ ). From Fig. 6-7, it is seen that the ac line current and the capacitor voltage are free of the lower order harmonics of Fig. 6-6, as they have been removed by the Pole Placement state feedback control.

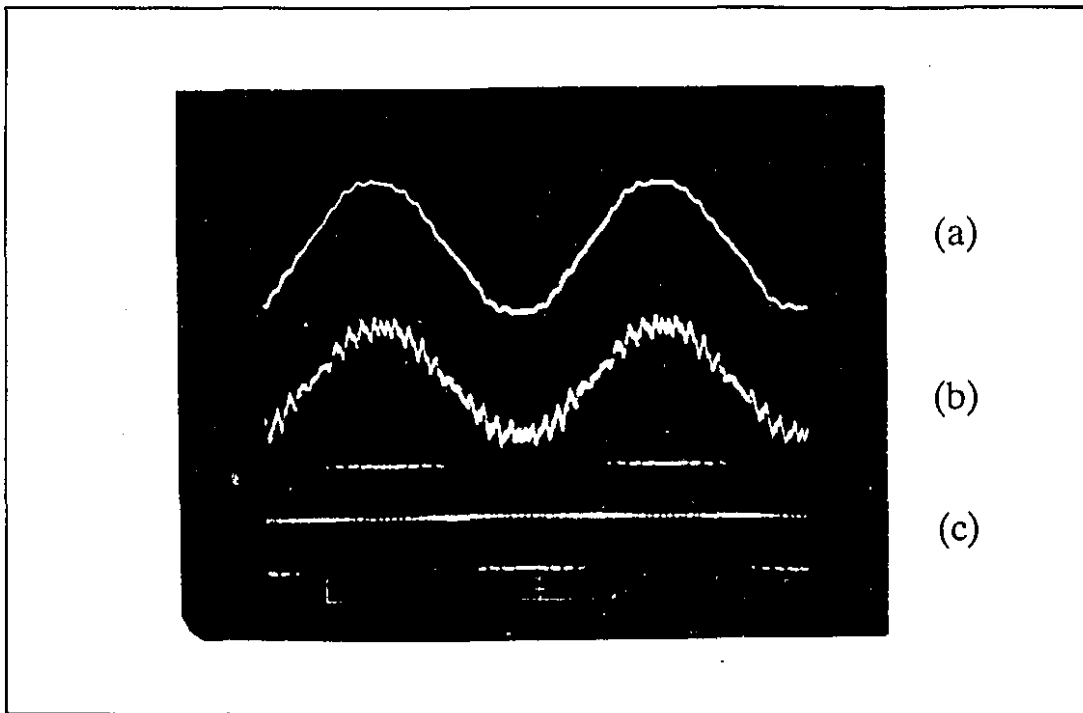


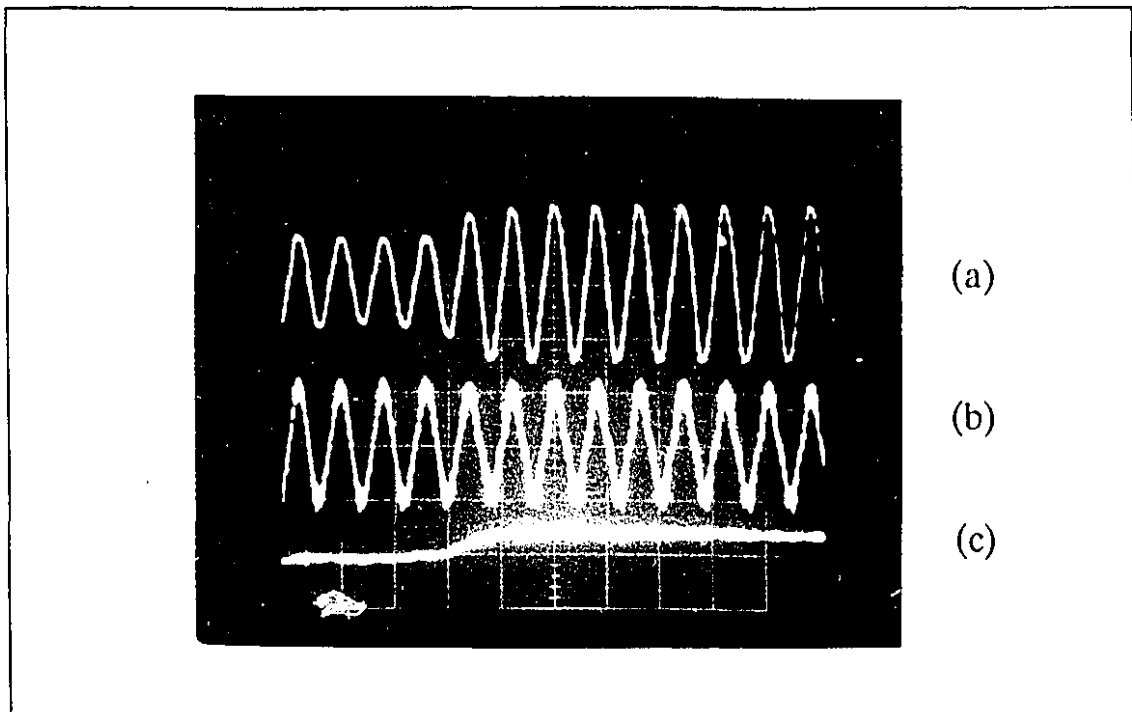
Figure 6-7 Waveforms with Pole Placement state feedback control:

(a) ac line current,  $5 A_{rms}$ ; (b) capacitor voltage,  $67 V_{rms}$ ; (c) converter terminal pulse current,  $i_{pj}(t)$ .

( dc line current  $I_{dc} = 10 A$ , and load  $R_{dc} + R_{load} = 9 \text{ ohm}$  )

### 6.6.2 Transient Test

Fig. 6-8 shows the oscillogram of: (a) the ac line current, (b) the capacitor voltage and (c) the dc link current, when the converter dc link current reference,  $I_{dref}$ , has a step change from 8 A to 11 A. The dc link current regulator proportional gain  $K_{P-dc}=0.19$  and integral gain  $K_{I-dc}=0.02$ . As can be seen, the



**Figure 6-8** Transient response of a step change in the dc link current reference when the Pole Placement state feedback control method is used:

(a) ac line current, from 3.4  $A_{rms}$  to 6.4  $A_{rms}$ ; (b) capacitor voltage; (c) dc link current, from 8 A to 11 A.

( dc resistance load  $R_{dc}+R_{load}=9\ ohm$  )

transient response is fast and the unity power factor ac line current is a good sine wave.

## 6.7 Summary

The incentive for the research of **Chapter 5** and the present chapter has been to bring to the perfection the 3-phase, 6-valve, current-source type PWM converter suitable for all power conditioning applications. The research has focused on a specific application. This is a high quality rectifier which is capable of: (i) generating almost sinusoidal current waveforms under unity power factor, (ii) actively filtering the ac line harmonics, and (iii) regulating the dc current.

The main difficulties have been identified in **Chapter 5**. The new control strategy: the Dynamic Tri-Logic Sinusoidal PWM method with the Decoupler Pre-Processor control scheme, has been proposed, analyzed and described in **Chapter 5**. This chapter has described the Pole Placement state feedback control which has been implemented by a high performance multi-DSP real-time controller. The predictions of its performance have been verified experimentally in a  $1\text{-kVA}$  laboratory converter.

The investigations of **Chapter 5** and the present chapter allow the following **conclusions** to be made:

- (1) The high quality, unity power factor, 6-valve, 3-phase, current-source type,

PWM rectifier can be controlled entirely by software algorithm implemented by multi-DSPs. The key to the success consists of achieving a sufficiently broad frequency bandwidth channel to convey the control feedback information. This requires: (i) the use of high-speed DSPs to execute the algorithm concurrently to minimize the computational delay time in the real-time control, (ii) the use of a sufficiently high triangular carrier frequency in the SPWM strategy.

- (2) The research has proposed and proven a new control design based on applying the Pole Placement state feedback technique to the inner ac line current control loop in each of the ac phases. The new design succeeds in: (i) improving the time response, (ii) actively filtering out the line harmonics.
- (3) Pivotal to the success is the Dynamic Tri-Logic SPWM method and the Decoupler Pre-Processor which can be used in all 6-valve, 3-phase, current-source converter bridges. The ability of the PWM strategy to operate as a linear amplifier with respect to the control inputs is an important asset. This is because the current-source type of PWM converters are increasingly called upon to fulfil the duties of filtering, stabilization and dynamic performance enhancement.

Essentially, all the difficulties of the current-source PWM converter have been identified and removed.

## CONCLUSIONS

This thesis has contributed to the advances of the Pulse Width Modulation techniques as applied to Power Electronics. At every step, the advances have been proven, initially by digital computer simulations, then by analysis, and finally by laboratory experiments. The conclusions are reported here under the following headings:

1. Advances in Pulse Width Modulation Theory,
2. Advances in Engineering Applications.
3. Advances in the Implementation of Pulse Width Modulation Techniques.

## 7.1 Advances in Pulse Width Modulation Theory

### 7.1.1 Two-Level or Bi-Logic PWM (Part I: Chapters 2, 3 and 4)

The Two-Level or Bi-Logic PWM has existed for several decades and because of its mature state of development, there is little room for contributions.

1. Nevertheless, Part I of the thesis has uncovered the last frontier – Phase Angle Control. This completes the three control attributes of the sinusoidal waveform in PWM: the original two attributes being, Amplitude Control and Frequency Control.
2. Phase Angle Control and Frequency Control are not completely independent. If the feedback signal to the Phase Angle Controller is considered to be Proportional feedback, then the same signal to the Frequency Controller is the Integral feedback.
3. Using the Phase Angle and the Frequency Controls, the PWM converter can be synchronized to another system (such as the electric power utility system which has a nominal frequency of *50 Hz* or *60 Hz*) through phase lock principles. Depending on the feedback error, the Phase Lock Loop (PLL) enables the PWM converter to fulfil regulatory functions. The two regulatory functions, demonstrated experimentally in the research of this thesis, are:
  - (i) dc voltage regulation,



- (ii) dc power regulation.
- 4. In the electric power utility system, the Phase Angle and Frequency Controls affect the real power transmission whereas the Amplitude Control affects the reactive power.

#### 7.1.2 Three-Level or Tri-Logic PWM (Part II: Chapters 5 and 6)

The contributions to the Three-Level or Tri-Logic PWM are extensive because it has only been recently recognized that the Current-Source, 6-Valve, 3-Phase PWM Bridge Converter must operate under Tri-Logic PWM.

- 5. A definitive method of generating Tri-Logic PWM from Bi-Logic PWM by the linear transformation of Eq. (5.2) in **Chapter 5** is proposed and proven by the truth table of Table 5-2.
- 6. Since the Tri-Logic PWM signals are generated by a linear transformation, then the preferred Bi-Logic PWM signals are those which have linear output-to-input relationship with respect to the modulating signals. An example of such a class of Bi-Logic PWM is the Sinusoidal PWM, in which the local averages of the Two-Level output pulse signals are the linearly amplified modulating signals. Thus the Tri-Logic PWM signals are also linear transformations of the modulating signals.
- 7. Using the Decoupler Pre-Processing Stage (Section 5.3.5), it is possible to compensate for the non-diagonal linear transformation equation of Eq.

(5.2), so that the local average of the Tri-Logic PWM signal of any of the three phases is linearly proportional to the modulating signal for that phase. The outputs and inputs of the three phases are decoupled. Essentially, the Tri-Logic PWM converter becomes three independent linear amplifiers (constant gain, without phase shift), one amplifier for each of the three phases.

8. All the linear properties of the Bi-Logic Sinusoidal PWM are conferred to the Tri-Logic PWM. For example, the ability to control (i) the Amplitude, (ii) the Frequency and (iii) the Phase Angle of the fundamental Fourier Component in the Bi-Logic PWM is also built into the Tri-Logic PWM. The linear amplifier property includes a broad frequency bandwidth channel (about  $1/3$  of the triangular carrier frequency) to convey non-sinusoidal signal transmission. The broad frequency bandwidth is necessary for the implementation of feedback and active filtering functions.
9. The linear transformation of Eq. 5.2 includes the switching harmonics. As the carrier and sideband harmonics of the Bi-Logic SPWM are known, the carriers and sideband harmonics of the Tri-Logic PWM are predictable, as shown in Fig. 5-5.

## 7.2 Advances in Engineering Applications

The applications chosen for the Bi-Logic PWM and the Tri-Logic PWM

are respectively the High Voltage Direct Current Transmission System and the Current-Source PWM Rectifier.

#### 7.2.1 HVDC Transmission System (Part I: Chapters 2, 3 and 4)

1. The conceptual study in **Chapter 2** shows that the Voltage-Source PWM converter has performance characteristics which are superior to those of the existing line-commutated converters presently used in HVDC Transmission System. The ability to connect the dc sides of the converter stations directly in parallel, in the face of power reversals, is particularly attractive in multi-terminal application. The existing line-commutated HVDC system requires mechanical reversing switches for power reversals in multi-terminal connections.
2. The concepts are proven to be correct in **Chapter 3** in tests using *1-KVA* size converter modules. Of special interest, is the successful reversal of power in the multi-terminal connection while using local control in the individual converter station. The existing HVDC multi-terminal connections require centralized controls with remote communication links to the geographically separated stations.
3. The parametric studies of component sizes of the voltage-source PWM stations in **Chapter 4** demonstrate that they are within the "ball-park" figures of the line-commutated HVDC stations.

#### **7.2.1.1 General Conclusion**

The laboratory and the feasibility studies have shown that the concept of the Voltage-Source PWM-HVDC Transmission System is sound and merits follow-up, in-depth studies.

#### **7.2.2 Current-Source PWM Rectifier (Part II: Chapters 5 and 6)**

4. A stand-alone, 3-phase, 6-valve, current-source, PWM Rectifier has been built. Tests show that the demanding performance characteristics are all met:
  - (i) Regulated dc link current,
  - (ii) Unity power factor operation,
  - (iii) Near sinusoidal ac current,
  - (iv) Active Filtering to remove ac source harmonics,
  - (v) fast response.

### **7.3 Advances In The Implementation of Pulse Width Modulation Techniques**

The advances in the theory and the applications of Pulse Width Modulation techniques have been possible because of the advances in the methods of implementation: in hardware and in software, in analogue and in digital forms.

### 7.3.1 Phase Lock Loop Control (Part I: Chapters 2, 3 and 4)

Figs. A-2 and A-3 in **Appendix A** constitute a proven design of the Phase Lock Loop Control of the Voltage-Source Type Force-Commutated Converter Station. In the experimental results in **Chapter 3**, the same Phase Lock Loop Control has been used to make the Converter station into a DC Voltage Regulator and then as a Power Dispatcher simply by changing the feedback signals from Fig. 2-9 to Fig. 2-10.

To emphasize its versatility, in Ref. [86] the same controller is used to make the converter into a Static VAR Controller.

#### 7.3.1.1 Real Power Controlled by Phase Lock Loop

Through the Phase Lock Loop Control, the PWM converter is synchronized to the nominal standard frequency of the electric utility system. The real power is controlled by the phase angle (which has the status of the proportional channel in feedback) and the frequency (which has the status of the integral channel in feedback). The reactive power is controlled through the amplitude of the PWM modulating signal.

### 7.3.2 Multi-DSP Controlled Current-Source PWM Rectifier (Part II: Chapters 5 and 6)

In Part I, the hardware implementation is hybrid: a mixture of analogue and digital methods. In the control of the current-source PWM converter in Part

II, the objective is to realize an entirely digital controller based on a multi-DSP platform and PAL (Programmable Array Logic) circuit. The multi-DSP platform has been designed and constructed by a fellow Ph.D. candidate, Ms. Y. Guo [94-96]. The feedforward, the feedback and regulatory controls of **Chapter 6** are realized by software programs (**Appendix C**) executed in real-time.

#### **7.3.2.1 Frequency Bandwidth and Computational Delays**

A very important conclusion of this research is the necessity to reduce computational delays by parallel processing so as to secure sufficient frequency bandwidth in the PWM controller to implement the Pole-Placement strategies. Laboratory experience shows that without the frequency bandwidth, the stability and the active filtering cannot be achieved.

#### **7.3.2.2 Implementation of Dynamic Tri-Logic PWM**

A very important contribution to reducing the computational delays is the use of Programmable Array Logic (PAL). The design of the PAL Gating Logic Circuit is shown in Fig. B-3 in **Appendix B**. The program lists of PAL chip designs are in Tables B-1 to B-6 of **Appendix B**. The PAL circuits implement the Tri-Logic SPWM described in **Chapter 5**.

#### **7.3.2.3 Innovative Feedback Method**

Another contribution to reducing the computational delay is the Innovative

Feedback Method in which the ac side equations remain in the  $a-b-c$  frame, thus avoiding the steps of transformations to the  $o-d-q$  frame and back.

The Innovative Feedback Method achieves Active Filtering from the Pole-Placement strategy which is originally intended for fast time response characteristics.

#### **7.4 Suggestions For Future Work**

The Bi-Logic PWM has an extensive literature and future advance in the theory is the range of diminishing returns. The Tri-Logic PWM is still in its infancy and there is scope for important contributions, especially in the Dynamic Type.

This thesis has opened up the application of PWM techniques in the utility environment. Because of switching losses, future research should concentrate on the lowest possible switching frequencies of the PWM technique. Beside HVDC, the future work will be on Static VAR Compensators (Shunt and Series Types), Phase Shifters, Power Conditioners for Storage Systems.

## IMPLEMENTATION OF VOLTAGE-SOURCE PWM CONVERTER

### A.1 Introduction

The experimental work, in the research of the PWM-HVDC transmission system of **Chapters 2-4**, has been successfully carried out by using two  $1\text{-kVA}$  size bipolar transistor converter bridges to present two PWM-HVDC stations. The converter bridges have been built in our power electronics laboratory. A detail description of each converter can be found in Appendix-B of Ref.[89].

For demonstrating and verifying the concepts of the PWM-HVDC transmission system, a new design of the phase lock loop controller, described in **Chapter 2**, has been implemented. By configuring the feedback controls the converter is made to operate either as a DC Voltage Regulator (*VR*) or as a Power Dispatcher (*DISP*). A brief description of the hardware design and



practical implementation of this controller is given here. Figs. A-1, A-2 and A-3 show the circuit diagrams of the controller in detail.

## A.2 Sinusoidal Modulating Signal

In the design, the 3-phase Sinusoidal PWM modulating signals,  $V_m-A$ ,  $V_m-B$  and  $V_m-C$  as shown in Fig. A-1, are generated using the so-call "EPROM" method. Each of the 3-phase sinusoidal waveform templates in one complete period is sampled equally by  $2^9=512$  points. The samples are then digitized (8-bit resolution) and stored in three EPROMs (2764s), one for each phase. When the EPROMs are addressed by a 9-bit number (A0-A8), the outputs from the EPROMs are converted into 3-phase analog sinusoidal waveforms,  $V_m-A$ ,  $V_m-B$  and  $V_m-C$ , through the *D-to-A* converting circuits (consisting of the MC1408s and LM747s, shown in Fig. A-1). In the experiments, the amplitudes of the analog modulating signals are kept as constants which correspond to the modulating index  $M=0.8$ . The frequency of the modulating signals is determined by the rate at which the 9-bit address counter is increased by the VCO (*voltage controlled oscillator*).

## A.3 The PLL Control

The PLL (*phase lock loop*) control, with the switch  $S$  turned to the position of 1 shown in Fig. A-2, is used to synchronize the output modulating signals,  $V_m-A$ ,  $V_m-B$  and  $V_m-C$ , to the utility ac line voltages prior to the closing the circuit breaker. The utility has the nominal frequency of the 60 or 50 Hz standards and

the autonomous frequency of the converter bridge has to be synchronized to the utility frequency. The chip CD4046 in Fig. A-2 plays a key role in the PLL control, which consists of a phase comparator and a VCO (*voltage controlled oscillator*). The output pulse signal from the VCO (*VCOUT* pin) is used as the clock of a 12-bit binary counter (74LS161s) shown in Fig. A-3. The most significant 9 bits of the counter (*Y3-Y11*) are chosen to address the EPROMs. In order to obtain the 60 Hz sine-wave output, the central frequency of the VCO is set at  $f_0 = 60 \times 2^{12} = 245760$  Hz by choosing the values of *R1*, *R2* and *CX* under the condition that the VCO input voltage  $V_{COIN} = 0.5V_{dd} = 2.5$  V. The 2.5 V can be obtained by adjusting the potentiometer *Rf*. The phase angle of the ac source voltage is measured using a *Zero-Crossing Detector* circuit (consisting of a second-order filter and two comparators, LM318 and LM319). The output phase signal, *SP*, with the duty ratio of 1:1, is sent into the phase comparator on the chip CD4046 through the pin *SIN*, and compared with the MSB bit of the counter, *Y11*. The phase error, *PE*, between signals of *SP* and *Y11* is obtained by filtering the harmonics and removing the dc offset components contained in the output of phase comparator, *P1*, through a *R-C* low-Pass (*LP*) filter and an adder circuit. The error signal *PE* is used as a negative feedback signal,  $\Delta\omega$ , to adjust the VCO output frequency so as to vary the cycling rate of the counter to null the error of *PE*.

A phase angle control channel is inserted into the PLL control as shown in Fig. A-3. The analog phase angle control signal,  $\Delta\delta$ , is firstly digitalized into a 8-

bit binary number ( $X0-X7$ ) through an *A-to-D* converter (ADC0804), then added onto the number contained in the address by a 9-bit binary adder circuit (74LS83s and 74LS373), so that the EPROM address ( $A0-A8$ ) is equal to  $(Y3-Y11)+(X0-X7,X7)$ . Thus an instantaneous change in the phase angle of modulating signal can be implemented. The phase angle control channel is effectively a proportional feedback channel because the modulating signal phase shift is proportional to the control signal  $\Delta\delta$ . Normally, during the procedure of closing circuit breaker, the  $\Delta\delta$  is adjusted as zero as the converter is not loaded.

#### A.4 The VR/DISP Control

By turning the switch  $S$  to the position of 2 after the converter circuit breaker has been closed, the converter operates as either a voltage regulator (*VR*) or a power dispatcher (*DISP*). In the case of *VR*, the dc link voltage is measured using a Hall Effect (LEM) sensor circuit (with the frequency bandwidth 0-100 kHz) shown in Fig. A-2. The error signal,  $ER$ , between  $V_{dc}$  and its reference setting is obtained from the *feedback comparator*, then amplified and fed to the VCO and the phase angle control circuits respectively to adjust the control signals  $\Delta\omega$  and the  $\Delta\delta$ . For the case of *DISP*, the only change needed is the feedback signal, which is now the signal  $I_{dc}$ , whose Hall Effect (LEM) feedback sensor circuit is shown in Fig. A-2 also.

All of the control circuits shown in Figs. A-1, A-2 and A-3 have been built on breadboards.

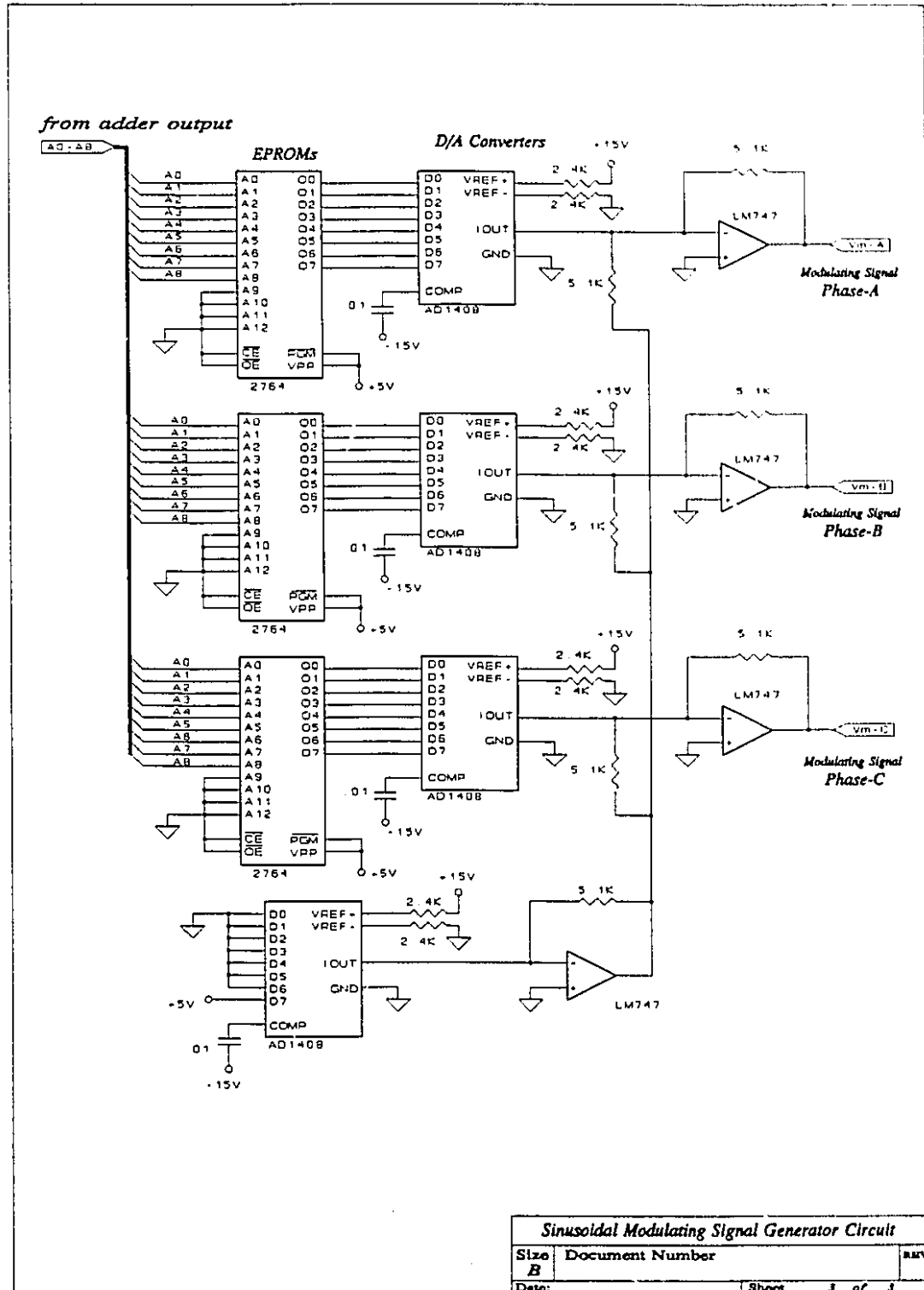


Figure A-1 Sinusoidal Modulating Signal Generator Circuit.

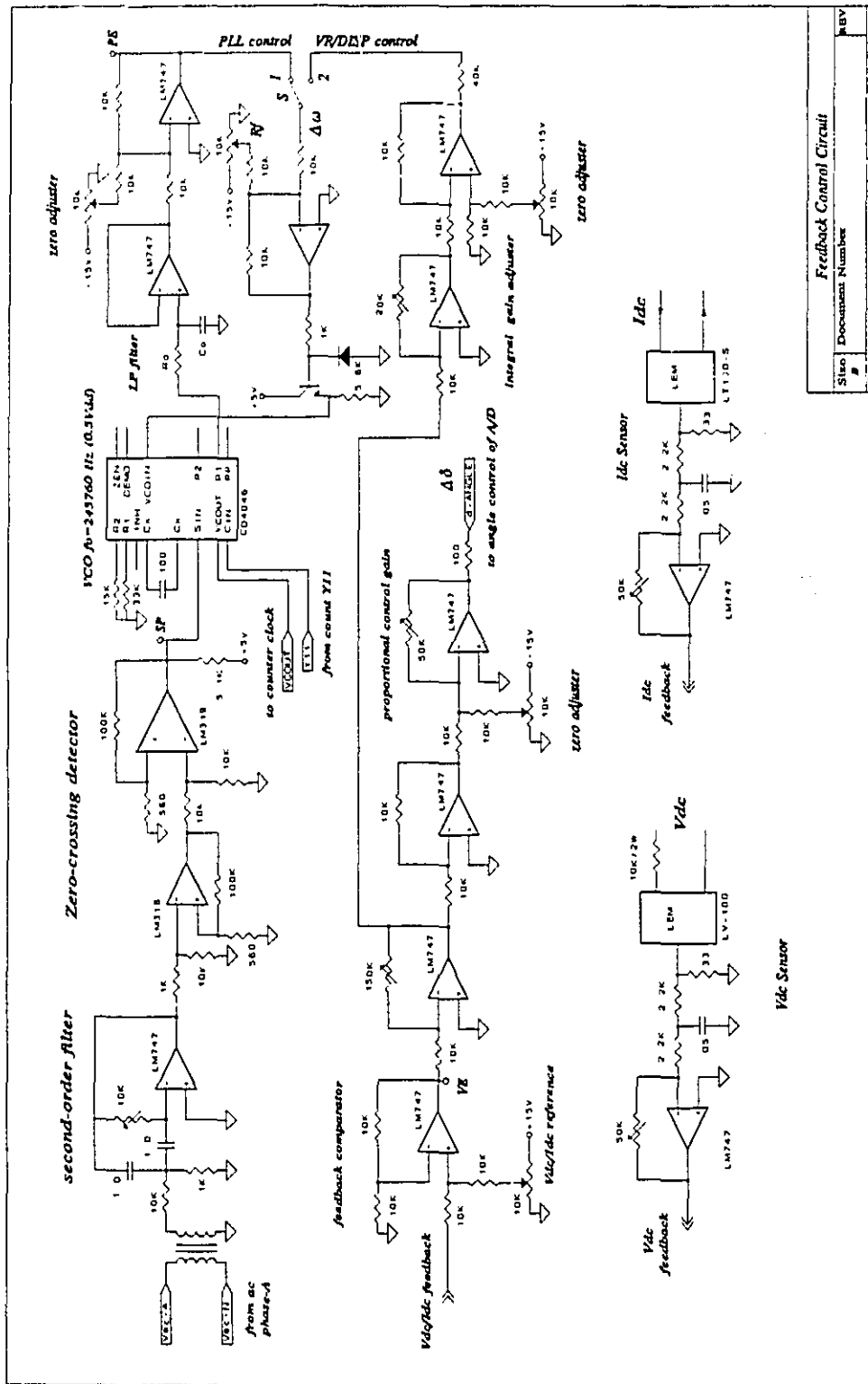


Figure A-2 Phase-Loop Controller.

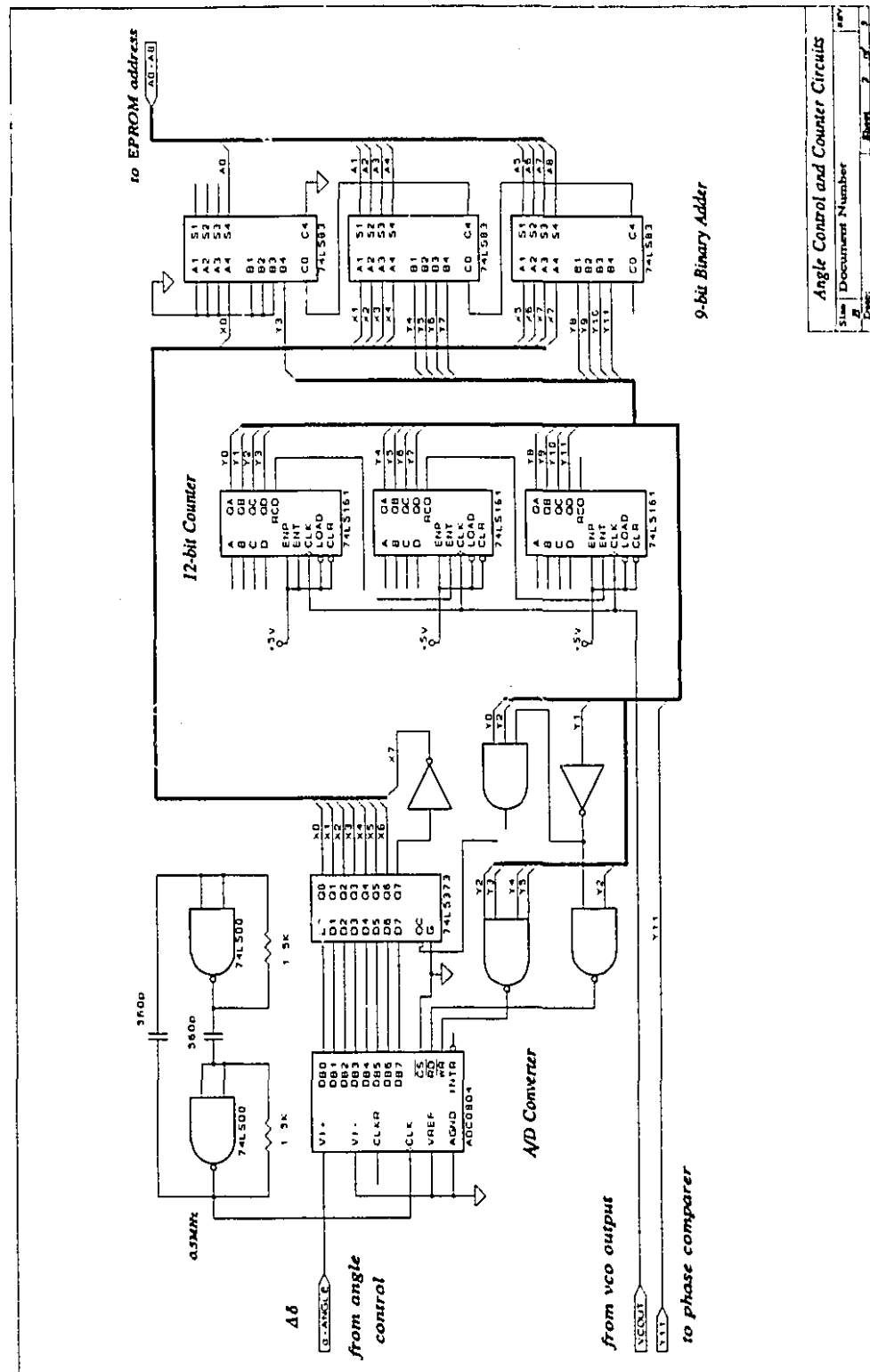


Figure A-3 EPROM Address Generator Circuit.

## IMPLEMENTATION OF DYNAMIC TRI-LOGIC PWM CONTROL

### **B.1 Introduction**

Fig. B-1 shows a photograph of the experimental set-up of a multi-DSP controlled,  $1\text{-KVA}$  size of 3-phase, 6-valve, current-source PWM converter system, which has been implemented for demonstrating and verifying the concepts described in **Chapters 5 and 6**. The main converter, shown by the arrow *A*, has been inherited from previous researches [69-72] in our laboratory. Here, it has been reconnected into a 3-phase, 6-valve, current-source PWM converter bridge. A multi-DSP controller [94-96] and a PC XT computer have been employed to perform all the feedback control tasks described in **Chapter 6**. The controller consists of three high speed Texas Instrument TMS320C25 DSPs and execute the feedback calculations in parallel. The control programs are compiled and then

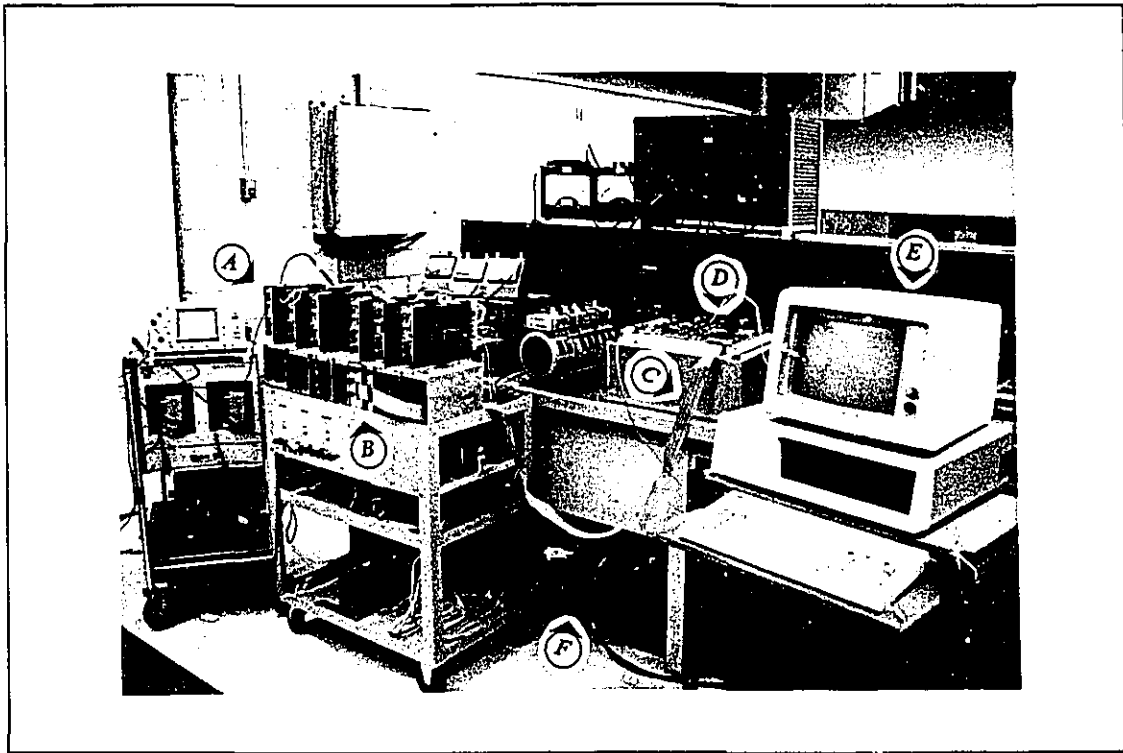


Figure B-1 Experimental set-up of the multi-DSP controlled 3-phase, current-source PWM converter system.

A) 1-KVA size of bipolar transistor PWM converter bridge, B) PAL Gating Logic and A/D converter circuit boards, C) Data transmission cable, D) Multi-DSP controller board, E) PC-XT computer, F) inductor and capacitor boxes.

the machine codes are download to each DSP by using the PC XT computer. A new PAL Gating Logic circuit and a four channel A/D Converter circuit have been built and installed onto the converter, shown by the arrow B, to perform the functions of the Bi/Tri-Logic SPWM Translation (Section 5.3.2 of Chpater 5) and the feedback signal sampling. The data are transmitted between the multi-DSP



controller and the PAL circuits through a parallel cable shown by the arrow C.

## B.2 Converter Bridge Circuit

Fig. B-2 shows the main converter bridge circuit of the 3-phase, 6-valve Current-source PWM converter. A detail description for each of the six switch units can be found in Ref.[72] (the component parameters in the Base Drive circuit have been modified here to improve the switching speed). A dc snubber circuit, consisting of  $R_s$ ,  $C_s$  and  $D_s$ , is connected across the dc terminals for protection against  $L_{dc}dI_{dc}/dt$  voltage. As mentioned in Chapter 5, because of the ac capacitors, a reverse biased capacitor voltage can appear directly across on a valve which is receiving a turning ON signal. This valve will be remain turned OFF until the reverse biased voltage is removed by the proper turning OFF of other valve. During this transient period both valves are OFF and the dc snubber circuit provides the dc link current with an alternate path so as to eliminate the large inductive voltage across the dc line inductance which can damage the switch device.

## B.3 PAL Gating Logic Circuit

Fig. B-3 shows the circuit of PAL Gating Logic circuit. It receives the 3-phase Bi-Logic SPWM signals,  $S_{-abc}$  (or  $X_a$ ,  $X_b$  and  $X_c$  in Fig. 5-1), from the multi-DSP controller and translates them into the Tri-Logic SPWM signals

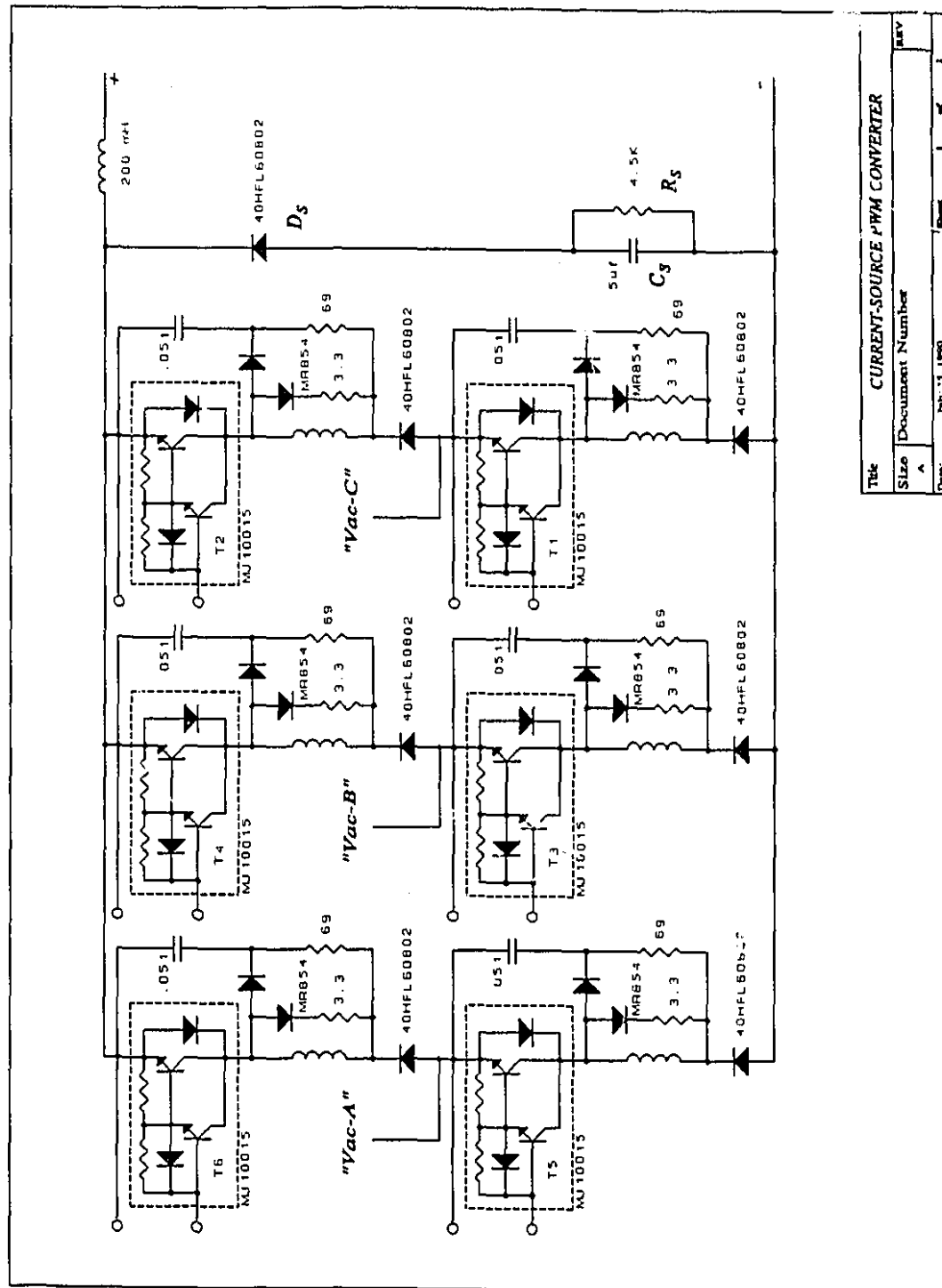


Figure B-2 The main switching circuit of 3-phase current-source PWM converter.

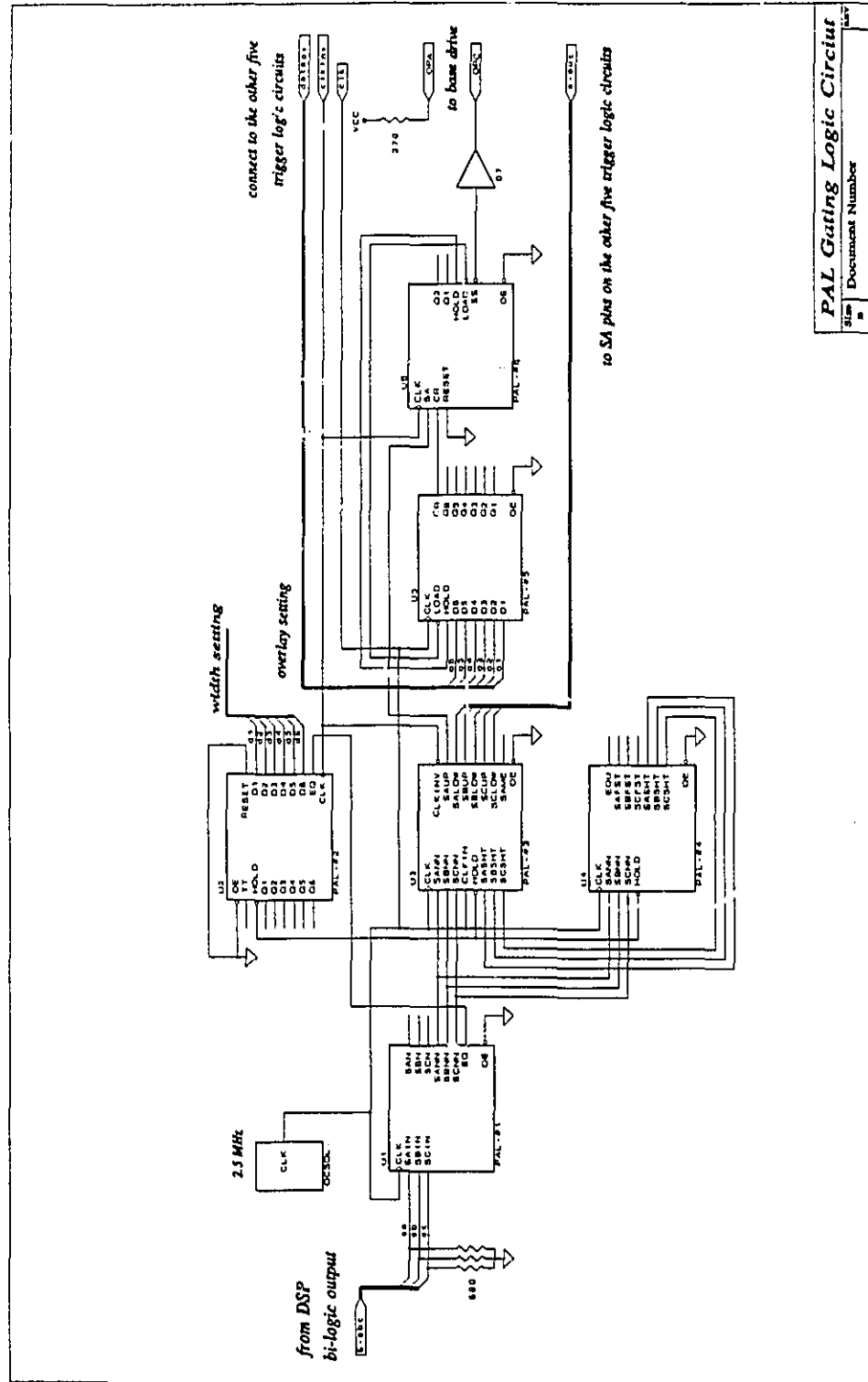


Figure B-3 PAL Gating Logic Circuit.

through the PAL chips *U1-U4*. The output Tri-Logic SPWM triggering signals are finally sent to each valve through the PAL chips *U5-U6*.

### B.3.1 Bi/Tri-Logic Translation Circuit Programming

Table B-1 is the program list of the design for chip *U1*. Its function is to sample the Bi-Logic SPWM input signals *S-abc* at each rising edge of the circuit clock, and then output the signal *EQ* to indicate that a change has occurred in the signals *S-abc*.

Table B-2 shows the program list of the design for chip *U2*. Its function is to eliminate very narrow triggering pulses in the signals *S-abc* so as to protect the valve from unnecessary fast switching and from the effects of the noise in the signals *S-abc*. The data of *D1-D6* specify the width setting for the narrow pulse elimination.

The chip *U3* plays the function of The Bi/Tri-logic SPWM Translation and the *U4* determines the shoot-through signals based on the methods described in Section 5.3.3 of **Chapter 5**. The details of the designs for chips *U3* and *U4* are listed in Table B-3 and B-4, respectively.

### B.3.2 Triggering Logic Circuit Programming

In Fig. B-3, chips *U5* and *U6* produce the trigger signal for one of the six valves of the converter bridge. The triggering logic circuits for the other five valves are exactly identical. The chip *U6* adds a short delay time to the turning

OFF edge of the triggering signal. Thus there is a short overlap time during which both valves are ON as one valve is receiving the turning ON signal and other is being turned OFF. The object is to shorten the switching transient. The chip *U5* controls the width of this short overlap by choosing the data of *O1-O6*.

The output trigger signal at the terminals *OPA* and *OPC* is used directly to drive the optocoupler in the Base Drive circuit of valve (which is not shown in Fig. B-2).

All of the PAL circuit designs in Fig. B-3 are implemented by using the specialized chip GAL16V8-25ns [97], which can be programmed to assume different function by using 'OrCAD/PLD' [98] as the CAD tools. The design has

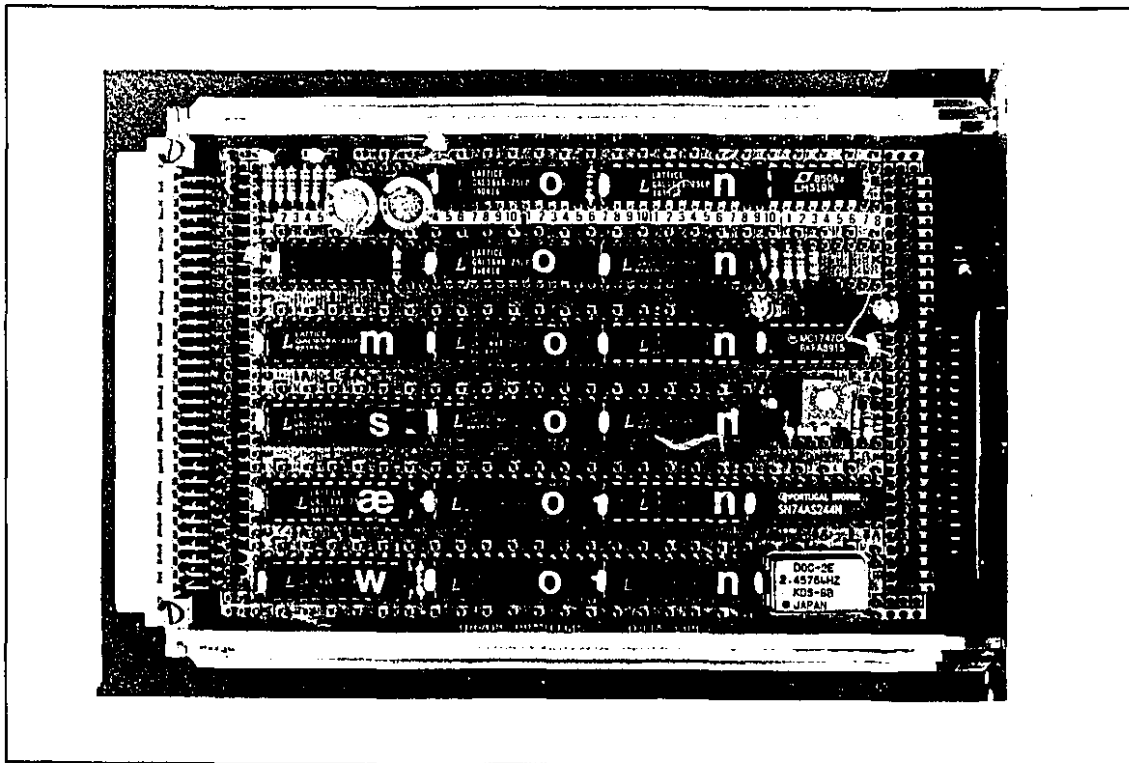


Figure B-4 The PAL Gating Logic circuit Implementation Using The Speedwire board.

been tested on a *speedwire circuit board* as shown in Fig. B-4. Table B-1 to B-6 show the logic designs

**Table B-1 The Program List of PAL Chip #1 Design.**

```

.....
* CHIP NAME      : PAL-#1
* FUNCTION       : latch the bi-logic SPWM input signals
.....

|PAL16RP8  indale, sbin, scin),
|          out: (san, sbn, scn, sann, sbnn, scnn, eq),
|          clock: clk
|
| active-high: "all"
|
| san = sain
| sbn scn = scin
| sann = san
| sbnn = sbn
| scnn = scn
| eq = (san' & sbn' & scn' & sann' & sbnn' & scnn')
|      # (san' & sbn' & scn & sann' & sbnn' & scnn)
|      # (san' & sbn & scn' & sann' & sbnn' & scnn)
|      # (san' & sbn & scn & sann' & sbnn & scnn)
|      # (san & sbn' & scn' & sann & sbnn' & scnn)
|      # (san & sbn' & scn & sann' & sbnn' & scnn)
|      # (san & sbn & scn' & sann & sbnn & scnn)
|      # (san & sbn & scn & sann & sbnn & scnn)
|

```

**Table B-2 The Program List of PAL Chip #2 Design.**

```

.....
* CHIP NAME      : PAL-#2
* FUNCTION       : counting the width of input pules
.....

|PAL16RP8  in: (eq, d[6~1], reset),
|          out: (q[6~1], ttr[2~1]),
|          clock: clk
|
| active-high: "all"
|
| procedure: reset, ttr[2~1]
| { states: state1 = 00b,
|          state2 = 01b,
|          state3 = 10b
|
| state1. eq? -> state2
|         -> state1
| state2. eq? -> state1
|         eq & q[6~1] = -0? -> state3
|         -> state2
| state3. eq? -> state1
|         -> state3 }
|

```

```

| q1 = ((q1' & tr[2-1] = 1 & eq)
|   # (d1 & tr[2-1] = 0 & tr[2-1] = 2 & eq))) & reset'
| q2 = (((q1 & q2) & (q1' & q2')) & tr[2-1] = 1 & eq)
|   # (d2 & tr[2-1] = 0 & tr[2-1] = 2 & eq))) & reset'
| q3 = (((q[3-1] = 0 & q[3-1] = 7 & q[3-1] = 6 & q[3-1] = 5) & tr[2-1] = 1 & eq)
|   # (d3 & tr[2-1] = 0 & tr[2-1] = 2 & eq))) & reset'
| q4 = (((q[4-1] = 0 & (q[4-1] = 8 & q4)) & tr[2-1] = 1 & eq)
|   # (d4 & tr[2-1] = 0 & tr[2-1] = 2 & eq))) & reset'
| q5 = (((q[5-1] = 0 & (q[5-1] = 16 & q5)) & tr[2-1] = 1 & eq)
|   # (d5 & tr[2-1] = 0 & tr[2-1] = 2 & eq))) & reset'
| q6 = ((q[6-1] = 32 & q6 & tr[2-1] = 1 & eq)
|   # (d6 & tr[2-1] = 0 & tr[2-1] = 2 & eq))) & reset'

```

Table B-3 The Program List of PAL Chip #3 Design.

```

*****
* CHIP NAME      : PAL-#3 (version 3)
* FUNCTION       : bi-logic to tri-logic transformation
*****

{PAL16RP6 In: (sa, sb, sc, clkIn, hold, sasht, sbsht, scsht),
  lo: (clkInv, same),
  out: q[6-1],
  clock: clk

| active-low: hold
| registers: q[6-1]

| same = (sa & sb & sc) & (sa' & sb' & sc')
|
| q6 = (sa & sb' & hold)
|   # (same & sasht' & sbsht' & scsht' & hold)
|   # (same & sasht' & sbsht' & scsht' & q6 & hold)
|   # (same & sasht' & sbsht' & q6 & hold)
|   # (same & sasht' & scsht' & q6 & hold)
|   # (same & sbsht' & scsht' & q6 & hold)
|   # (same & q6 & q5' & q4' & q3' & q2' & q1' & hold)
|   # (q6 & hold)
| q5 = (sa' & sb & hold)
|   # (same & sasht' & sbsht' & scsht' & hold)
|   # (same & sasht' & sbsht' & scsht' & q6 & hold)
|   # (same & sasht' & sbsht' & q6 & hold)
|   # (same & sasht' & scsht' & q6 & hold)
|   # (same & sbsht' & scsht' & q6 & hold)
|   # (same & q6 & q5' & q4' & q3' & q2' & q1' & hold)
|   # (q5 & hold)
| q4 = (sb & sc' & hold)
|   # (same & sasht' & sbsht' & scsht' & hold)
|   # (same & sasht' & sbsht' & scsht' & q4 & hold)
|   # (same & sasht' & sbsht' & q4 & hold)
|   # (same & sasht' & scsht' & q4 & hold)
|   # (same & sbsht' & scsht' & q4 & hold)
|   # (same & q6' & q5' & q4' & q3' & q2' & q1' & hold)
|   # (q4 & hold)
| q3 = (sb' & sc & hold)
|   # (same & sasht' & sbsht' & scsht' & hold)
|   # (same & sasht' & sbsht' & scsht' & q4 & hold)
|   # (same & sasht' & sbsht' & q4 & hold)
|   # (same & sasht' & scsht' & q4 & hold)
|   # (same & sbsht' & scsht' & q4 & hold)
|   # (same & q6' & q5' & q4' & q3' & q2' & q1' & hold)
|   # (q3 & hold)
| q2 = (sc & sa' & hold)
|   # (same & sasht' & sbsht' & scsht' & hold)
|   # (same & sasht' & sbsht' & scsht' & q2 & hold)
|   # (same & sasht' & sbsht' & q2 & hold)
|   # (same & sasht' & scsht' & q2 & hold)
|   # (same & sbsht' & scsht' & q2 & hold)

```

```

| # (same & q6' & q5' & q4' & q3' & q2 & q1 & hold')
| # (q2 & hold')
| q1 = (sc' & sa & hold')
| # (same & sash1' & sbsh1' & scsh1 & hold')
| # (same & sash1' & sbsh1' & scsh1' & q2 & hold')
| # (same & sash1 & sbsh1 & q2 & hold')
| # (same & sash1 & scsh1 & q2 & hold')
| # (same & sbsh1 & scsh1 & q2 & hold')
| # (same & q6' & q5' & q4' & q3' & q2 & q1 & hold')
| # (q1 & hold')
|
| clkinv = 1 ?? clkIn'

```

Table B-4 The Program List of PAL Chip #4 Design.

```

.....
* CHIP NAME      : PAL-#4
* FUNCTION       : store previous bi-logic input signals, produce shoot-through signal
* .....
| PAL16RP8 In: (sann, sbnn, scnn, hold),
|             out: (equ, safst, sbfst, scfst, sash1, sbsh1, scsh1),
|             clock: clk
|
| active-low: hold
|
| equ = (sann' & sbnn' & scnn' & hold')
|      # (sann & sbnn & scnn & hold')
|      # (equ & hold)
|
| safst = (sann & equ & hold')
|         # (safst & equ' & hold')
|         # (safst & hold)
|
| sbfst = (sbnn & equ & hold')
|         # (sbfst & equ' & hold')
|         # (sbfst & hold)
|
| scfst = (scnn & equ & hold')
|         # (scfst & equ' & hold')
|         # (scfst & hold)
|
| sash1 = (sann & sbnn' & scnn & safst & sbfst' & scfst & equ' & hold')
|         # (sann & sbnn' & scnn & safst & sbfst' & scfst' & equ' & hold')
|         # (sann & sbnn' & scnn' & safst & sbfst' & scfst & equ' & hold')
|         # (sann' & sbnn & scnn' & safst' & sbfst & scfst' & equ' & hold')
|         # (sann' & sbnn & scnn & safst' & sbfst' & scfst & equ' & hold')
|         # (sann' & sbnn' & scnn' & safst' & sbfst & scfst & equ' & hold')
|         # (sash1 & ((sann & sbnn & scnn) # (sann' & sbnn' & scnn') # equ # hold))
|
| sbsh1 = (sann & sbnn & scnn' & safst & sbfst & scfst' & equ' & hold')
|         # (sann & sbnn & scnn' & safst' & sbfst & scfst' & equ' & hold')
|         # (sann' & sbnn & scnn' & safst & sbfst & scfst' & equ' & hold')
|         # (sann' & sbnn' & scnn & safst' & sbfst' & scfst & equ' & hold')
|         # (sann' & sbnn' & scnn & safst & sbfst' & scfst & equ' & hold')
|         # (sbsh1 & ((sann & sbnn & scnn) # (sann' & sbnn' & scnn') # equ # hold))
|
| scsh1 = (sann & sbnn' & scnn' & safst & sbfst' & scfst' & equ' & hold')
|         # (sann & sbnn & scnn' & safst & sbfst' & scfst' & equ' & hold')
|         # (sann & sbnn' & scnn' & safst & sbfst & scfst' & equ' & hold')
|         # (sann' & sbnn & scnn & safst' & sbfst & scfst & equ' & hold')
|         # (sann' & sbnn & scnn & safst' & sbfst' & scfst & equ' & hold')
|         # (sann' & sbnn' & scnn & safst' & sbfst & scfst & equ' & hold')
|         # (scsh1 & ((sann & sbnn & scnn) # (sann' & sbnn' & scnn') # equ # hold))

```



Table B-5 The Program List of PAL Chip #5 Design.

```

*****
* CHIP NAME   : PAL-#5
* FUNCTION    : 8 bits down counter used with PAL-#8 to count the overlap width
*****

|PAL16RP8 In: (load, hold, d[6-1]),
|          lo: cr,
|          out: q[6-1],
|          clock: clk
|
| active-low: load
|
| q1 = (q1' & load' & hold')
|      # (q1 & load' & hold)
|      # (d1 & load)
| q2 = (((q1 & q2) # (q1' & q2')) & load' & hold')
|      # (q2 & load' & hold)
|      # (d2 & load)
| q3 = (([q[3-1] = 0 # q[3-1] = 7 # q[3-1] = 6 # q[3-1] = 5] & load' & hold')
|      # (q3 & load' & hold)
|      # (d3 & load)
| q4 = (([q[4-1] = 0 # q[4-1] = 8 & q4]) & load' & hold')
|      # (q4 & load' & hold)
|      # (d4 & load)
| q5 = (([q[5-1] = 0 # q[5-1] = 16 & q5]) & load' & hold')
|      # (q5 & load' & hold)
|      # (d5 & load)
| q6 = ([q[6-1] = 32 & q6 & load' & hold']
|      # (q6 & load' & hold)
|      # (d6 & load)
|
| cr = 1 ?? q[6-1] = 0

```

Table B-6 The Program List of PAL Chip #6 Design.

```

*****
* CHIP NAME   : PAL-#6
* FUNCTION    : add a overlap to falling edge
*****

|PAL16RP8 In: (sa, cr, reset),
|          out: (q[2-1], hold, ldi, sa),
|          clock: clk
|
| active-low: ss
| register: q[2-1], hold, ldi, sa
|
| procedure: reset, q[2-1]
| {
|   state: state1 = 0,
|          state2 = 3,
|          state3 = 2
|
|   state1. sa = 0
|           hold = 1
|           ldi = 0
|           sa? -> state2
|           -> state1
|   state2. sa = 1
|           hold = 1
|           ldi = 0
|           sa? -> state3
|           -> state2
|   state3. sa = 1
|           hold = 0
|           ldi = 1
|           cr? -> state1
|           -> state3 }

```

## B.4 A/D Converter Circuit

A four-channel A/D converter circuit has been built. The design is shown in Fig. B-5. The device PCM-78P is a serial output type A/D converter with the conversion time of  $6.2 \mu s$  under  $6 MHz$  operating clock frequency. After receiving a "start" signal from the multi-DSP controller, the four channel input signals are sampled simultaneously and held by four S/H devices SHC-5320s. Then the four sampled signals are sent to the A/D converter sequentially through the multiplexer 4052. The four digital output data from the A/D are transmitted to the DSP #3 through a serial port. The whole A/D conversion procedure is controlled by the PAL control circuit consisting of the chips PAL-ADC-#1 and #2. A time of  $33 \mu s$  is needed for a complete conversion cycle. Fig. B-6 shows the implementation of the circuit. Tables B-7 and B-8 list the programs of the PAL control circuit designs.

## B.5 Voltage Sensor Circuit

The broad bandwidth voltage sensor circuit shown in Fig. B-7 is used to measure the ac capacitor voltage waveform in the feedback control.

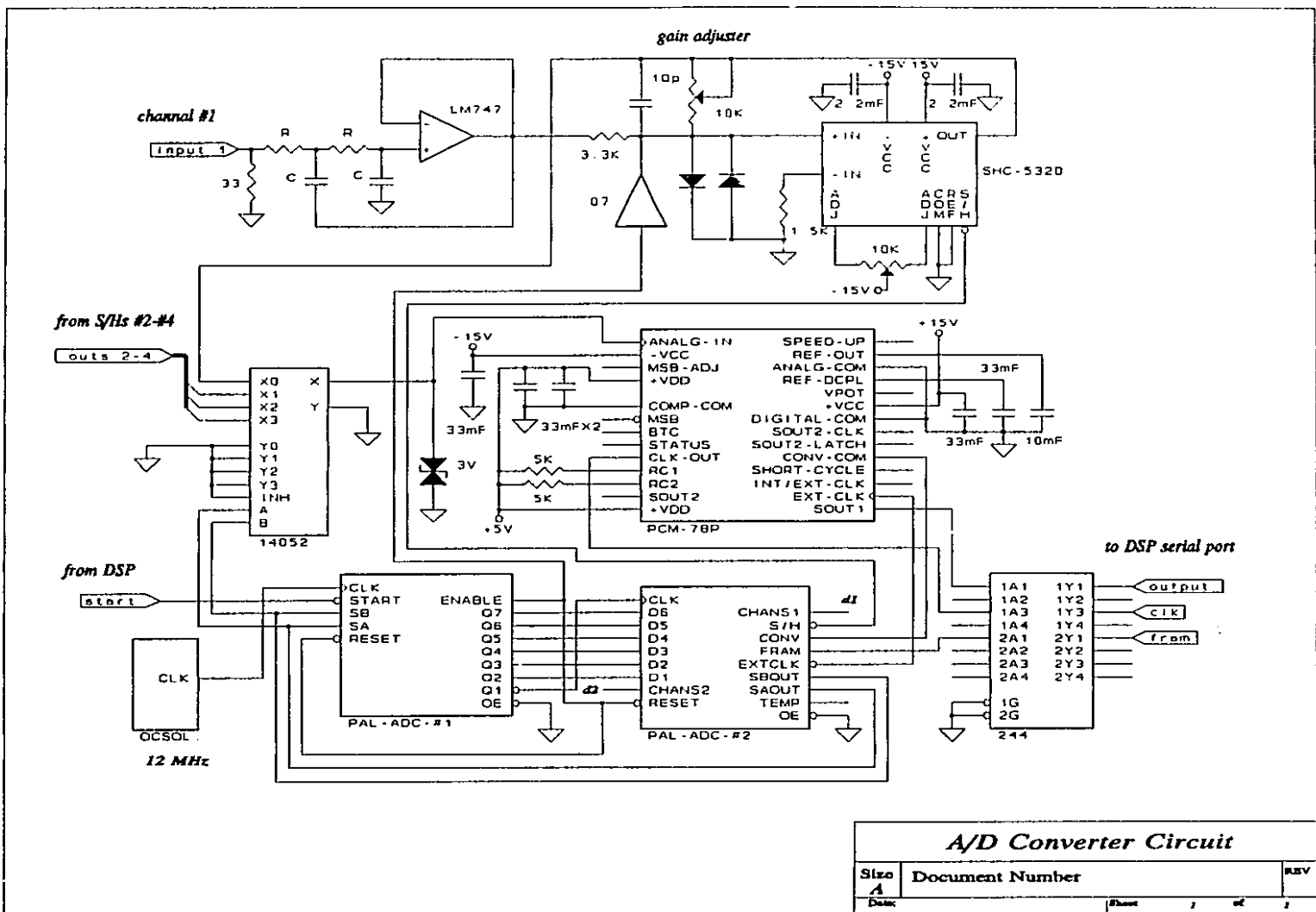


Figure B-5 The A/D converter circuit

Table B-7 The Program List of PAL Chip PAL-ADC-#2 Design.

```

*****
* CHIP NAME   : PAL-A/D#2
* FUNCTION    : A/D control circuit (2), control analog-multiplexer, generate sampling, conv, ext.clock
*              and frame pulses.
*              clock is the LSB of the PAL-A/D#1
*****

| PAL16RP8 In: (d[6-1], chann2, reset),
|           lo: (chann1, temp),
|           out: (sh, conv, frm, extclk, sb, sa),
|           clock: clk
|
| active-low: sh, reset
|
| temp = 1 ?? d[6-1] = -0
|
| chann1 = 0 ?? 0 | to be used as input pin
|
| sh = (d[6-1] = -62 # d[6-1] = -61 # d[6-1] = -60 # d[6-1] = -59 # d[6-1] = -58 # d[6-1] = -57
|      # d[6-1] = -56 # d[6-1] = -55 # d[6-1] = -54 # d[6-1] = -53 # d[6-1] = -52 # d[6-1] = -51
|      # d[6-1] = -50 # d[6-1] = -49 # d[6-1] = -48 # d[6-1] = -47 # d[6-1] = -46 # d[6-1] = -45)
|      & reset'
|
| conv = d[6-1] = -37 & reset'
|
| frm = (d[6-1] = -35
|      # d[6-1] = -34) & reset'
|
| extclk = (d[6-1] = -35 # d[6-1] = -33 # d[6-1] = -31 # d[6-1] = -29 # d[6-1] = -27
|          # d[6-1] = -25 # d[6-1] = -23 # d[6-1] = -21 # d[6-1] = -19 # d[6-1] = -17
|          # d[6-1] = -15 # d[6-1] = -13 # d[6-1] = -11 # d[6-1] = -09 # d[6-1] = -07
|          # d[6-1] = -05 # d[6-1] = -03) & reset'
|
| sb = ((chann2 & chann1 & sb & sa' & d[6-1] = -0)
|      # (chann2 & sb' & sa & d[6-1] = -0)
|      # (sb & temp')) & reset'
|
| sa = ((chann2 & chann1 & sa' & d[6-1] = -0)
|      # (chann2 & sb' & sa' & d[6-1] = -0)
|      # (chann1 & sb' & sa' & d[6-1] = -0)
|      # (sa & temp')) & reset'

```

Table B-8 The Program List of PAL chip PAL-ADC-#1 Design.

```

*****
* CHIP NAME   : PAL-A/D#1
* FUNCTION    : A/D converter control circuit (1), control "enable" signal, record states
*****

| PAL16RP8 In: (start, sb, sa, reset),
|           out: (enable, q[7-1]),
|           clock: clk
|
| active-low: start, q1, reset
|
| enable = start
|          # ((sb' & sa' & q[7-1] = -0) & reset')
|
| map: q[7-1] -> q[7-1]
| { n -> n-1, n/-0 & reset'
|   n -> 88, n = -0 & (sb # sa) & reset'
|   n -> 127, (n = -0 & sb' & sa' & reset') # reset' }

```

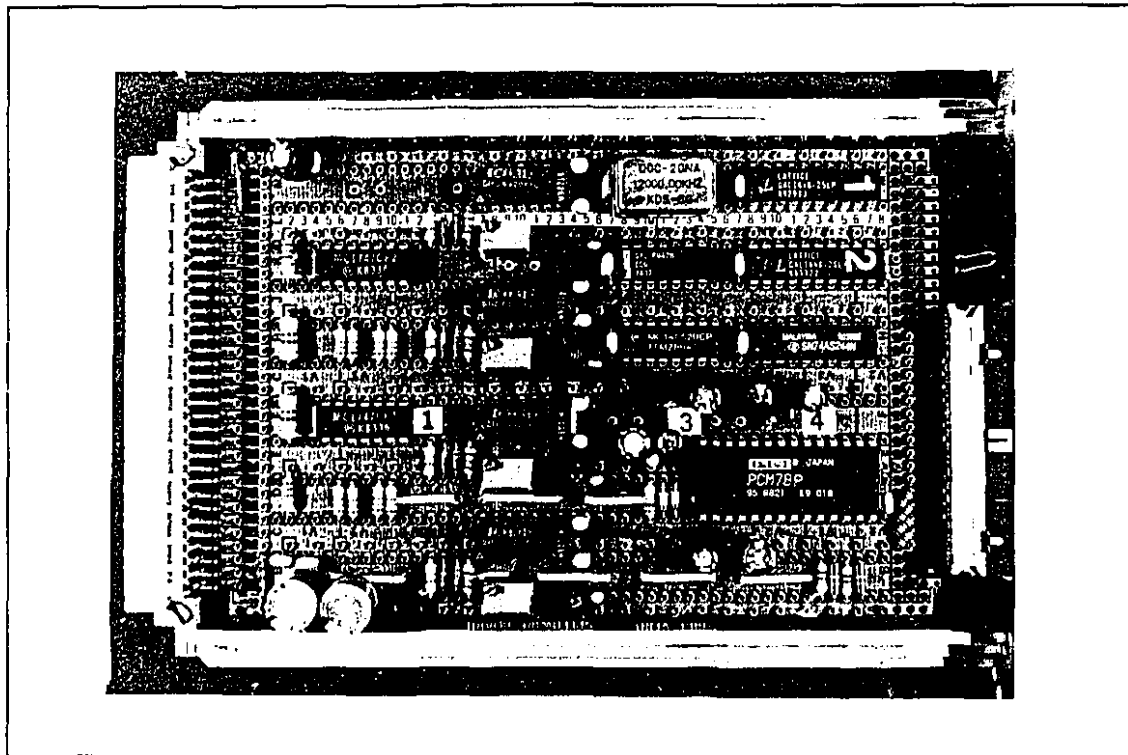


Figure B-6 The A/D converter circuit implementation using speedwire board.

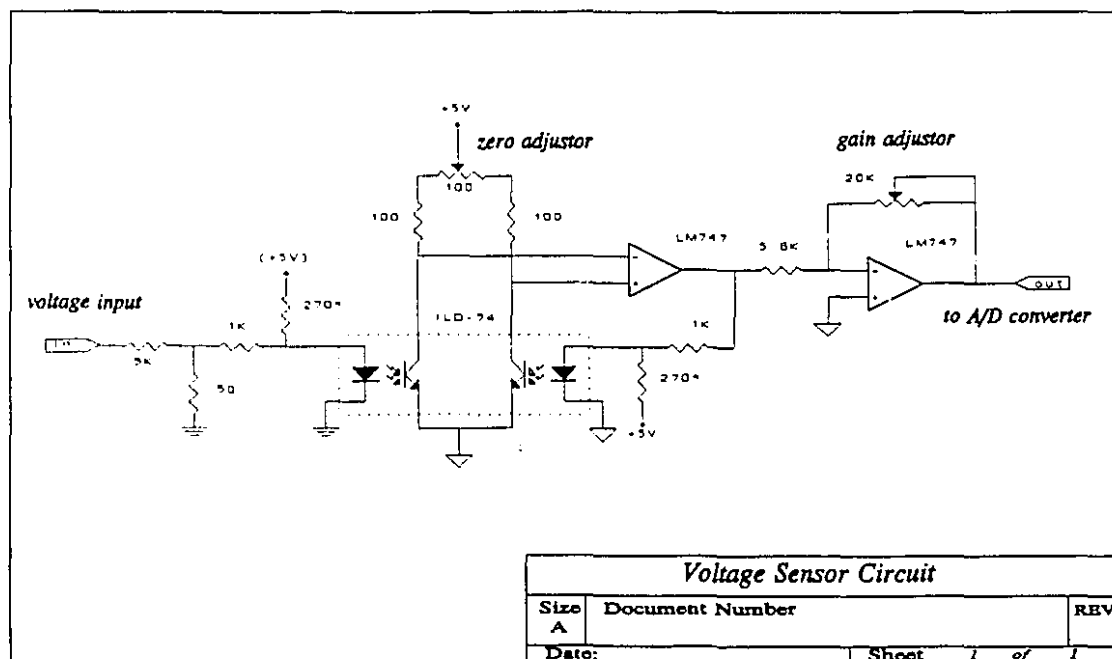


Figure B-7 The ac capacitor voltage sensor circuit.

## **SOFTWARE DESIGN OF MULTI-DSP CONTROL**

### **C.1 Introduction**

The controls of the 6-valve, 3-phase, current-source PWM converter, using the Dynamic Tri-Logic SPWM and the Pole Placement control methods described in **Chapters 5** and **6**, have been implemented by a multi-DSP controller. The controller has been designed and constructed in our laboratory. A detailed description of the hardware design of the controller can be found in Refs. [94-96]. A brief descriptions of the software is given in here. The software is designed to be executed in parallel, in real-time.

### **C.2 Control Task Distribution**

In the Pole-Placement feedback control design of Fig. 6-3 in **Chapter 6**, the computation tasks which implement the system feedback configuration of Fig. 6-4

are distributed as follows:

**DSP #1:** User interface through the serial communication with Personal Computer. It allows the user to change and display the control parameters and the converter status in real-time.

**DSP #2:** Sampling the dc link current  $I_{dc}(t_k)$ ; calculating the 3-phase in-phase and in-quadrature reference waveforms  $\sin(t_k - \theta_j)$  and  $\cos(t_k - \theta_j)$  for  $j=a$  and  $b$ ; performing *phase lock loop* (PLL) control to synchronize the reference waveforms to the utility ac line voltages; calculating Eqs. (6.6) and (6.7) and the Bi-Logic SPWM timer settings for phases- $a$  and  $b$  using the "four timer" method [93]; outputting the 3-phase Bi-Logic SPWM signals.

**DSP #3:** Sampling the ac line currents  $i_{sj}(t_k)$  and the capacitor voltages  $v_{cj}(t_k)$  for  $j=a$  and  $b$ ; getting  $i_{so}(t_k)$  by doing the dc link current  $P$ - $I$  regulation; calculating the steady-state waveform templates  $i_{sjo}(t_k)$  and  $v_{cjo}(t_k)$  for  $j=a$  and  $b$ ; calculating the SPWM timer setting for phase- $c$ .

### C.3 Program Flow Charts and Lists

Fig. C-1 shows the flow charts of three DSP's "main" programs, whose functions are to initialize the system and then control the flashing of the LEDs on the multi-DSP controller board to indicate the operating status of each DSP. In the experiments, the program of DSP #3 is started firstly, then DSP #2 and DSP #1. After the three DSPs have completed the initialization tasks, DSP #1 sends an interrupt signal to DSP #2 to start the parallel calculations. Then it jumps to

its system monitor program, which is stored in its EPROMs, to execute the interfacing function with the PC computer. Having received the interrupt signal from DSP #1, DSP #2 starts its on-chip timer to control the beginning instant of each sampling control period in the parallel calculations of three DSPs.

Once DSP #2 receives an interrupt signal from its on-chip timer, in the interrupt service subroutine "MTIMINT" it sends two interrupt signals to DSP #1 and DSP #3 respectively. Then the three DSPs start the sampling feedback control calculations in parallel. As shown in flow charts of Figs. C-2 and C-3, the interrupt service subroutines "MTIMINT" and "P3RP2IT" perform the main feedback control tasks. In order to keep the parallel calculations in-step, after finishing one stage of the calculation each DSP sends a "ready" signal to the synchronizing circuit on the controller board. When the synchronizing circuit has received three "ready" signals, it send a "all-ready" signal back to each of DSPs to allow them to continue the calculations in next stage.

Although the main task of DSP #1 is interfacing with the PC, it has to send out the "ready" signals to the synchronizing circuit in its interrupt service subroutine to keep the synchronizing circuit working properly. The flow chart of its interrupt service subroutine is not shown here.

The flow charts of the subroutines, which are used to initialize the A/D and D/A converters, to transmit the sampled data, to measure the ac voltage phase angle, etc., are not shown here. The reader can easily work out the details from the program lists shown in Tables C-1, C-2 and C-3.



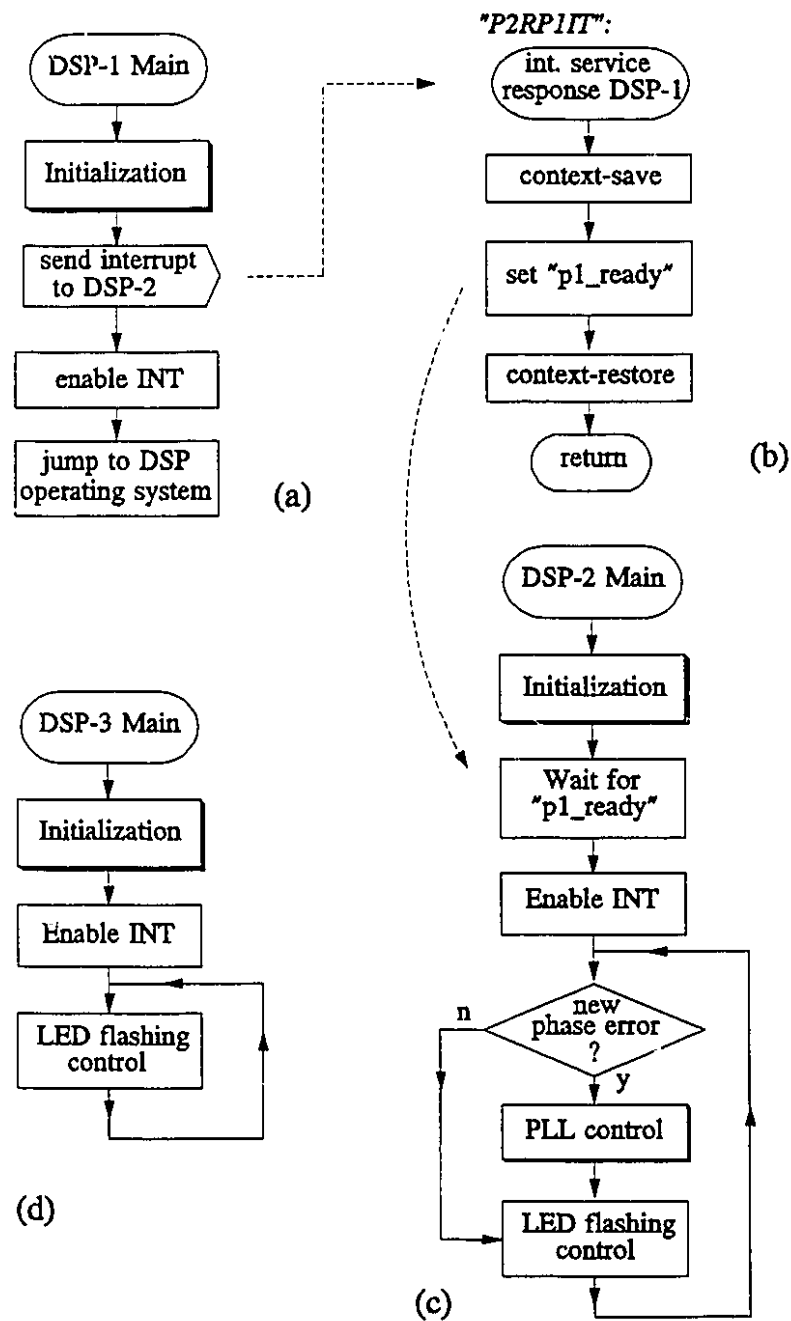


Figure C-1 Flow charts of DSP "main" programs. (a) DSP #1 The main program, (b) interrupt service subroutine "P1RP1IT" of DSP #2 , (c) DSP #2 main program, (d) DSP #3 main program.

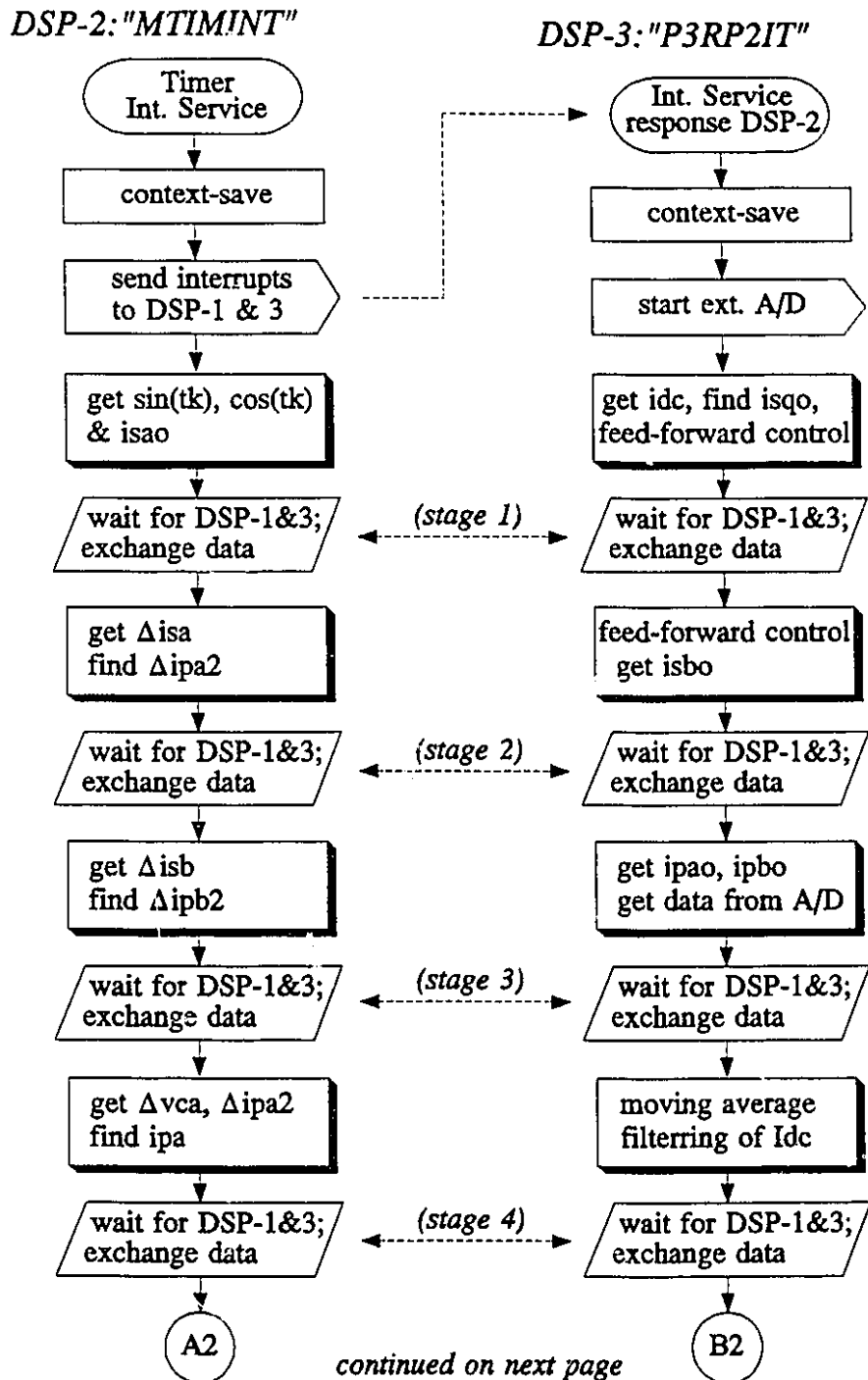


Figure C-2 The flow charts of interrupt service subroutines for parallel processing controls. (continued on Fig. C-3)

continued from last page

DSP-2: "MTIMINT"

DSP-3: "P3RP2IT"

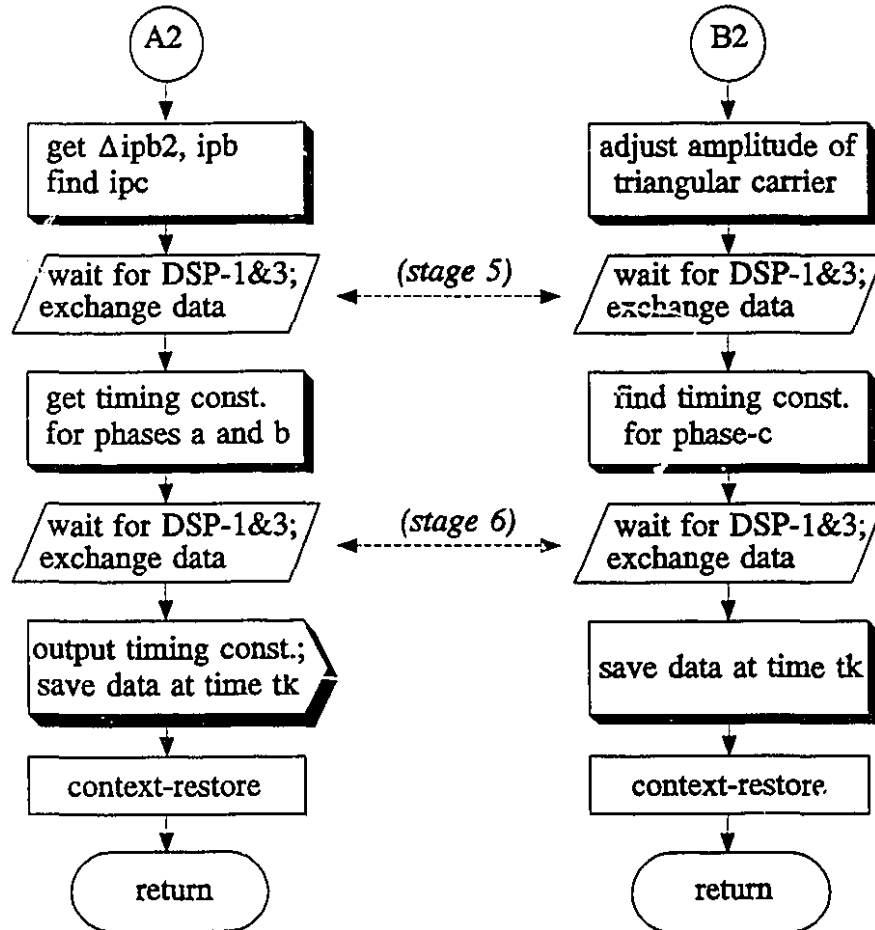


Figure C-3 The flow charts of interrupt service subroutines for parallel processing controls. (continued from Fig. C-2)

For more details about the compiling, linking, loading and executing procedures, please see the Refs. [99,100].

Table C-1 The List of DSP-2 Control Program.

<pre> ***** * Name      : DSP-2.ASM * Function  : parallel processing with DSP-1.ASM and DSP-3.ASM. *            start dsp1 and dsp3 at the beginning of each control period, measure ldc or ldcref *            using the A/D on the DSP board. * Input     : Interrupted by DSP #1 for starting parallel processing. *            data from DSP #3 and PC passing through global memory. * Output    : 3-phase BI-Logic SPWM trigger signals to PAL circuit. *            data required by DSP #3 to global memory. ***** </pre>			
.title	'DSP2 PROGRAM'		; *- page 0 (00000h-0007Fh) -*
DRR	.equ	00000h	
DXR	.equ	00001h	
TIM	.equ	00002h	
PRD	.equ	00003h	
IMR	.equ	00004h	
BCODE	.equ	00079h	; *- for Initializing Interrupt vectors -*
VINT0	.equ	0007Ah	
VINT1	.equ	0007Bh	
VINT2	.equ	0007Ch	
VTINT	.equ	0007Dh	
VRINT	.equ	0007Eh	
VXINT	.equ	0007Fh	
SMARK	.equ	00200h	; *- page 4 (00200h-0027Fh) -*
TRSIGN	.equ	00201h	; control output
TRAMGN	.equ	00202h	; sign: triangle rising and falling
FRONC	.equ	00203h	; triangle carrier magnitude
PHERR	.equ	00204h	; frequency reference
NEWPHE	.equ	00205h	; phase error in PLL at time kT
KPSYNC	.equ	00206h	; sign: new phase error is measured
DETFC	.equ	00207h	; proportional gain of PLL
PRDBAK	.equ	00208h	; frequency adjusting output
SCOUNT	.equ	00209h	; back-up of main timer constant
INSIDE	.equ	0020Ah	; time-pointer: kT
FCOUNT	.equ	0020Bh	; sign: time pointer has been increased
SWITCH	.equ	0020Ch	; LED flashing time control
P1READY	.equ	0020Dh	; control for closing inner loop
ADGIDC	.equ	0020Eh	; sign: starting signal is sent from DSP-1
SIND	.equ	0020Fh	; ldc(kT)
COSD	.equ	00210h	; sin(kT-dt)
SIN120D	.equ	00211h	; cos(kT-dt)
COS120D	.equ	00212h	; sin(kT-120-dt)
SINA	.equ	00213h	; cos(kT-120-dt)
COSA	.equ	00214h	; sin(kT + 1.5dt)
SIN120A	.equ	00215h	; cos(kT + 1.5dt)
COS120A	.equ	00216h	; sin(kT-120 + 1.5dt)
IACA_A	.equ	00217h	; cos(kT-120 + 1.5dt)
IACB_B	.equ	00218h	; isa[(k-1)T]
VCAFA_A	.equ	00219h	; isb[(k-1)T]
VCAFB_B	.equ	0021Ah	; Vca[(k-1)T]
AVGIACA	.equ	0021Bh	; Vcb[(k-1)T]
AVGIACB	.equ	0021Ch	; [isa[(k-1)T] - isb(kT)]/2
AVGVCAFA	.equ	0021Dh	; [isb[(k-1)T] - isb(kT)]/2
AVGVCAFB	.equ	0021Eh	; [Vca[(k-1)T] - Vca(kT)]/2
IACAO	.equ	0021Fh	; [Vcb[(k-1)T] - Vcb(kT)]/2
DETIACA	.equ	00220h	; isao(kT)
DETIACB	.equ	00221h	; delta_isa(kT)
DETVCAFA	.equ	00222h	; delta_isb(kT)
DETVCAFB	.equ	00223h	; delta_Vca(kT)
			; delta_Vcb(kT)
ICTRLA	.equ	00224h	; va(kT)
ICTRLB	.equ	00225h	; vb(kT)
DETIPA	.equ	00226h	; ks_4*va
DETIPAP	.equ	00227h	; ks_1*delta_isa + ks_2*delta_Vca + ks_3*delta_Ua(k-1)
DETIPBI	.equ	00228h	; ks_4*vb
DETIPBP	.equ	00229h	; ks_1*delta_isb + ks_2*delta_Vcb + ks_3*delta_Ub(k-1)
DETIPA	.equ	0022Ah	; Ua(kT)
DETIPB	.equ	0022Bh	; Ub(kT)
DETIPA_A	.equ	0022Ch	; Ua[(k-1)T]
DETIPB_B	.equ	0022Dh	; Ub[(k-1)T]
IPA	.equ	0022Eh	; isao + Ua
IPB	.equ	0022Fh	; isbo + Ub
IPC	.equ	00230h	; isco + Uc
IMPA	.equ	00231h	; Sma
IMPB	.equ	00232h	; Smb
IMPC	.equ	00233h	; Smc
CONSTA	.equ	00234h	; SPWM timing constant of phase a
CONSTB	.equ	00235h	; SPWM timing constant of phase b
CONSTC	.equ	00236h	; SPWM timing constant of phase c
KS_1	.equ	00237h	; state feedback gain K1
KS_2	.equ	00238h	; state feedback gain K2
KS_3	.equ	00239h	; state feedback gain K3
KS_4	.equ	0023Ah	; state feedback gain K4
SQR23	.equ	0023Bh	; constant
SYNCTT1	.equ	0023Ch	
SYNCTT2	.equ	0023Dh	
TEMP1	.equ	0023Eh	
TEMP2	.equ	0023Fh	
TEMP3	.equ	00240h	
TEMP4	.equ	00241h	
DADATA	.equ	00242h	; data for D/A output
DAOUT	.equ	00243h	; pointer of D/A output data
GDATP3	.equ	08004h	; *- global memory (page #256, 08000h) -*
GP2INDEX	.equ	08005h	; sign: display data in DSP-2 or DSP-3
GP3INDEX	.equ	08006h	; index of DSP-2's data to be displayed
GP3DA	.equ	08007h	; index of DSP-3's data to be displayed
GKPIDC	.equ	08010h	; DSP-3's data to be displayed
GKIIDC	.equ	08011h	; pc-controlled variables
GISTEP	.equ	08012h	; proportional gain of outer loop
GSWITCH	.equ	08014h	; integral gain of outer loop
GIREF	.equ	08017h	; command for step change of ldc ref
			; command for closing inner loop
			; ldc ref
			; exchanged data: from DSP-3
GIACA	.equ	08018h	
GIACB	.equ	08019h	
GVCAPA	.equ	0801Ah	
GVCAPB	.equ	0801Bh	
GVSQO	.equ	08020h	
GISQO	.equ	08021h	
GIACAO	.equ	08022h	
GIACBO	.equ	08023h	
GVCAPAO	.equ	08024h	
GVCAPBO	.equ	08025h	
GIPAO	.equ	08026h	
GIPBO	.equ	08027h	
			; exchanged data: to DSP-3
GSIND	.equ	08030h	
GCOSD	.equ	08031h	
GSIN120D	.equ	08032h	
GCOS120D	.equ	08033h	
GSINA	.equ	08034h	
GCOSA	.equ	08035h	
GSIN120A	.equ	08036h	
GCOS120A	.equ	08037h	

```
GADCIDC .equ 08038h
GPRDBAK .equ 08039h
GTRSIGN .equ 0803Ah
GTRAMGN .equ 0803Bh
GIMPC .equ 0803Ch
GCONSTC .equ 0803Dh
```

```
DEG30 .equ 00068h
DEG60 .equ 000D2h
DEG90 .equ 00138h
DEG150 .equ 0020Dh
TWOPI .equ 004ECh
HALFDA .equ 0000Fh
ONEHAFOA .equ 00017h
ICTRLMT .equ 06800h
SINTABLE .equ 00300h
COEFF .equ 05B48h
FCUMT .equ 00D00h
```

```
/* constants */
DEG30 = 105
DEG60 = 210
DEG90 = 315
DEG150 = 525
TWOPI = 1260
DA = 15
1.5*DA
xxxx xxx.x xxx xxx
pointer of sin-table
2*coeff (coefficient)
frequency limit
```

\*\*\*\*\* Initialization \*\*\*\*\*

```
START .sect "P2INIT"
DINT
SSXM
LDPK 00000h
; point to data page 0
; initialize interrupt vector
; interrupt vector for int0
; interrupt vector for int2.
; interrupt vector for on chip timer
; interrupt vector for A/D (serial port)
; interrupt vector for D/A (serial port)
; load "branch" operating code
; point to vectors address set by EPROM
; load interrupt vectors
ADDK 00001h
TBLW VINT0
ADDK 00003h
TBLW BCODE
ADDK 00001h
TBLW VINT2
ADDK 00001h
TBLW BCODE
ADDK 00001h
TBLW VTINT
ADDK 00001h
TBLW BCODE
ADDK 00001h
TBLW VRINT
ADDK 00001h
TBLW BCODE
ADDK 00001h
TBLW VXINT
LACK 00001h
SACL IMR
; enable int0 only
LALK 00F7Fh
SACL PRD
; 1/(60*42) = 3968*100ns
; start main timer
```

```
LRLK AR0,00280h
LRLK AR1,002C0h
LRLK AR2,002E0h
LRLK AR3,00281h
LRLK AR4,00200h
LRLK AR5,00300h
LRLK AR6,00320h
LRLK AR7,00340h
```

```
LARP 00004h
LACK 00000h
RPTK 255
SACL *+
RPTK 255
SACL *+
```

```
LARP 00003h
LALK 00000h
SACL *+
LALK 0FFE3h
SACL *+
LACK 00003h
SACL *+
LALK 01E3Eh
SACL *+
LACK 00003h
SACL *+
LALK 02244h
SACL *
```

```
LDPK 00004h
LALK 0F207h
SACL SMARK
OUT SMARK,0Fh
OUT SMARK,08h
OUT SMARK,09h
ANDK 0AFFh
SACL SMARK
```

```
LACK 00001h
SACL TRSIGN
```

```
LALK 05E3Fh
SACL FRQNC
```

```
LALK 03800h
SACL KPSYNC
```

```
LALK 00F7Fh
SACL PRDBAK
```

```
LALK 06A1Bh
SACL KS_1
LALK 00641h
SACL KS_2
LALK 03T9Bh
SACL KS_3
LALK 02BF1h
SACL KS_4
LALK 07421h
```

/\* initialize addressing register \*/  
AR0 is used for A/D initialization  
AR1 is used for SYNCINT stack  
AR2 is used for MTIMINT stack  
AR3 is used for A/D initialization

ARS is used for DACUTIT stack  
AR6 is used for ADININT stack  
AR7 is used for P2RP1IT stack

/\* clear registers \*/  
using AR4  
clearing working area

/\* A/D Initialization \*/  
using AR3 for load codes

load first D/A initialization code

/\* point to data page 4 \*/  
initialize SMARK  
turn on 3 LEDs 0000111(7-0)  
reset PWM timers 111100x0(15-8)  
switch A/D converter to channel 0

prepared for starting PWM timers

initialize triangle edge sign

frequency reference = 60 Hz

set the gain of PLL

backup PRD  
/\* initialize state feedback gains \*/  
x.xxx xxxx xxxx xxxx

x.xxx xxxx xxxx xxxx

x.xxx xxxx xxxx xxxx

x.xxx xxxx xxxx xxxx

/\* initialize coefficients \*/

```

SACL    SQR23    :sqr23 = 65536x16368xsqrt(2)/14745/sqrt(3)
                        *- load PWM timing constants -*

LALK    0330h
SACL    00000h
LALK    00202h
SACL    00000h
LALK    00F00h
SACL    00000h
LALK    00200h
SACL    FCOUNT

                        :set LED flashing time control counter

LARP    00004h
LRLK    AR4,08000h
LALK    00000h
RPTK    255
SACL    *+
RPTK    255
SACL    *+

                        *- initialize global memory -*

LRLK    AR4,GKPIDC
LALK    00300h
SACL    *+
LALK    00068h
SACL    *

                        :kpide = xxxx x,xxx xxxx xxxx
                        :gkpide = kpide
                        :klide = xxx.x xxxx xxxx xxxx
                        :gklide = klide

LRLK    AR4,GVSQ3
LALK    03C9Fh
SACL    *

                        *- set ac source voltage amplitude
                        :2*[sqrt(3)*70v] =xxxx xxxx xx,xx xxxx

LRLK    AR4,GIREF
LALK    02000h
SACL    *

                        :ldcref = xxxx xx,xx xxxx xxxx

LRLK    AR4,GPRDBAK
LALK    PRDBAK
SACL    *+
LALK    TRSGN
SACL    *

                        :gprdbak = prdbak
                        :gtrsign = trsign

EINT    :enable interrupt

WAITP1  LAC      P1READY
        BZ      WAITP1

LACK    00020h
LDPK    00000h
SACL    IMR

                        :enable xint only

LACK    00003h
SACL    DXR

                        :start D/A initialization

LDPK    00004h
EINT    :enable interrupt

```

```

* Main Loop
* Function : PLL regulation and LED flashing control
* Input   : NEWPHE, PHERR
* Output  : FRQNC, PRD, PRDBAK, FCOUNT

```

```

ADJFRQ  LAC      NEWPHE
        BZ      FLASH

                        :*- new phase error has been tested -*
DINT    :disable interrupt
LT      PHERR
                        :load phase error to T register

```

```

MPY      KPSYNC
SPM      00002h
SPH      DETFC

                        *- output limit -*

POSFC    LAC      DETFC
        BLZ     NEGFC
        SBLK    FCUMT
        BLZ     ADDFO
        LALK    FCUMT
        SACL    DETFC
        B       ADDFO
NEGFC    ADLK    FCUMT
        BGZ     ADDFO
        LALK    FCUMT
        NEG     DETFC
        SACL    DETFC

                        :if detfc > 0 then
                        :if |detfc| > fclimit then
                        :detfc = fclimit

                        :elseif detfc < 0 then
                        :if |detfc| > fclimit then
                        :detfc = -fclimit

ADDFO    LALK    05E3Fh
        SUB     DETFC
        SACL    FRQNC

                        *- fc = 60Hz-detfc -*

LALK    COEFF,0Fh
RPTK    12
SUBC    FRQNC
LDPK    00000h
SACL    PRD
LDPK    00004h
SACL    PRDBAK

                        :load main timing data to PRD.
                        :backup PRD

CLRSGN   LACK    00000h
        SACL    NEWPHE

                        :clear NEWPHE sign

FLASH    LAC      FCOUNT
        BGZ     ADJEND
        LAC      SMARK
        XORK    0003Fh
        SACL    SMARK
        OUT     SMARK,0Fh
        LALK    00200h
        SACL    FCOUNT

                        :check flashing count
                        :if fcount = 0 then
                        :change LEDs

                        :fcount = 200

ADJEND   B       ADJFRQ

                        :do loop

```

```

* Subroutine : MTIMINT response to the Main-timer interrupt call
* Function   : start DSP-3 and DSP-1 to do parallel calculation
*             : sampling idc, state feedback control, get spwm timing data
* Output     : bi-logic spwm trigger signals
* Call       : PWMRTN1
* Affect     : AR2 is used to save current registers
*             : AR4 is point to global memory.
*             : Temp1-8 are used.

```

```

.sect    "MTIMINT"
MTIMINT  LARP    00022h
        ADRK    0C001h
        SST1    *+
        SST     *+
        SACL    *+
        SPM     00000h
        SPM     *+
        SPL     *+
        MPYK    0C001h

                        *- save current registers -*
                        :point to AR2

```

	SPL	*,4	point to AR4		LAC	SIN120D	
FSTJOB	OUT	SMARK,0Eh	Interrupt DSP-3		ADLK	SINTABLE	
	OUT	SMARK,0Dh	Interrupt DSP-1		TBLR	SIN120D	get sin(w-120-da)
					LAC	COS120D	
PNEXT0	LDPK	00004h			ADLK	SINTABLE	
	LAC	SCC111T	*- kT = kT + dT -*		TBLR	COS120D	get cos(w-120-da)
	ADDK	0001Eh			LAC	SINA	
	SBLK	TWOPI			ADLK	SINTABLE	
	BGEZ	NEXT0			TBLR	SINA	get sin(w+1.5da)
NEXT0	ADLK	TWOPI			LAC	COSA	
	SACL	SCOUNT			ADLK	SINTABLE	
					TBLR	COSA	get cos(w+1.5da)
	LACK	00001h	set INSIDE		LAC	SIN120A	
	SACL	INSIDE			ADLK	SINTABLE	
					TBLR	SIN120A	get sin(w-120+1.5da)
	LAC	SMARK	*- set "busy" signal to sync. circuit -*		LAC	COS120A	
	ANDK	OFF7Fh			ADLK	SINTABLE	
	SACL	SMARK			TBLR	COS120A	get cos(w-120+1.5da)
	OUT	SMARK,0Fh	reset bit7 of port F	SDATAD	LRLK	AR4,GSIND	*- transfer to global memory -*
	EINT				LAC	SIND	
			*- get phase angles -*		SACL	+	
WWTT	LAC	SCOUNT			LAC	COSD	
	SUBK	HALFDA			SACL	+	
	BGEZ	NEXTWT0			LAC	SIN120D	
	ADLK	TWOPI			SACL	+	
NEXTWT0	SACL	SIND	save (kT-da)		LAC	COS120D	
	SUBK	DEG30			SACL	*	*- get isao(kT) -*
	BGEZ	NEXTWT1					
	ADLK	TWOPI		FIACAO	LT	SQR23	
NEXTWT1	SACL	COS120D	save (kT-120-da)+90		MPY	SIND	
	SBLK	DEG90			LRLK	AR4,GISQO	
	BGEZ	NEXTWT2			LTP	*	
	ADLK	TWOPI			SACH	SIND,1	xx.xx xxxx xxxx xxxx
NEXTWT2	SACL	SIN120D	save (kT-120-da)		MPY	SIND	x.xxx xxxx xxxx xxxx
	SBLK	DEG150			LTP	KS_4	
	BGEZ	NEXTWT3			NEG		xxxx x.xxx xxxx xxxx
NEXTWT3	ADLK	TWOPI	save (kT-da)+90		SACH	IACAO,4	*- set "ready" to sync. circuit -*
	SACL	COSD					
					RXF		clear BIO
	LAC	SCOUNT			SXF		
	ADDK	ONEHALFDA			LAC	SMARK	
	SBLK	TWOPI			ORK	00080h	
	BGEZ	NEXTWT4			SACL	SMARK	
	ADLK	TWOPI	save (kT+1.5*da)	WAIT_1	OUT	SMARK,0Fh	set bit7 of port F for "ready"
NEXTWT4	SUBK	SINA			BIOZ	WAIT_1	*- wait for "all-ready" from sync. circuit -*
	BGEZ	DEG30			LAC	SMARK	
	ADLK	NEXTWT5			ANDK	OFF7Fh	
NEXTWT5	SACL	TWOPI	save (kT-120+1.5*da)+90		SACL	SMARK	
	SBLK	COS120A			OUT	SMARK,0Fh	reset bit7 of port F
	BGEZ	DEG90		FAVGIACA			
	ADLK	NEXTWT6			LRLK	AR4,GIACA	AR4 point to GIACA
NEXTWT6	SACL	TWOPI	save (kT-120+1.5*da)		LAC	IACA_A,15	
	SBLK	SIN120A			ADD	*,15	
	BGEZ	DEG150			SACH	AVGIACA	avgIaca = (Iaca + IACA_e)/2
NEXTWT7	ADLK	NEXTWT7			LAC	*	IACA_a = IACA
	SACL	TWOPI	save (kT+1.5*da)+90		SACL	IACA_A	
		COSA	*- look up sin(x) table -*	FDETIACA	LAC	AVGIACA,15	*- get delta-isa -*
SINTAB	LAC	SIND			SUB	IACAO,15	xxxx xx,xx xxxx xxxx
	ADLK	SINTABLE			SACH	DETIACA	yyyy yyyy yyyy yyyy(31-16)
	TBLR	SIND	get sin(w-da)	FICTRLA	LAC	ICTRLA,15	xxxx xxx.x xxxx xxxx
	LAC	COSD			SUB	DETIACA,14	
	ADLK	SINTABLE	get cos(w-da)		SACH	ICTRLA,1	
	TBLR	COSD					

LMT1	LAC	ICTRLA	*- output limit -*
CHKUP1	BLZ	CHKLOW1	
	SBLK	ICTRLMT	
	BLEZ	FDETIPAI	
	LALK	ICTRLMT	
	SACL	ICTRLA	
CHKLOW1	B	FDETIPAI	
	ADLK	ICTRLMT	
	BGEZ	FDETIPAI	
	LALK	ICTRLMT	
	NEG		
	SACL	ICTRLA	
FDETIPAI	MPY	ICTRLA	icrla*ks_4
	LTP	KS_1	XXXX XX.XX XXXX XXXX
	SACH	DETIPAI,2	
FDETIPAP	MPY	DETIACA	detiaca*ks_1
	LTP	KS_3	
	MPY	DETIPA_A	detipa_a*ks_3
	LTS	KS_4	
	SACL	TEMP1	YYY YYY-Y YYY YYY
	SACH	TEMP2	
	LRLK	AR4,GSWITCH	
	LAC	*	load switch
	SACL	SWITCH	
SDATAA	LRLK	AR4,GSINA	transfer data to DSP-3
	LAC	SINA	
	SACL	+	
	LAC	COSA	
	SACL	+	
	LAC	SIN120A	
	SACL	+	
	LAC	COS120A	
	SACL	*	
	RXF		
	SXF		
	LAC	SMARK	
	ORK	00080h	
	SACL	SMARK	
WAIT_2	OUT	SMARK,0Fh	
	BIOZ	WAIT_2	
	LAC	SMARK	
	ANDK	0FF7Fh	
	SACL	SMARK	
	OUT	SMARK,0Fh	
FAVGIACB	LRLK	AR4,GIACB	
	LAC	IACB_B,15	
	ADD	*,15	avgiacb = (iacb + iacb_b)/2
	SACH	AVGIACB	
	LAC	*	iacb_b = iacb
	SACL	IACB_B	
FDETIACB	LAC	AVGIACB,15	
	LRLK	AR4,GIACBO	
	SUB	*,15	XXXX XX.XX XXXX XXXX
	SACH	DETIACB	
FCTRLB	LAC	ICTRLB,15	YYY YYY-Y YYY YYY
	SUB	DETIACB,14	XXXX XXX.X XXXX XXXX
	SACH	ICTRLB,1	

LMT2	LAC	ICTRLB	
CHKUP2	BLZ	CHKLOW2	
	SBLK	ICTRLMT	
	BLEZ	FDETIPBI	
	LALK	ICTRLMT	
	SACL	ICTRLB	
CHKLOW2	B	FDETIPBI	
	ADLK	ICTRLMT	
	BGEZ	FDETIPBI	
	LALK	ICTRLMT	
	NEG		
	SACL	ICTRLB	
FDETIPBI	MPY	ICTRLB	
	LTP	KS_1	XXXX XX.XX XXXX XXXX
	SACH	DETIPBI,2	
FDETIPBP	MPY	DETIACB	
	LTP	KS_3	
	MPY	DETIPB_B	
	LTS	KS_2	
	SACL	TEMP3	
	SACH	TEMP4	
	RXF		
	SXF		
	LAC	SMARK	
	ORK	00080h	
	SACL	SMARK	
WAIT_3	OUT	SMARK,0Fh	
	BIOZ	WAIT_3	
	LAC	SMARK	
	ANDK	0FF7Fh	
	SACL	SMARK	
	OUT	SMARK,0Fh	
FAVGVA	LRLK	AR4,GVCAPA	AR4 point back to gvcapa
	LAC	VCAPA_A,15	
	ADD	*,15	avgvcapa = (vcapa + vcapa_a)/2
	SACH	AVGVCAPA	
	LAC	*	vcapa_a = vcapa
	SACL	VCAPA_A	
FDETVA	LAC	AVGVCAPA	
	LRLK	AR4,GVCAPAO	
	SUB	*	XXXX XXXX XX.XX XXXX
	SACL	DETVCAPA	
FDETIPA2	ZALS	TEMP1	
	ADDDH	TEMP2	
	MPY	DETVCAPA	
	SPM	00002h	using add since ks_2 < 0
	APAC		XXXX XX.XX XXXX XXXX
	3PM	00000h	
	SACH	DETIPAP,1	
FIPA	LRLK	AR4,GIPAO	
	LAC	*	
	SACL	IPA	load ipa
	LACK		
	SACL	00000h	
		DETIPA	initialize detipa
TSIA	LAC	SWITCH	*- test integral control switch -*
	ANDK	0FF00h	
	BZ	TSPA	



ADDIPAI	LAC ADD SACL	DETIPA DETIPAI DETIPA	*- adding Integral control In -*
TSPA	LAC ANDK BZ	SWITCH 000FFh TOTIPA	*- test proportional control switch -*
ADDIPAP	LAC ADD SACL	DETIPA DETIPAP DETIPA	*- adding proportional control In -*
TOTIPA	LAC ADD SACL	IPA DETIPA IPA	*- get output of ipa -*
WAIT_4	RXF SXF LAC ORK SACL OUT BIOZ LAC ANDK SACL OUT	SMARK 00080h SMARK SMARK_0Fh WAIT_4 SMARK 0FF7Fh SMARK SMARK_0Fh	
FAVGVB	LRLK LAC ADD SACH LAC SACL	AR4,GVCAPB VCAPB_B,15 *,15 AVGVCAPB * VCAPB_B	AR4 point back to GVCAPB  $avgvcapb = (vcapb + vcapb\_b)/2$ $vcapb\_b = vcapb$
FOETVB	LAC LRLK SUB SACL	AVGVCAPB AR4,GVCAPB0 * DETVCAPB	*- get detvcapb -*
FDETIPB2	ZALS ADDOH MPY SPM APAC SPM SACH	TEMP3 TEMP4 DETVCAPB 00002h  00000h DETIPBP,1	using add since KS_2<0
FIPB	LRLK LAC SACL	AR4,GIPB0 * IPB	load ipb
	LACK SACL	00000h DETIPB	initialize detipb
TSIB	LAC ANDK BZ	SWITCH 0FF00h TSPB	*- test Integral control switch -*
ADDIPBI	LAC ADD SACL	DETIPB DETIPBI DETIPB	*- adding Integral control in -*
TSPB	LAC ANDK	SWITCH 000FFh	*- test proportional control switch -*
	BZ	TOTIPB	
ADDIPBP	LAC ADD SACL	DETIPB DETIPBP DETIPB	*- adding proportional control In -*
TOTIPB	LAC ADD SACL	IPB DETIPB IPB	*- get output of ipb -*
FIPM	LAC ADD NEG SACL	IPA IPB IPC	$ipc = ipa - ipb$ *- decoupling processing -*
	SUB SACL	IPB IMPC	$impc = ipc - ipb$
	LRLK SACL	AR4,GIMPC *	send impc to global memory
WAIT_5	RXF SXF LAC ORK SACL OUT BIOZ LAC ANDK SACL OUT	SMARK 00080h SMARK SMARK_0Fh WAIT_5 SMARK 0FF7Fh SMARK SMARK_0Fh	
	LAC SUB SACL LAC SUB SACL	IPB IPA IMPB IPA IPC IMPA	$ipmb = ipb - ipa$  $ipma = ipa - ipc$ *- calculating spwm timing data -*
FDATA	LRLK LAC SACL LT	AR4,GTRAMGN * TRAMGN PFDBAK	load triangle magnitude load period variable *- find timing constant for phase A -*
FDATAA	LAC SACL CALL SACL	IMPA TEMP1 SUBRTN1 CONSTA	using temp1 to transfer data ipma to 'subrtn1' save timing data of timer A *- find timing constant for phase B -*
FDATAB	LAC SACL CALL SACL	IMPB TEMP1 SUBRTN1 CONSTB	save timing data of timer B. *- wait for data of timer C -*
	RXF SXF LAC ORK SACL OUT BIOZ LAC ANDK SACL OUT	SMARK 00060h SMARK SMARK_0Fh WAIT_6 SMARK 0FF7Fh SMARK SMARK_0Fh	
WAIT_6			

```

LRLK    AR4,GCONSTC
LAC     *
SACL    CONSTC

LASTP   DINT
OUTTIM  OUT    CONSTA,0Ah
        OUT    CONSTB,0Bh
        OUT    CONSTC,0Ch
        LAC    SMARK,08h
        ORK    0F000h
        SACL   SMARK
        OUT    SMARK,08h

        LAC    DETIPA
        SACL   DETIPA_A
        LAC    DETIPB
        SACL   DETIPB_B

LRLK    AR4,GPRDBAK
LAC     PRDBAK
SACL    *+

LAC     TRSIGN
XORK    00001h
SACL    TRSIGN

BNZ     JUMP1
LAC     SMARK
ANDK    087FFh
SACL    SMARK
JUMP2   JUMP2
LAC     SMARK
ANDK    0AFFh
ORL     00800h
SACL    SMARK

JUMP2   LAC    FCOUNT
        SUBK   00001h
        SACL   FCOUNT

LRLK    AR4,GDATP3
LAC     *
BNZ     DATP2

DATP2   LRLK    AR4,GP2INDEX
        LALK   00200h
        ADD    *
        SACL   DAOUT
        LAR    AR4,DAOUT
        LAC    *
        SACL   DADATA
        B      RECOVW

DATP3   LRLK    AR4,GP3DA
        LAC     *
        SACL    DADATA

RECOVW  LACK    00000h
        SACL    INSIDE

        SPM     00000h
        LARP    00002h
        MAR     *

```

\*- get timing constant of phase C from DSP-3 -\*

\*- output timing constants to PWM timer -\*

disenable all interrupts

start the PWM timers,  
and set/reset trigger register.

release the trigger register.

\*- preparing for next period calculations -\*

AR4 point to global memory

send prdbak to global memory

change the triangle edge sign.

send trsign to global memory

if present one is rising edge, then  
prepare for outputting falling edge

(ready for Q=1/0)

else prepare for outputting rising edge

(ready for Q=0/1)

fcount=fcount-1

\*- output data to D/A, for debugging only -\*

testing which DSP's data will be displayed

\*- display DSP-2's data -\*

point to index

load beginning address of variables

save address

load data to be displayed to  
working register of D/A

\*- display DSP-3's data -\*

load data to be displayed from DSP-3  
to working register of D/A

clear sign of inside

\*- recover previous registers -\*

point to AR2

```

LT      *+
MPYK    00001h
LT      *+
MAR      *+
LPH      *+
ZALS     *+
ADDDH    *+
LST      *+
LST1     *+
EINT
RET

```

.....

\* Subroutine : SUBRTN1 called by MTIMINT

\* Function : calculate the timing constant using 'four timer method'.

\* Input : modulating signal (vm) in 'temp1', period length in T register

\* Output : timing constant in ACC

.....

```

SUBRTN1 BLZ     NEGSGN
        LACK    00000h
        SACL    TEMP2
        B      FRACT

NEGSGN  ABS     TEMP1
        SACL    00001h
        LACK    TEMP2
        SACL    TEMP1
        LAC     SUB
        SUB     TRAMGN
        BLZ     DIVID
        LAC     TRSIGN
        BZ      SIGN0
        LAC     TEMP2
        BZ      PRDMAX
        LACK    00008h
        B      CORRECT
        LAC     PRDBAK
        B      CORRECT
        LAC     TEMP2
        BZ      PRDMIN
        B      PRDMAX
        DIVID    TEMP1
        RPTK    10
        SUBC    TRAMGN
        SACL    TEMP1
        LAC     TEMP2
        BZ      ADDTRA
        ZAC     TEMP1
        SUB     TEMP1
        SACL    TRSIGN
        LAC     MINUS
        BZ      LALK
        ADD     00800h
        B      TEMP1
        MPRDO2  00800h
        LALK    TEMP1
        SUB     TEMP1
        SACL    TEMP1
        MPY     TEMP1
        SPM     00002h
        SPH     TEMP1
        LAC     TEMP1
        CORRECT ADLK 00100h
        RET

```

if vm > 0 then  
set TEMP2 = 0

if vm < 0 then  
vm = |vm|, set TEMP2 = 1

if |vm| > tramgn then  
if trsign = rising then  
if vm < 0 then  
data = prdmin  
else data = prdmax

elseif vm < 0 then  
data = prdmin  
else data = prdmax

quot = xxxx x.xxx xxx x.xxx

if vm < 0 then  
quot = -quot

fetch triangle edge sign

if trsign = rising then  
acc = 1 + quot

else acc = 1 - quot

save (1 +/- vm/tramgn)  
PRD\*(1 +/- vm/tramgn)/2

add offset, since hardware design  
acc = timing constant



```

* Subroutine : ADININ response to RINT, DRR full interrupt call.
* Function   : sample the ldc.
* Output     : ADCIDC and GADCIDC

```

```

.sect "ADININT"
ADININT LARP 00006h ; *- save current registers *-
        ADRK 00001h ; point to AR6
        SST1 *+
        SST *+
        SACH *+
        SACL *,0,7 ; point to AR7
                ; (ldc is connected to channel 1 of A/D)
LCH1 LDPK 00000h ; load ldc
      LAC DRR
      LDPK 00004h ; considering there is a inverter circuit in A/D
      NEG ; send data to ADCIDC
      SACL ADCIDC ; send to global memory
      LRLK AR7,GADCIDC
      SACL *,0,6 ; point back to AR6
                ; *- recover previous registers *-
RECOVA ZALS *-
        ADDH *-
        LST *-
        LST1 *-
        EINT ; ***. enable interrupt ***
        RET

```

```

* Subroutine : P2RP1IT response to DSP-1 Interrupt call from int0
* Function : set the sign to ask DSP-2 to start the parallel processing.

```

```

.sect "P2RP1IT"
P2RP1IT LARP 00007h ; *- save current registers *-
        ADRK 00001h ; point to AR7
        SST1 *+
        SST *+
        SACH *+
        SACL *+
                ;
        LACK 00001h
        SACL P1READY ; set sign of P1READY
                ; *- recover previous registers *-
RECOVP ZALS *-
        ADDH *-
        LST *-
        LST1 *-
        RET

```

```

.end

```

```

*** end of file ***

```

Table C-2 The List of DSP-3 Control Program.

```

*Name : DSP-3.ASM
*Function : Parallel processing with DSP-2.ASM and DSP-1.ASM
            ; measure isa, isb, vcapa and vcapb using the A/D in PAL circuits box
*Input : Interrupted by DSP #2 to start each sampling control calculation.
*Output : transfer inter-medium results and timing constant of phase-C to DSP #2

```

```

.title "DSP-3 Program"

```

```

; *- page 0 (00000h-0007Fh) *-
; (see dsp-2.asm)
DRR .equ 00000h
DXR .equ 00001h
TIM .equ 00002h
PRD .equ 00003h
IMR .equ 00004h
BCODE .equ 00079h
VINT0 .equ 0007Ah
VINT1 .equ 0007Bh
VINT2 .equ 0007Ch
VTINT .equ 0007Dh
VPRINT .equ 0007Eh
VXINT .equ 0007Fh

; *- page 4 (00200h-0027Fh) *-
SMARK .equ 00200h
FCOUNT .equ 00201h
ADINNO .equ 00202h
ADINDAT1 .equ 00203h
ADINDAT2 .equ 00204h
ADINDAT3 .equ 00205h
ADINDAT4 .equ 00206h
IDCERR .equ 00207h
INTERR .equ 00208h
SIND .equ 00209h
COSD .equ 0020Ah
SIN120D .equ 0020Bh
COS120D .equ 0020Ch
SINA .equ 0020Dh
COSA .equ 0020Eh
SIN120A .equ 0020Fh
COS120A .equ 00210h
SQR23 .equ 00211h
ISQO .equ 00212h
IACBO .equ 00213h
VCDO .equ 00214h
VCOO .equ 00215h
VCAPAO .equ 00216h
VCAPBO .equ 00217h
IPDO .equ 00218h
IPQO .equ 00219h
IPAO .equ 0021Ah
IPBO .equ 0021Bh
ADGIDC .equ 0021Ch
IDCREf .equ 0021Dh
INV42 .equ 00220h
TRAMGN .equ 00221h
PROBAK .equ 00222h
TRSIGN .equ 00223h
HIG1_1122 .equ 00224h
HIG1_1221 .equ 00225h
KIF1_1221 .equ 00226h
TEMP1 .equ 00227h
TEMP2 .equ 00228h

```

```

;
; isqo[k] = xxxx xxx.x xxx xxx
; iacbo[k] = xxxx x.xxx xxx xxx
; vcdo[k] = xxxx xxx.x xxx xxx
; vcqo[k] = xxxx xxx.x xxx xxx
; vcapao[k] = xxxx xxx.x xxx xxx
; vcapbo[k] = xxxx xxx.x xxx xxx
; ipdo[k] = xxxx x.x xxx xxx
; ipqo[k] = xxxx x.x xxx xxx
; ipao[k] = xxxx x.x xxx xxx
; ipbo[k] = xxxx x.x xxx xxx
; dc link current xxxx x.x xxx xxx
; ldc reference xxxx x.x xxx xxx
; save data of '1/42'
; triangle magnitude xxxx x.x xxx xxx

```

```

; feedforward control parameters
;

```

```

TEMP3 .equ 00228h
TEMP4 .equ 0022Ah
DAOUT .equ 0022Bh ; saving data to be displayed
AVG2IDC .equ 0022Eh ; switching harmonic filter output of ldc
SUMIDCL .equ 0022Fh
SUMIDCH .equ 00230h ; 42 points sum of ldc
MAVGIDC .equ 00231h ; moving average filter output of ldc
SUMIAL .equ 00232h
SUMIAH .equ 00233h ; 42 points sum of isa
AVGIA .equ 00234h ; moving average filter output of isa
SUMIBL .equ 00235h
SUMIBH .equ 00236h ; 42 points sum of isb
AVGIB .equ 00237h ; moving average filter output of isb
SUMVCAH .equ 00238h
SUMVCAH .equ 00239h ; 42 points sum of vcapa
AVGVCA .equ 0023Ah ; moving average filter output of vcapa
SUMVCBL .equ 0023Bh
SUMVCBL .equ 0023Ch ; 42 points sum of vcapb
AVGVCB .equ 0023Dh ; moving average filter output of vcapb
SWAVG .equ 0023Eh ; sign: removing offset in sensor

MIDC_1 .equ 002D6h ; 42 points ldc
MIDC_42 .equ 002FFh
IACA_1 .equ 00300h ; 42 points isa
IACA_42 .equ 00329h
IACB_1 .equ 0032Ah ; 42 points isb
IACB_42 .equ 00353h
VCA_1 .equ 00354h ; 42 points vcapa
VCA_42 .equ 0037Dh
VCB_1 .equ 0037Eh ; 42 points vcapb
VCB_42 .equ 003A7h ; *- global memory (page No.256, > 08000h) *-

GDATP3 .equ 08004h
GP2INDEX .equ 08005h
GP3INDEX .equ 08006h
GP3DA .equ 08007h ; p:-controlled variables

GKPIDC .equ 08010h
GKIDC .equ 08011h
GISTEP .equ 08012h
GSWITCH .equ 08014h

GIREF .equ 08017h ; exchanged data: to DSP-2

GIACA .equ 08018h
GIACB .equ 08019h
GVCAPK .equ 0801Ah
GVCAPB .equ 0801Bh

GVSQO .equ 08020h
GISQO .equ 08021h
GIACAO .equ 08022h
GIACBO .equ 08023h
GVCAPAO .equ 08024h
GVCAPBO .equ 08025h
GIPAO .equ 08026h
GIPBO .equ 08027h ; exchanged data: from DSP-2

GSIND .equ 08030h
GOOSD .equ 08031h
GSIN120D .equ 08032h
GCOS120D .equ 08033h
GSINA .equ 08034h
GCOSA .equ 08035h
GSIN120A .equ 08036h
GCOS120A .equ 08037h

```

```

GADCIDC .equ 08038h
GPRDBAK .equ 08039h
GTRSIGN .equ 0803Ah
GTRAMGN .equ 0803Bh
GIMPC .equ 0803Ch
GCONSTC .equ 0803Dh ; *- constants *-

IDCINLMT .equ 08000h ; XXXX XXXX.XXXX XXXX
ISQOLMT .equ 01A00h ; XXXX XXX.X XXXX XXXX
TRAMIN .equ 01400h ; XXXX XX.XX XXXX XXXX

***** initialization *****
*
.sect "P3INIT"
START DINT
SSXM
LDPK 00000h ; point to data page 0
; *- initial interrupt vectors *-
; interrupt vector for P3RP2IT
LALK P3RP2IT
SACL VINT2
LALK ADININT ; interrupt vector for A/D
SACL VRINT
LALK 0FF80h ; get branch operating code
SACL BCODE
LALK 03FF0h ; get first vector address
ADDK 00004h
TBLW BCODE ; load branch instruction code
ADDK 00001h ; acc = 03FF5h
TBLW VINT2
ADDK 00003h
TBLW BCODE
ADDK 00001h
TBLW VRINT

LACK 00014h ; enable RINT INT2
SACL IMR

LRLK AR1,00280h ; *- initialize ARX *-
LRLK AR2,002A0h ; AR1 is used for P3RP2IT stack
LRLK AR4,00200h ; AR2 is used for ADININT stack

LARP 00004h ; point to AR4
LACK 00000h ; clear working area on chip
RPTK 255
SACL *+
RPTK 255
SACL *+

LDPK 00004h ; *- point to page 4 *-
LALK 00038h ; initialize SMARK
SACL SMARK
OUT SMARK,0Fh ; turn on 3 LEDs -> 00111000(0-7)

LALK 00200h ; set LED flashing time control counter
SACL FCOUNT

LACK 00001h
SACL SWAVG ; set sign of

LALK 01CCDh ; *- initialize system matrix *-
SACL HIG1_1122 ; h1g1(2,2) = [-.9](-.1rc) = XXX.X XXXX XXXX XXXX
LALK 05000h ; h1g1(1,2) = 2.5(-.x)
SACL HIG1_1221 ; h1f1(1,2) = 0.0113(-.wc) = ffff XXXX
LALK 02E53h

```

```

SACL      KIF1_1221
LALK      07421h
SACL      SQR23      :sqr23 = 65536x16368xsqrt(2)/14745/sqrt(3)

LALK      06187h
SACL      INV42      :1/42 = y.yyyy xxxx xxxx xxxx

LALK      02000h
SACL      IDCREF      :ldcref = xxxx xx.xx xxxx xxxx
LALK      007D2h
SACL      ISQOO      :just used for first step calculation

EINT      :*- enable Interrupt -*

*****
*                               Main program                               *
* Function : control the LED lights flashing                             *
*****

FLASH     LAC      FCOUNT      :*- LED light flashing control -*
          BGZ      ADJEND      :load flashing time control count

          LAC      SMARK      :if fcount = 0 then
          XORK      0003Fh      :interchange lights
          SACL      SMARK
          OUT      SMARK,0Fh
          LALK      00200h      :set fcount
          SACL      FCOUNT      :fcount = 200
          B        FLASH      :do loop
          ADJEND

*****
* Subroutine : P3RP2IT,ASM response to DSP-2 interrupt call              *
* Function   : parallel processing with DSP-2, sampling isa, isb, vcpea and vcapb *
*****

.sect "P3RP2IT"

P3RP2IT   LARP      00001h      :*- save current registers -*
          ADRK      00001h      :point to AR1
          SST1      *+
          SST       *+
          SACH      *+
          SACL      *,0,4      :point to AR4

BBP3      OUT      SMARK,0Ch      :start A/D on PAL circuit box
          LRLK      AR3,ADINDAT1 :AR3 point to first A/D data_in address
          LACK      00000h
          SACL      ADINNO      :clear A/D input count

          LAC      SMARK      :*- set "busy" signal to sync. circuit -*
          ANDK      0FF7Fh
          SACL      SMARK
          OUT      SMARK,0Fh

          EINT

          LRLK      AR4,GADCIDC
          LAC      *
          SACL      ADCIDC      :load ldc
          :*- moving average filtering of ldc -*

          LRLK      AR4,MIDC_1
          LAC      *,15
          ADD      ADCIDC,15
          SACH      AVG2IDC      :avg2ldc = (ldc(k) + ldc(k-1))/2

```

```

LREF      LRLK      AR4,GIREF
          LAC      *
          SACL      IDCREF      :load ldcref

FERROR    LAC      IDCREF
          SUB      AVG2IDC
          SACL      IDCERR      :ldcerr = ldcref-avg2ldc
          :*- integral control -*

IIDC      ZALH      INTERR
          SOVM
          ADD      IDCERR,14
          ROVM
          SACH      INTERR      :interr = interr + ldcerr
          :*- proportional control -*

FISQO     LRLK      AR4,GKPIDC
          LT        *
          MPY      IDCERR
          LRLK      AR4,GKIIDC
          LTP      *
          MPY      INTERR
          LRLK      AR4,HIG1_1221
          LTA      *
          NEG      ISQO,4      :isqo = -(ldcerrxKp + interrxKi)
          SACH      :*- limiter -*

          LAC      ISQO
          BLZ      CHKLOW2
          SBLK      ISQOLMT
          BLEZ      SDISQO
          LALK      ISQOLMT
          SACL      ISQO
          B        SDISQO
          ADLK      ISQOLMT
          BGEZ      SDISQO
          LALK      ISQOLMT
          NEG      ISQO
          SACL      ISQO      :if isqo < isqolmt (isqo >= 0) then
          :no change
          :else isqo = isqolmt

          LRLK      AR4,GISQO
          LAC      *
          SACL      ISQO      :if isqo > -isqolmt (isqo < 0) then
          :no change
          :else isqo = -isqolmt

SDISQO    LRLK      AR4,GISQO
          LAC      *
          SACL      ISQO      :*- send isqo to global memory -*

FVCDO     MPY      ISQO
          LTP      HIG1_1122
          SACH      VCDO      :vcdo = hig1(1,2)*isqo

FVCQO     MPY      ISQO
          LTP      KIF1_1221
          NEG
          LRLK      AR4,GVSQO
          SUB      *,15
          SACH      VCQO      :vcqo = -|hig1(2,2)|*isqo-|2*vsqo|

FIPDO     MPY      VCQO
          PAC
          SACH      IPDO      :ipdo = kif1(1,2)*vcqo

FIPQO     MPY      VCDO
          LTP      INV42
          NEG
          SFR
          ADDH      ISQO
          SACH      IPQO,1      :ipqo = -|Kif1(2,1)|*vcdo + isqo

TESTIA    LAC      ADINNO      :waiting for A/D input iaca

```

	BZ	TESTIA			LTP	VCOO	
	LAC	ADINDAT1			MPY	SIN120D	
	NEG				LTS	ISQO	
	SACL	ADINDAT1	considering there is a inverter in sensor		SACH	VCAPBO,2	vcapbo = sqr23x(vcdoxcos120d-vcqoxsin120d)
	LAC	SWAVG	*- test if need to remove sensor drift -*	SVCAPBO	LRLK	AR4,GVCAPBO	send vcapbo to global memory
	BZ	SIACA	*- 42 points moving average filtering -*		SACH	*,2	
RMZIA	ZALS	SUMIAH		FIBO	MPY	SIN120D	
	ADDDH	SUMIAH			LTP	INV42	
	LRLK	AR4,IACA_42			NEG		*- iacbo = sqr23xsin120dxisqo
	SUB	*,12			SACH	IACBO,4	ACC* 16 xxxx x,xxx xxxx xxxx
	ADD	ADINDAT1,12		SIACBO	LRLK	AR4,GIACBO	
	SACL	SUMIAL	sumiah = sumiah-iaca(k-42) + iaca(k)		SACH	*,4	send iacbo to global memory
	SACH	SUMIAH		TESTIB	LAC	ADINNO	*- waiting for iacb -*
	MPY	SUMIAH			SUBK	00002h	
	LTP	AVGIA	avgia = sumiah/42		BLZ	TESTIB	
SIACA	LRLK	AR4,GIACA			LAC	ADINDAT2	load iacb
	LAC	ADINDAT1			NEG	ADINDAT2	considering there is a inverter in sensor
	SUB	AVGIA	iacb = iacb-avgia		SACL		*- test if need to remove sensor drift -*
	SACL	*	*- set "ready" to sync. circuit -*		LAC	SWAVG	*- 42 points moving average filtering -*
	RXF				BZ	SIACB	
	SXF	SMARK	clear BIO	RMZIB	ZALS	SUMIBL	
	LAC	00080h			ADDDH	SUMIBH	
	ORK	SMARK			LRLK	AR4,IACB_42	
	SACL	SMARK			SUB	*,12	
WAIT_1	OUT	SMARK,0Fh	set bit7 of port F for ready		ADD	ADINDAT2,12	
	BIOZ	WAIT_1	*- wait for "all-ready" from sync. circuit -*		SACL	SUMIBL	
	LAC	SMARK			SACH	SUMIBH	sumibh = sumibh-iacb(k-42) + iacb(k)
	ANDK	OFF7Fh			MPY	SUMIBH	
	SACL	SMARK	reset bit7 of port F		LTP	SQR23	
	OUT	SMARK,0Fh			SACH	AVGIB	avgib = sumibh/42
FCOSD	LRLK	AR4,GCOSD		SIACB	LRLK	AR4,GACB	
	MPY	*,	sqr23xcosd		LAC	ADINDAT2	
	PAC	COSD,1	xxx,xxx xxxx xxxx xxxx		SUB	AVGIB	
	SACH				SACL	*	iacb = iacb-avgib
FSIND	MPY	*			RXF		
	LTP	VCOO			SXF	SMARK	
	SACH	SIND,1	sqr23xsind		LAC	00080h	
FVCAPAO	MPY	COSD			ORK	SMARK	
	LTP	VCOO			SACL	SMARK,0Fh	
	MPY	SIND	vcapao = sqr23x(vcdoxcosd-vcqoxsind)	WAIT_2	OUT	WAIT_2	
	LTS	SQR23	xxxx xxxx x,xxx xxxx		BIOZ	SMARK	
	SACH	VCAPAO,2			LAC	OFF7Fh	
SVCAPAO	LRLK	AR4,GVCAPAO	send vcapao to global memory		ANDK	SMARK	
	SACH	*,2			SACL	SMARK,0Fh	
FCOS120D	LRLK	AR4,GCOS120D		FCOSA	LRLK	AR4,GCOOSA	
	MPY	*,			MPY	*,	
	PAC	COS120D,1	sqr23xcos120d		PAC	COSA,1	sqr23xcosa
	SACH			FSINA	MPY	*	
FSIN120D	MPY	*			LTP	IPDO	
	LTP	VCOO	sqr23xsin120d		SACH	SINA,1	sqr23xsina
	SACH	SIN120D,1		FIPAO	MPY	COSA	
FVCAPBO	MPY	COS120D					

	LTP MPY LTS SACH	IPQO SINA SQR23 IPAO,2	ipao = sqr23x(ipdoxcosa-ipqoxsina) xxxx xx.xx xxxx xxxx		SACL SACH	SUMIDCL SUMIDCH	sumidch = sumidch-idc(k-42) + idc(k) xxxx xxxx xx.xx xxxx
SIPAO	LRLK SACH	AR4,GIPAO *,2	send ipao to global memory		MPY PAC SACH	SUMIDCH MAVGIDC	mavgidc = sumidch/42 xxxx xx.xx xxxx xxxx
FCOS120A	LRLK MPY PAC SACH	AR4,GCOS120A *, COS120A,1	sqr23xcos120a	TESTVB	LAC SUBK BLZ	ADINNO 00004h TESTVB	*- waiting for vcapb -*
FSIN120A	MPY LTP SACH	* IPDO SIN120A,1	sqr23xsin120a		LAC BZ	SWAVG SVCAPB	*- test if need to remove sensor drift -* *- 42 point moving average filtering -*
FIPBO	MPY LTP MPY LTS SACH	COS120A IPQO SIN120A INV42 IPBO,2	ipbo = sqr23x(ipdoxcos120a-ipqoxsin120a)	RMZVB	ZALS ADDH LRLK SUB ADD SACL SACH	SUMVCBL SUMVCBH AR4,VCB_42 *,12 ADINDAT4,12 SUMVCBL SUMVCBH	sumvcbh = sumvcbh-vcapb(k-42) + vcapb(k)
SIPBO	LRLK SACH	AR4,GIPBO *,2	send ipbo to global memory		MPY PAC SACH	SUMVCBH AVGVCB	avgvcb = sumvcbh/42
TESTVA	LAC SUBK BLZ	ADINNO 00003h TESTVA	*- waiting for vcapa -* *- test if need to remove sensor drift -* *- 42 points moving average filtering -*	SVCAPB	LRLK LAC SUB SACL	AR4,GVCAPB ADINDAT4 AVGVCB *	vcapb = vcapb-avgvcb
RMZVA	ZALS ADDH LRLK SUB ADD SACL SACH	SUMVCAL SUMVCAH AR4,VCA_42 *,12 ADINDAT3,12 SUMVCAL SUMVCAH	sumvcah = sumvcah-vcapa(k-42) + vcapa(k)		RXF SXF LAC ORF SACL OUT BIOZ LAC ANDK SACL OUT	SMARK 00080h SMARK SMARK,0Fh WAIT_4 SMARK OFF7Fh SMARK SMARK,0Fh	*- get triangle magnitude -* *- minimal limiter -*
	MPY PAC SACH	SUMVCAH AVGVCA	avgvca = sumvcah/42	WAIT_4	LAC SBLK BGEZ LAL ADLK SACH B	MAVGIDC TRAMIN TIMES05 TRAMIN,15 TRAMIN,14 TRAMGN,1 STRAMGN	framgn = 1.5xtramin
SVCAPA	LRLK LAC SUB SACL	AR4,GVCAPA ADINDAT3 AVGVCA *	vcapa = vcapa-avgvca	FTRA	LAC ADD SACH	MAVGIDC,15 MAVGIDC,14 TRAMGN,1	framgn = 1.5xmavgidc
	RXF SXF LAC ORF SACL OUT	SMARK 00080h SMARK SMARK,0Fh		TIMES05	LRLK SACH	AR4,GTRAMGN *,1	send tramgn to global memory
WAIT_3	BIOZ LAC ANDK SACL OUT	WAIT_3 SMARK OFF7Fh SMARK SMARK,0Fh	*- 42 points moving average filtering for idc -*	STRAMGN	LRLK LAC SACL LAC SACL LT	AR4,GPRDBAK *+ PRDBAK * TRSIGN PRDBAK	load PRDBAK load TRSIGN
FMAVGIDC	ZALS ADDH LRLK SUB ADD	SUMIDCL SUMIDCH AR4,MIDC_42 *,12 ADGIDC,12			RXF		



```

WAIT_5      SXF      SMARK
            LAC      00080h
            ORK
            SACL     SMARK
            OUT     SMARK,0Fh
            BIOZ    WAIT_5
            LAC     SMARK
            ANDK    0FF7Fh
            SACL    SMARK
            OUT     SMARK,0Fh

            LRLK     AR4,GIMPC
            LAC      *
            SACL     TEMP1
            BLZ     NEGSGN
            LACK    00000h
            SACL    TEMP2
            B       FRACF
            ABS     TEMP1
            SACL    TEMP1
            LACK    00001h
            SACL    TEMP2
            LAC     TEMP1
            SUB     TRAMGN
            BLZ     DIVD
            LAC     TRSIGN
            BZ      SIGN0
            LAC     TEMP2
            FZ      PRDMAX
            LACK    00008h
            B       CORRECT
            LAC     PRDBAK
            B       CORRECT
            LAC     TEMP2
            BZ      PRDMIN
            B       PRDMAX
            LAC     TEMP1
            ZALH    10
            RPTK    TRAMGN
            SUBC    TEMP1
            SACL    TEMP2
            LAC     ADDTRA
            BZ      TEMP1
            ZAC     TEMP1
            SUB     TRSIGN
            SACL    MINUS
            LAC     00800h
            ADD     TEMP1
            B       MPRDO2
            LACK    00800h
            SUB     TEMP1
            SACL    TEMP1
            MPRDO2  TEMP1
            MPRDO2  TEMP1
            SPY     00002h
            SPY     TEMP1
            LAC     TEMP1
            CORRECT ADLK 00100h

            LRLK     AR4,GCONSTC
            SACL     *

            RZF
            SXF
            LAC     SMARK
            ORK     00080h

```

\*- get timing constant for phase C -\*

load impc

if impc > 0 then  
set temp2 = 0

if impc < 0 then  
impc = |impc|, set temp2 = 1

if |impc| > tramgn then  
if trsign = rising then  
if impc < 0 then

data = prdmin

else data = prdmax

elseif impc < 0 then  
data = prdmin  
else data = prdmax

quot = xxxx x,xxx xxxx xxxx

if impc < 0 then  
quot = -quot

fetch triangle edge sign.

if trsign = rising then  
acc = 1 + temp1

else acc = 1 - temp1

save (1 +/- impc/tramgn)  
PRD\*(1 +/- impc/tramgn)/2

add offset, since hardware design  
acc = timing constant

send constc to global memory

```

WAIT_6      SACL     SMARK
            OUT     SMARK,0Fh
            BIOZ    WAIT_6
            LAC     SMARK
            ANDK    0FF7Fh
            SACL    SMARK
            OUT     SMARK,0Fh

MOVIDC      LRLK     AR4,MIDC_41
            RPTK     40
            DMOV    *
            LRLK     AR4,MIDC_1
            LAC     ADCIDC
            SACL     *

            LAC     SWAVG
            BZ      LASTP

MOVING      LRLK     AR4,VCB_41
            RPTK     168
            DMOV    *
            LRLK     AR4,IACA_1
            LAC     ADINDAT1
            SACL     *
            LRLK     AR4,IACB_1
            LAC     ADINDAT2
            SACL     *
            LRLK     AR4,VCA_1
            LAC     ADINDAT3
            SACL     *
            LRLK     AR4,VCB_1
            LAC     ADINDAT4
            SACL     *

            LAC     SWAVG
            ADDK     00001h
            LAC     FCOUNT
            SUBK     00001h
            SACL     FCOUNT

            LRLK     AR4,GP3INDEX
            LALK     00200h
            ADJ      *
            SACL     DAOUT
            LAR      AR4,DAQLT
            LAC      *
            LRLK     AR4,GP3DA
            SACL     *

RECOVF      LARP     00001h
            ZALS    *
            ADDH    *
            LST     *
            LST1    *
            EINT
            RET

.....
* Subroutine : ADININT.ASM response to A/D data-in interrupt call
* Function : transferring 4 input data from DRR to global memory
* Affect : AR2 is used to save current field, AR3 is used to send data
* Output : ADINNO
.....

.sect "ADININT"
; *- save current registers -*

```

\*- data shifting -\*

for i = 42 to 2  
idc(i) = idc(i-1),

idc(1) = adcldc

if need to remove sensor drift then

\*- do the same work like shifting idc on iac and vcap -\*

shift whole group of iac and vcap data

iac(1) = iaca

iacb(1) = iacb

vcap(1) = vcapa

vcapb(1) = vcapb

swavg = swavg + 1, until swavg = 0  
fcount = fcount - 1

\*- output to be displayed data to global memory -\*

point to index

load begin address of variables

save address

load the data to be displayed

then send it to global memory

\*- recover previous registers -\*

enable interrupt

```

ADININT  LARP      00002h      ; point to AR2
         ADRK      00001h
         SST1      *+
         SST       *+
         SACH      *+
         SACL      *,0,3

         LAC        ADINNO
         ADDK      00001h
         SACL      ADINNO      ; adinno = adinno + 1, indicate one more data in
         LDPK      00000h      ; point to page 0
         LAC        DDR
         LDPK      00004h
         SFR
         SACL      *,0,2      ; DDR = 00xx xxxx xxxxx xxxxx
                                ; save data to global memory
                                ; *- recover previous registers -*

RECOVA   ZALS      *+
         ADDH      *+
         LST1      *+
         EINT
         RET
                                ; enable interrupt

.end
                                ; *** end of file ***

```

Table C-3 The List of DSP-1 Control Program.

```

.....
* Name      : DSP-1.ASM
* Function   : Interrupt (int0) service subroutine cooperates with DSP-2 and DSP-3, to send the
               "ready" signals to the sync. circuit all the time.
               The main tasks of communication with PC are performed by using the utilities wrote in
               the EPROM monitor program.
.....

               .title 'DSP-1 program'
IMR           .equ      00004h      ; page 0 (00000h-0007Fh)
SMARK         .equ      00060h
BCODE         .equ      00078h
VINT0         .equ      0007Ah

.....
*           initialization
.....

START         .sect      "P1INITI"
               DINT
               LDPK      00000h      ; point to data page 0
                                   ; *- initialize interrupt vector -*

               LALK      P1RP2IT
               SACL      VINT0
               LALK      0FF80h      ; load branch operating code
               SACL      BCODE
               LALK      03FF0h      ; load first vector address
               TBLW      BCODE      ; start to load interrupt vectors
               ADDK      00001h
               TBLW      VINT0
               LAC        IMR
               ORK        00001h      ; set enable mark for int0
               SACL      IMR

               OUT        SMARK,0Eh      ; *- send a interrupt signal to DSP-2 asking *-
                                   ; for starting parallel processing
               LACK      00040h      ; EPROM enter address is pushed on the top of stack
               PUSH
               EINT
               RET
                                   ; enable interrupt
                                   ; jump to the EPROM monitor programs

.....
* Subroutine : P1RP2IT.ASM response to the DSP-2 Interrupt call.
.....

               .sect      "P1RP2IT"
               LARP      00005h      ; *- save current registers -*
               LRLK      AR5,00300h
               SST1      *+
               SST       *+
               SACH      *+
               SACL      *+
               LAC        SMARK
               SACL      *

               LDPK      00000h      ; point to page 0
               LALK      00008h
               SUBK      00001h
               BGZ        HHDD1
               RXF

```



---

## REFERENCES

---

- [1] W. D. Cockrell, "Industrial Electronics Control", New York: McGraw-Hill Book Company, 1944.
- [2] E. W. Kimbark, "Direct Current Transmission", Vol. I, New York: John Wiley & Sons, Inc., 1971.
- [3] L. Gyugyi and B. R. Pelly, "Static Power Frequency Changers", New York: John Wiley & Sons, Inc., 1976.
- [4] L. Gyugyi, R. A. Otto, T. H. Putman, "Principles And Applications Of Static, Thyristor-Controlled Shunt Compensators", *IEEE Trans. Power Appar. Syst.*, Vol.PAS-97, No.5, pp.1935-1945, Sept/Oct 1980.
- [5] Canadian Electrical Ass., "Static Compensators For Reactive Power Control", Cantext Publications, 1984.
- [6] General Electric Company, "SCR Manual", Edited by D. R. Grafham and F. B. Golden, Sixth Edition, 1979.
- [7] W. McMurray, "SCR Inverter Commutated By An Auxiliary Impluse", *IEEE Trans. Communications and Electronics*, Vol.83, No.75, pp.824-829, 1964.
- [8] A. J. Humphrey, "Inverter Commutation Circuits", *IEEE Trans. Ind. Gener. Appl.*, Vol.IGA-4, No.1, pp.104-110, Jan/Feb 1968.
- [9] B. D. Bedford and R. G. Holf, "Principles Of Inverter Circuits", New York: John Wiley & Sons, Inc., 1964.
- [10] K. Heumann, "Development Of Inverters With Forced-Comutation For AC Motor Speed Control Up To The Megawatt Range", *IEEE Trans. Ind. Gener.*

- Appl.*, Vol.IGA-5, No.1, pp.61-67, Jan/Feb 1969.
- [11] J. M. D. Murphy and F. G. Turnbull, "Power Electronic Control Of AC Motors", Oxford: Pergamon Press, 1988, pp.4-5.
  - [12] N. Mohan, T. M. Undeland and W.P. Robbins, "Power Electronics: Converters, Applications, And Design", New York: John Wiley & Sons., Inc., 1989.
  - [13] B. K. Bose, "Recent Advances In Power Electronics", *IEEE Trans. Power Electron.*, Vol.PE-7, No.1, pp.2-16, Jan. 1992.
  - [14] A. Cogan and R. A. Blanchard, "Discrete Semiconductor Switches: Still Improving", *Powerconversion & Intelligent Motion*, 1986, pp.15-22.
  - [15] B. R. Pelly, "Power MOSFETs - A Status Review", *Int. Power Electron. Conf. Rec.*, Tokyo, 1983, pp.19-32.
  - [16] H. Yilmaz, J. L. Benjamin, K. Owyang, M. F. Chang and W. R. Van Dell, "Recent Advances In Insulated Gate Bipolar Transistor Technology", *IEEE- IAS Annu. Meeting Conf. Rec.*, Denver, Colorado, Sept. 1986, pp.345-349.
  - [17] D. A. Paice and K. E. Mattern, "Gate-Turn-Off Thyristors And Their Applications", *Int. Power Electron. Conf. Rec.*, 1984, pp.7-10.
  - [18] J. Nishizawa, K. Muraoka, T. Tamamushi and Y. Kawamura, "Low-Loss High-Speed Switching Devices, 2300V, 150A Static Induction Thyristor", *IEEE Trans. Electron. Devices*, Vol.ED-32, No.4, pp.822-830, April 1985.
  - [19] V. A. K. Temple, "MOS Controlled Thyristor - A New Class Of Power Devices", *IEEE Trans. Electron. Devices*, Vol.ED-33, No.10, pp.1609-1618, 1986.
  - [20] G. S. Buja and G. B. Indri, "Optimal Pulsewidth Modulation For Feeding AC Motors", *IEEE Trans. Ind. Appl.*, Vol.IA-13, No.1, Jan/Feb 1977.
  - [21] H. S. Patel and R. G. Hoft, "Generalized Techniques Of Harmonic

- Elimination And Voltage Control In Thyristor Inverters: Part I - Harmine Elimination", *IEEE Trans. Ind. Appl.*, Vol.IA-9, No.3, pp.310-317, May/June 1973.
- [22] J. Holtz, "Pulsewidth Modulation - A Survey", *IEEE Trans. Ind. Electron.*, Vol.IE-39, No.5, pp.410-420, Dec. 1992.
- [23] P. Wood, "Switching Power Converter", Litton Educational Publishing, Inc., 1981, pp.156.
- [24] T. Kanzaki, I. Yasuoka and G. Yamamoto, "Direct Digital Controlled PWM GTO Inverter For DC 1500 V Electric Cars", *Int. Power Electron. Conf. Rec.*, 1983, pp.1587-1598.
- [25] B. K. Bose, "Microcomputer Control Of Power Electronics And Drives", IEEE Press, 1987.
- [26] J. Holtz and B. Beyer, "The Optimal Pulsewidth Modulation For AC Servos And Low-Cost Industrial Drives", *IEEE-IAS Annu. Meeting Conf. Rec.*, Houston, Texas, Oct. 1992, pp.1010-1017.
- [27] Y. Murai, Y. Gohshi and I. Hosono, "High Frequency Split-Zerovector PWM With Harmonic Reduction For Induction Motor Drive", *IEEE-IAS Annu. Meeting Conf. Rec.*, San Diego, California, Oct. 1989, pp.396-401.
- [28] H. Kohlmeier, O. Niermeyer and D. Schroder, "High Dynamic Four Quadrant AC-Motor Drive With Improved Power Factor And NO-Line Optimized Pulse Pattern With PROMC", *IEEE Trans. Ind. Appl.*, Vol.IA-23, No.6, pp.1001-1009, Nov/Dec 1987.
- [29] H. Kohlmeier and D. Schroder, "Control Of A Double Voltage Inverter System Coupling A Three Phase Mains With An AC Drive", *IEEE-IAS Annu. Meeting Conf. Rec.*, Atlanta, Georgia, Oct. 1987, pp.593-599.
- [30] X. L. Ma, "High-Performance PWM Frequency Changers", *IEEE Trans. Ind. Appl.*, Vol.IA-22, No.2, pp.267-280, Mar/Apr 1986.

- [31] A. B. Plunkett, "A Current-Controlled PWM Transistor Inverter Drive", *IEEE-IAS Annu. Meeting Conf. Rec.*, Oct. 1979, pp.785-792.
- [32] B. T. Ooi, J. C. Salmon, J. W. Dixon and A. B. Kulkarni, "A Three-Phase Controlled Current PWM Converter With Leading Power Factor", *IEEE Trans. Ind. Appl.*, Vol.IA-23, No.1, pp.78-84, Jan/Feb 1987.
- [33] A. B. Kulkarni, J. W. Dixon, M. Nishimoto and B. T. Ooi, "Transient Tests On A Voltage Regulated Controlled-Current PWM Converter", *IEEE Trans. Ind. Electron.*, Vol.IE-34, No.3 pp.319-324, Aug. 1987.
- [34] M. Nishimoto, J. W. Dixon, A. B. Kulkarni and B. T. Ooi, "An Integrated Controlled-Current PWM Rectifier Chopper Link For Sliding Mode Position Control", *IEEE Trans. Ind. Appl.*, Vol.IA-23, No.5, pp.894-900, Sept/Oct 1987.
- [35] J. W. Dixon, A. B. Kulkarni, M. Nishimoto and B. T. Ooi, "Characteristics Of A Controlled-Current PWM Rectifier Inverter Link", *IEEE Trans. Ind. Appl.*, Vol.IA-23, No.6, pp.1022-1028, Nov/Dec 1987.
- [36] B. T. Ooi, J. W. Dixon, A. B. Kulkarni and M. Nishimoto, "An Integrated AC Drive System Using A Controlled Current PWM Rectifier-Inverter Link", *IEEE Trans. Power Electron.*, Vol.PE-3, No.1, pp.64-71, Jan. 1988.
- [37] O. Stihl and B. T. Ooi, "A single-Phase Controlled-Current PWM Rectifier", *IEEE Trans. Power Electron.*, Vol.PE-3, No.4, pp.453-459, Oct. 1988.
- [38] M. A. Boost and P. D. Ziogas, "State-Of-The-Art Carrier PWM Techniques: A Critical Evaluation", *IEEE Trans. Ind. Appl.*, Vol.IA-24, No.2, March/April 1988.
- [39] L. Moran, P. D. Ziogas and G. Joos, "Analysis And Design Of A Three-Phase Current-Source Solid-State Var Compensator", *IEEE Trans. Ind. Appl.*, Vol.IA-25, No.2, March/April 1989.
- [40] M. Hombu, S. Ueda, A. Ueda and Y. Matsuda, "A New Current-Source GTO Inverter With Sinusoidal Output Voltage And Current", *IEEE-IAS Annu.*

- Meeting Conf. Rec.*, Chicago, Illinois, Sept. 1984, pp.807-812.
- [41] M. Hombu, S. Ueda and A. Ueda, "A Current Source GTO Inverter With Sinusoidal Inputs And Outputs", *IEEE Trans. Ind. Appl.*, Vol.IA-23, No. 2, pp.247-255, Mar/Apr 1987.
- [42] C. Namuduri and P.C. Sen, "Optimal Pulse Width Modulation For Current-Source Inverters", *IEEE-IAS Annu. Meeting Conf. Rec.*, Toronto, Canada, Oct. 1985, pp.1087-1100.
- [43] S. Fukuda and N. Takada, "PWM Current-Source Rectifier With Sinusoidal Line Current", *IEEE-IAS Annu. Meeting Conf. Rec.*, Atlanta, Georgia, Oct. 1987, pp.679-684.
- [44] P.N. Enjeti, P.D. Ziogas, J.F. Lindsay, "Programmed PWM Techniques To Eliminate Harmonics - A Critical Evaluation", *IEEE-IAS Annu. Meeting Conf. Rec.*, Pittsburgh, Pennsylvania, Oct. 1988, pp.418-430.
- [45] P.N. Enjeti, P.D. Ziogas, J.F. Lindsay, "A Current Source PWM Inverter With Instantaneous Current Control Capability", *IEEE-IAS Annu. Meeting Conf. Rec.*, Pittsburgh, Pennsylvania, Oct. 1988, pp.927-933.
- [46] M. Iwahori and K. Kousaka, "Three-Phase Current-Source GTO Rectifier Adopting New PWM Control Techniques", *IEEE-IAS Annu. Meeting Conf. Rec.*, San Diego, California, Oct. 1989, pp.855-860.
- [47] P. Vas, "Vector Control Of AC Machines", Oxford Science Publications, 1990.
- [48] D. W. Novotny and R. D. Lorenz, "Introduction To Field Orientation And High Performance AC Drives", *IEEE-IAS Annu. Meeting Tutorial Course*, Denver, Sept. 1986, IEEE Inc., 1986
- [49] T. A. Lipo, "Recent Progress In The Development Of Solid-State AC Motor Drives", *IEEE Trans. Power Electron.*, Vol.PE-3, No.2, pp.105-117, April 1988.
- [50] A. Kusko, "Emergency/Standby Power Systems", McGraw-Hill Book



Company, 1989.

- [51] T. Kawabata, S. Doi, T. Morikawa, T. Nakamura and M. Shigenobu, "Large Capacity Parallel Redundant Transistor UPS", *Int. Power Electron. Conf. Rec.*, Vol.1, March 1983, pp.660-671.
- [52] J. Holtz, W. Lotzkat and K. H. Werner, "A High-Power Multi Transistor-Inverter Uninterruptible Power Supply System", *17th IEEE-PESC Rec.*, 1986, pp.311-320.
- [53] K. Fuliwara, R. G. Holf and H. Nomura, "Series Connected Bridge Converters Using Unequal AC Input Voltages And Optimum Sequence Control", *IEEE-IAS Annu. Meeting Conf. Rec.*, Atlanta, Georgia, Oct. 1987, pp.641-647.
- [54] J. A. Wilson, "The Forced Commutated Inverter As A Regenerative Rectifier", *IEEE Trans. Ind. Appl.*, Vol.IA-14, No.4, pp.335-340, Jul/Aug 1978.
- [55] E. P. Wiechmann, P. D. Ziogas and V. R. Stefanovic, "A Novel Bilateral Power Conversion For Variable Frequency Static Power Supplies", *IEEE Trans. Ind. Appl.*, Vol.IA-21, No.5, pp.1226-1233, Sept/Oct 1985.
- [56] L. Malesani and P. Tenti, "Three-Phase AC/DC PWM Converter With Sinusoidal AC Current And Minimum Filter Requirements", *IEEE Trans. Ind. Appl.*, Vol.IA-23, No.1, pp.71-77, Jan/Feb 1987.
- [57] S. K. Biswas, M. S. Mahesh and B. S. Ramakrishna, "A Three-Phase GTO AC To DC Converter With Input Displacement Factor And Output Voltage Control", *IEEE-IAS Annu. Meeting Conf. Rec.*, Atlanta, Georgia, Oct. 1987, pp.684-690.
- [58] J. W. Dixon and B. T. Ooi, "Indirect Current Control Of Unity Power Factor Sinusoidal Current Boost Type Three-Phase Rectifier", *IEEE Trans. Ind. Electron.*, Vol.IE-35, No.4, pp.508-515, Nov. 1988.
- [59] J. W. Dixon and B. T. Ooi, "Dynamically Stabilized Indirect Current Controlled SPWM Boost Type 3-Phase Rectifier", *IEEE-IAS Annu. Meeting*

- Conf. Rec.*, Pittsburgh, Pennsylvania, Oct. 1988, pp.700-705.
- [60] J. W. Dixon and B. T. Ooi, "Series And Parallel Operation Of Hystersis Current-Controlled PWM Rectifier", *IEEE Trans. Ind Appl.*, Vol.IA-25, No.4, pp.644-651, Jul/Aug 1989.
- [61] Z. C. Zhang, J. B. Kuang, X. Wang and B. T. Ooi, "Force Commuataed HVDC And SVC Based On Phase-Shifted Multi-Converter Modules", *IEEE-PES Winter Meeting*, New York, New York, Feb. 1991, 91 WM 119-8 PWRD.
- [62] C. Adamson and N. G. Hingorani, "High Voltage Direct Current Power Transmission", Garraway Ltd., England, 1960.
- [63] J. Arrillaga, "High Voltage Direct Current Transmission", Peter Peregrinws Ltd., 1983.
- [64] A. Gole and R. Menzies, "Analysis Of Certain Aspects Of Force Commutated HVDC Inverters", *IEEE Trans. Power Appl. Soc.*, Vol.PAS-100, No.5, pp.2258-2262, May 1981.
- [65] H. M. Turanli, R. W. Menzies and D. A. Woodford, "Feasibility Of DC Transmission With Forced Commutation To Remote Loads", *IEEE Trans. Power Appl. Soc.*, Vol.PAS-103, No.6, pp.1256-1262, June 1984.
- [66] K. S. Tam and R. Lasseter, "Implementation Of The Hydrid Inverter For HVDC/Weak AC System Interconnection", *IEEE Trans. Power Delivery*, Vol.PWRD-1, No.4, pp.259-267, Oct. 1986.
- [67] N. Kimura, "Dynamic Behavior Of HVDC System Using Forced Commutation Converter", *Int. Power Electron. Conf. Rec.*, Tokyo, 1990, pp.1243-1250.
- [68] Y. Tokiwa, K. Suzuki, T. Kawai and C. Tanaka, "Application Of Self-Commuated Converter Using SI-Thyristor On A HVDC Transmission System", *Int. Power Electron. Conf. Rec.*, Tokyo, 1990, pp.1258-1267.
- [69] B. M. M. Mwinyiwiwa, P. M. Birks and B. T. Ooi, "Delta Modulated Buck

- Type PWM Converter", *IEEE-IAS Annu. Meeting Conf. Rec.*, San Diego, California, Oct. 1989, 885-890.
- [70] B. T. Ooi, B. M. M. Mwinyiwiwa, X. Wang and G. Joos, "Operating Limits Of The Current-Regulated Delta-Modulated Current-Source PWM Rectifier", *IEEE Trans. Ind. Electron.*, Vol.IE-38, No.4, pp.268-274, August 1991.
- [71] S. Z. Dai, N. Lujara and B. T. Ooi, "A Unity Power Factor Current-Regulated PWM Rectifier With A Notch Feedback For Stabilization And Active Filtering", *IEEE Trans. Power Electron.*, Vol.PE-7, No.2, pp.356-363, April 1992.
- [72] B. M. M. Mwinyiwiwa, "Construction And Test Of A Delta Modulated Buck Type 3-Phase Converter", M.Eng. Thesis, McGill University, 1989.
- [73] X. Wang and B. T. Ooi, "Real-Time Multi-DSP Control Of Three Phase Current-Source Unity Power Factor PWM Rectifier", Accepted by the *IEEE Trans. Power Electron.* for publication.
- [74] B. T. Ooi and X. Wang, "Voltage-Source Type HVDC Transmission System", *Int. Power Electron. Conf. Rec.*, Tokyo, Japan, April 1990, pp.1251-1257.
- [75] B. T. Ooi and X. Wang, "Voltage Phase Angle Lock Loop Control Of the Boost Type PWM Converter For HVDC Application", *IEEE Trans. Power Electron.*, Vol.PE-5, No.2, pp.229-232, April 1990.
- [76] B. T. Ooi and X. Wang, "Boost Type PWM HVDC Transmission System", *IEEE Trans. Power Delivery*, Vol.PWRD-6, No.4, pp.1557-1563, Oct. 1991.
- [77] B. T. Ooi and X. Wang, "High Voltage Direct Current Transmission System Based On Voltage Source Converter", *21st IEEE-PESC Rec.*, Texas, June 1990, pp.325-332.
- [78] X. Wang and B. T. Ooi, "Unity PF Current-Source Rectifier Based On Dynamic Tri-Logic PWM", Accepted by the *IEEE Trans. Power Electron.* for publication.

- [79] B. M. Weedy, "Electric Power Systems", John Wiley & Sons Ltd., 1967.
- [80] P. M. Anderson and A. A. Fouad, "Power System Control And Stability", The Iowa State University Press, 1977.
- [81] K. Taniguchi and H. Irie, "Trapezoidal Modulating Signal For Three-Phase PWM Inverter", *IEEE Trans. Ind. Electron.*, Vol.IE-33, No.2, pp.193-200, May 1986.
- [82] Siemens AG, "High Voltage Direct Current Transmission (HVDC) References", Power Transmission and Distribution, E50001-U131-A7-X-7600.
- [83] L. Moran, P. D. Ziogas and G. Joos, "Analysis And Design Of A Three-Phase Synchronous Solid-State Var Compensator", *IEEE Trans. Ind. Appl.*, Vol.IA-25, No.4, pp.598-608, Jul/Aug 1989.
- [84] L. Moran, P. D. Ziogas and G. Joos, "Analysis And Design Of A Novel 3- $\phi$  Solid-State Power Factor Compensator And Harmonic Suppressor System", *IEEE Trans. Ind. Appl.*, Vol.IA-25, No.4, pp.609-619, Jul/Aug 1989.
- [85] C. K. Duffeg and R. P. Stratford, "Update Of Harmonic Standard IEEE-519 IEEE Recommended Practices and Requirements For Harmonic Control In Electric Power Systems", *IEEE-IAS Petroleum and Chemical Industry Conference*, Dallas, Sept. 1988.
- [86] X. Wang, S. Z. Dai and B. T. Ooi, "A Series Capacitive Reactance Compensators", *IEEE-IAS Annu. Meeting Conf. Rec.*, Dearborn, Michigan, Oct. 1991, pp.918-924.
- [87] B. T. Ooi and Z. C. Zhang, "Gain-Bandwidth Of SPWM Converters As Linear Amplifiers", Submitted to *IEEE Trans. Ind. Electronics*.
- [88] D. C. White and H. H. Woodson, "Electromechanical Energy Conversion", New York: John Wiley and Sons., Inc., 1959.
- [89] J. W. Dixon, "Boost Type PWM Rectifiers For High Power Applications", Ph. D.

Thesis, McGill University, June 1988.

- [90] B. Friedland, "Control System Design: An Introduction To State-Space Methods", McGraw-Hill Book Company, 1986.
- [91] K. J. Åström and B. Wittenmark, "Computer Controlled System: Theory And Design", Prentice/Hall International, Inc., 1984.
- [92] K. Ogata, "Discrete-Time Control Systems", Prentice-Hall, Inc., 1987.
- [93] S. R. Bowes and A. Midour, "Microprocessor Implementation Of New Optimal PWM Switching Strategy", *Proc. IEE, Pt.B*, Vol.135, No.5, pp.269-280, Sept. 1989.
- [94] Y. Guo, X. Wang, H. C. Lee and B. T. Ooi, "Concurrent Microprocessor-Based PWM Converter Control", *IEEE-LAS Annu. Meeting Conf. Rec.*, Seattle, Oct. 1990, pp.991-996.
- [95] Y. Guo, X. Wang, H. C. Lee and B. T. Ooi, "A Multiprocessor Digital Signal Processing System For Real-Time Power Converter Application", *IEEE Trans. Power Syst.*, Vol.7, No.2, pp.805-811, May 1992.
- [96] Y. Guo, X. Wang, H. C. Lee and B. T. Ooi, "Pole-Placement Control Of Voltage-Regulated PWM Rectifier Through Real-Time Multi-Processing", *Proc. IECON'91*, Kobe, Japan, Oct. 1991, pp.513-518.
- [97] "High Performance E<sup>2</sup>CMOS Generic Array Logic", Lattice Semiconductor Corporation.
- [98] C. L. Lehman, "Programmable Logic Design Tools", OrCAD Systems Corporation, 1989.
- [99] "TMS320C25 User's Guide", Texas Instruments Inc., 1986.
- [100] "TMS320C1X/TMS320C2X Assembly Language Tools - User's Guide", Texas Instruments Inc., 1987.